

Statistical Properties of Quasi-periodic Electromagnetic Ion Cyclotron Waves: ULF Modulation Effects

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Key Points:

- We conduct statistics of quasi-periodic EMIC waves modulated by compressional ULF waves
- Most ULF-modulated EMIC waves are observed on dayside magnetosphere at $L \in [8, 12]$
- We construct an empirical model for EMIC wave characteristics as a function of L -shell and MLT

Abstract

Electromagnetic ion cyclotron (EMIC) waves effectively scatter relativistic electrons in the Earth's radiation belts and energetic ions in the ring current. Empirical models parameterizing EMIC wave characteristics are important elements of inner magnetosphere simulations. Two main EMIC wave populations included in such simulations are the population generated by plasma sheet injections and another population generated by magnetospheric compression due to solar wind. In this study, we investigate a third class of EMIC waves, generated by hot plasma sheet ions modulated by compressional ultra-low-frequency (ULF) waves. Such ULF-modulated EMIC waves are mostly observed on the dayside, between magnetopause and the outer radiation belt edge. We show that ULF-modulated EMIC waves are weakly oblique (with wave normal angle $\approx 20^\circ \pm 10^\circ$) and narrow banded (with spectral width of $\sim 1/3$ of the mean frequency). We further construct an empirical model of EMIC wave characteristics as a function of L -shell and MLT. The low ratio of plasma frequency to electron gyrofrequency ($f_{pe}/f_{ce} \sim 5\text{--}10$) around the EMIC wave generation region does not allow these waves to scatter energetic electrons. However, these waves provide very effective (comparable to strong diffusion) quasi-periodic precipitation of plasma sheet protons.

1 Introduction

Electromagnetic ion cyclotron (EMIC) waves are the primary wave mode responsible for scattering and heating of cold ions (e.g., Kitamura et al., 2018; Ma et al., 2019) and precipitating relativistic electrons in the inner magnetosphere (see, e.g., Millan & Thorne, 2007; Usanova et al., 2014; Yahnin et al., 2017; Drozdov et al., 2022; Bashir et al., 2022; Angelopoulos et al., 2023, and references therein). These waves can be generated by hot, transversely anisotropic ions injected from the plasma sheet and drifting duskward (e.g., L. Chen et al., 2010; Jun et al., 2019; Bashir et al., 2022, and references therein). Such a localized EMIC generation region leads to the prevalence of EMIC-driven relativistic electron precipitation at the nightside/dusk flank (e.g., Blum et al., 2015; Yahnin et al., 2016; Capannolo et al., 2019, 2023). EMIC waves can also be generated by another mechanism on the dayside. This mechanism involves intense, compressional ultra-low-frequency (ULF) waves that may magnetically trap anisotropic, hot ion populations and transport them into the inner magnetosphere. Such ULF waves are often generated in response to the magnetopause impact by solar wind/magnetosheath transients (e.g., M. D. Hartinger et al., 2013, 2014; Wang et al., 2018; Wang, Nishimura, et al., 2019). Another ULF mode capable of hot ion trapping and transport is the drift mirror mode (e.g., Hasegawa, 1969): nonlinear mirror mode waves are local magnetic field depletions filled with transversely anisotropic hot ions (Rae et al., 2007; Balikhin et al., 2009; Soto-Chavez et al., 2019; Cooper et al., 2021). Nonlinear mirror waves are generated around the magnetopause and can transport trapped ion population earthward (due to convection electric field), where larger cold background density change the stability conditions of this population and may drive EMIC wave generation within mirror modes (Loto'Aniu et al., 2009; Kitamura et al., 2021; Z. Y. Liu et al., 2022; Yin et al., 2022).

In contrast to EMIC waves generated by plasma sheet ion injections (e.g., Jun et al., 2019, 2021) and thus parameterized by geomagnetic indexes and solar wind conditions (e.g., Usanova et al., 2012; Ma et al., 2015; H. Chen et al., 2019; Ross et al., 2021; Gamayunov et al., 2020), the ULF-associated EMIC waves are not expected to strongly correlate with geomagnetic conditions; instead, they should be mostly determined by day-side magnetosphere interaction with mesoscale (or even ion kinetic scale) transients. Thus, this EMIC wave population may be smoothed out in an index-based empirical model and requires alternative parameterization for further incorporation into simulations of the radiation belt dynamics in the inner magnetosphere. Such ULF-associated EMIC waves may play an important role in relativistic electron precipitation at higher L -shells, well outside the plasmapause (see statistics of relativistic electron precipitation events at high- L in Capannolo et al., 2022). Moreover, the small scale of mirror mode structures (the primary source of ULF-modulated EMIC waves), relative to the usually large-scale EMIC wave generation region (Blum et al., 2016, 2017) may explain the temporally and spatially localized EMIC-driven electron precipitation in observations (Shumko et al., 2022). Additionally, EMIC waves are also responsible for scattering and isotropization/precipitation of ring current ions (e.g., Jordanova et al., 2001, 2007; Khazanov et al., 2007). Therefore, EMIC wave modulation/generation within mirror mode structures indicates the solar wind impact on ring current dynamics.

This study aims to statistically investigate the characteristics of ULF-modulated EMIC waves, their spatial (in L -shell, MLT) distribution, and the associated plasma conditions. We utilize 5 years (2017-2021) of THEMIS E (Angelopoulos, 2008) measurements in the inner magnetosphere and near-Earth plasma sheet. The collected dataset contains 330 intervals with multiple EMIC bursts modulated by compressional ULF waves, with a total of 1555 individual bursts (each of them is within $\sim 1/2$ period of the simultaneously observed ULF wave). Section 2 describes typical events from our dataset, whereas Section 3 provides statistical properties of EMIC waves and surrounding plasma characteristics. The results are discussed and concluded in Section 4.

2 Spacecraft Instruments and Dataset

We examine data from three inner probes of THEMIS mission at an apogee of ~ 12 Earth radii (RE). These probes are equipped with identical instruments (Angelopoulos, 2008), and for investigation of EMIC waves we use: Fast Survey (1/4s sampling) measurements of the fluxgate magnetometer (FGM, see Auster et al., 2008), spin averaged (3s) measurements of ion and electron < 30 keV spectra and moments by the electrostatic analyzer (ESA, see McFadden et al., 2008), cold plasma density derived from the spacecraft potential (Bonnell et al., 2008; Nishimura et al., 2013). Ion temperature has been derived from combined measurements of ESA and solid state telescope (SST, see Angelopoulos et al., 2008). Our event selection criteria include: (1) search for quasi-periodic EMIC waves with at least three wave intensity peaks within one hour, (2) determine the ULF wave frequency range (within $[2.5, 20]$ mHz) exhibiting good correlation between ULF magnetic field minima and EMIC intensity peaks. Only events exhibiting such correlations are included in the dataset.

Figure 1 shows three typical events from the collected dataset. All are from the near-equatorial (B_z is the dominant component; see Panel (a)) transition region between the plasma sheet and the inner magnetosphere. The plasma frequency to electron gyrofrequency ratio, $f_{pe}/f_{ce} \in [5, 10]$, is typical for the near-Earth plasma sheet (see Panel (b)). Note that f_{pe}/f_{ce} derived from the spacecraft-potential density is much larger than f_{pe}/f_{ce} based on ESA density measurements, because a significant fraction of cold electrons are not measured by the ESA (McFadden et al., 2008).

Using magnetic field measurements, \mathbf{B} , we evaluate compressional fluctuations in the ULF frequency range: $\delta B_{\parallel} = (\mathbf{B} - \langle \mathbf{B} \rangle) \cdot \langle \mathbf{B} \rangle / |\langle \mathbf{B} \rangle|$. Panels (c) show quasi-periodic δB_{\parallel} variations with amplitudes of a fraction of nT, i.e., $\delta B_{\parallel} / |\langle \mathbf{B} \rangle| \sim 10^{-3}$. To evaluate δB_{\parallel} , we use the frequency range $[2.5, 20]$ mHz (i.e., $\langle \dots \rangle$ denotes 7 min averaging). For each event, we additionally check if changing the lower and upper-frequency limits (within the $[2.5, 20]$ mHz range) may improve the δB_{\parallel} correlation with EMIC wave intensity, and adjust these limits to maximize this correlation.

Such compressional ULF waves propagate in a hot, transversely anisotropic ion background (see Panels (d,e)), despite the low amplitude, can drive EMIC wave generation. Panels (f) show quasi-periodic EMIC bursts correlated with local minima of δB_{\parallel} , which are usually associated with enhanced hot transversely anisotropic ion population contributing to the pressure balance (e.g., Balikhin et al., 2009; Soto-Chavez et al., 2019). Wave ellipticity and polarization (panels (g,h)) confirm that these are classical, field-aligned EMIC waves.

Figure 2 zooms in several EMIC bursts from Fig. 1. All bursts are associated with local minima of ULF δB_{\parallel} , and such type of correlation has been found for all events in our dataset. Root mean square wave amplitude $\langle B_w \rangle = \left(\int_{f_{cp}/4}^{f_{cp}} B_w^2(f) df \right)^{1/2}$ is about 0.2–1 nT and mean wave frequency $\langle f \rangle = \int_{f_{cp}/4}^{f_{cp}} f B_w^2(f) df / \langle B_w \rangle^2$ is about 0.2–0.4 f_{cp} , quite typical for EMIC waves in the inner magnetosphere (see, e.g., Kersten et al., 2014; Zhang et al., 2016). For each wave burst, we also calculate wave frequency width $df = \int_{f_{cp}/4}^{f_{cp}} (f - \langle f \rangle)^2 B_w^2(f) df / \langle B_w \rangle^2$, mean wave normal angle WNA , and the dispersion of wave normal angles, $dWNA$. Wave bursts shown in Fig. 2 are quite narrow-banded with $df/\langle f \rangle < 1/5$ and weakly oblique with $WNA \approx 20^\circ \pm 10^\circ$. We determine these characteristics for all wave bursts in our dataset.

Figure 3 shows histograms for L -shell and MLT distributions for all datasets: ULF-modulated EMIC waves are mostly observed at high L -shells ($L > 8$) at the dayside sector (from 10 to 16), where compressional ULF waves are predominantly observed in response to solar wind transients and magnetopause oscillations (M. Hartinger et al., 2011; M. D. Hartinger et al., 2013; Wang et al., 2018; Wang, Nishimura, et al., 2019). At dawn

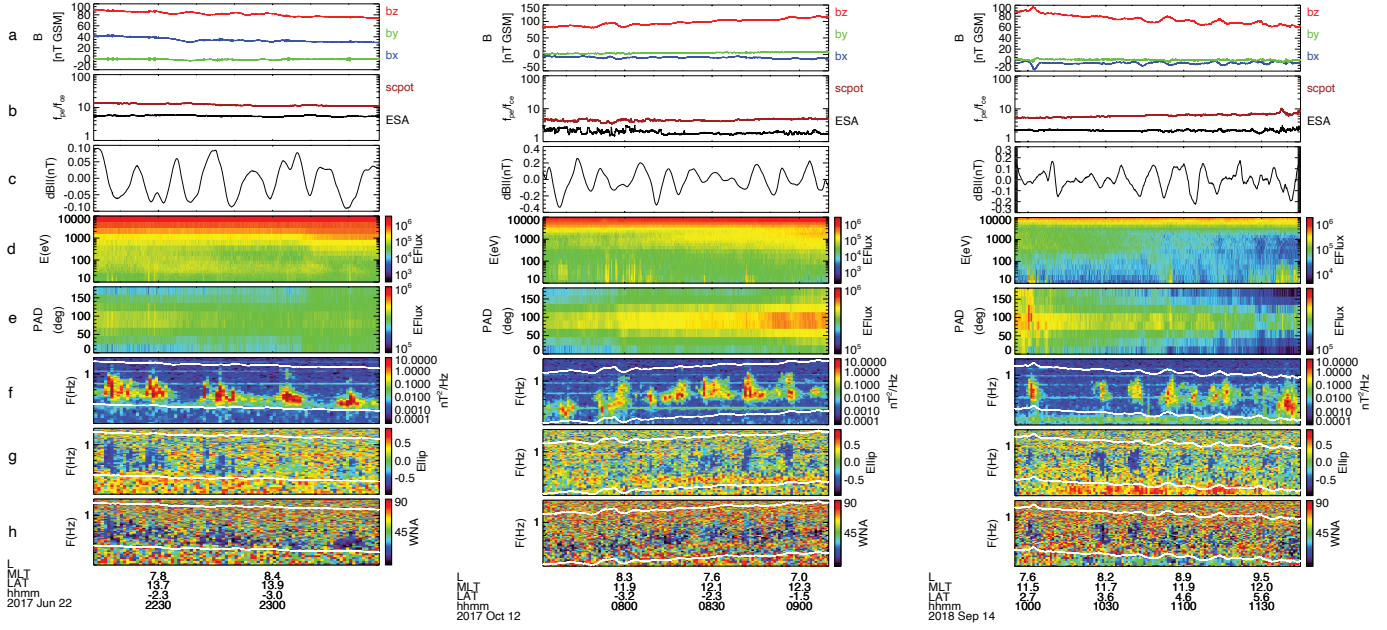


Figure 1. Three example events with quasi-periodic EMIC waves: (a) GSM magnetic field components, (b) f_{pe}/f_{ce} ratio, (c) ULF δB_{\parallel} field, (d) omni-directional spectrum of ions, (e) pitch-angle distribution of ~ 10 keV ions, (f) EMIC wave magnetic field spectrum with main frequencies shown in white, (g) EMIC wave ellipticity, (h) EMIC wave normal angle.

and dusk flanks, ULF-modulated EMIC waves are only observed at high L , whereas at the dayside sector such waves can be found even at $L \sim 5 - 6$.

3 Statistical properties of ULF-modulated EMIC waves

Figure 4 shows distributions of statistical properties of ULF-modulated EMIC waves. Burst-averaged wave amplitude (square root of the average wave intensity) is usually within $[50, 500]$ pT, but there are rare observations of very intense (~ 1 nT) waves (see panel (a)). These are typical intensities of the inner magnetosphere EMIC waves (Zhang et al., 2016; Jun et al., 2019). Most waves are observed in quite rarefied plasma environment with $f_{pe}/f_{ce} < 10$ (see panel (b)), typical in the plasma sheet, but much smaller than f_{pe}/f_{ce} in plasmaspheric density plumes (typical generation region of EMIC waves Usanova et al., 2013; Halford et al., 2015). As f_{pe}/f_{ce} controls the electron resonant energies for EMIC waves, small $f_{pe}/f_{ce} < 10$ would not allow EMIC waves to scatter ≤ 1 MeV electrons (Summers & Thorne, 2003), and only a small population of observations with $f_{pe}/f_{ce} > 15$ can explain the ≤ 1 MeV electron precipitation.

Most ULF-modulated EMIC waves are moderately oblique with $WNA \in [30^\circ, 60^\circ]$, with quite a small variation of wave normal angle, $dWNA \sim 7^\circ$ (see panels (c,d)). Such obliqueness may affect relativistic electron scattering by EMIC waves (Khazanov & Gamayunov, 2007; Gamayunov & Khazanov, 2007) and should be quite important for EMIC wave Landau resonance with warm electrons (Fu et al., 2018; Wang, Li, et al., 2019; Inaba et al., 2021) and plasma sheet ions (Ma et al., 2019; Usanova, 2021). The observed ULF-modulated EMIC wave frequencies and the frequency widths, $\langle f \rangle/f_{ce} \in [0.4, 0.55]$ and $\Delta f/f_{cp} \in [0.1, 0.2]$ (see panels (e,f)), are typical for EMICs in the inner magnetosphere (Kersten et al., 2014; Zhang et al., 2016).

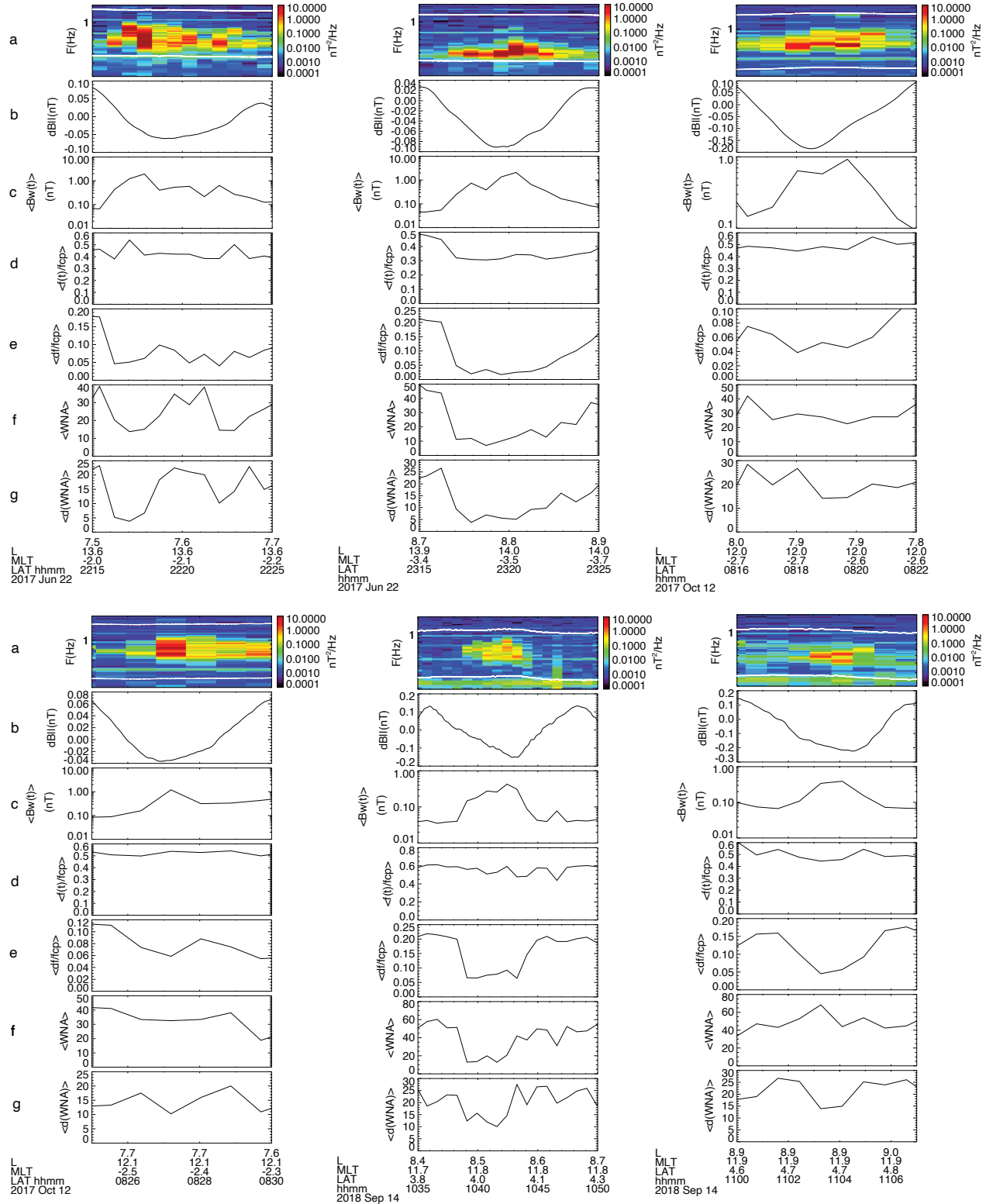


Figure 2. Characteristics of individual EMIC wave bursts associated with local δB_{\parallel} minima for three events from Fig. 1: (a) EMIC wave intensity $\langle B_w^2 \rangle$, (b) ULF field minima, (c) EMIC wave amplitude, (d) EMIC wave mean frequency normalized to f_{cp} , (e) width of EMIC wave mean frequency normalized to f_{cp} , (f) EMIC wave mean wave normal angle, and (g) width of the wave normal angle distribution.

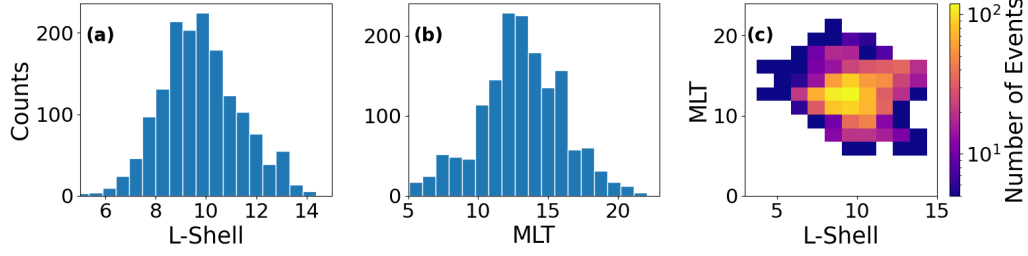


Figure 3. Distribution of events (individual EMIC wave bursts associated with ULF δB_{\parallel} minimum): (a) L -shell distribution, (b) MLT distribution, and (c) distribution of the total number of events in (L, MLT) plane.

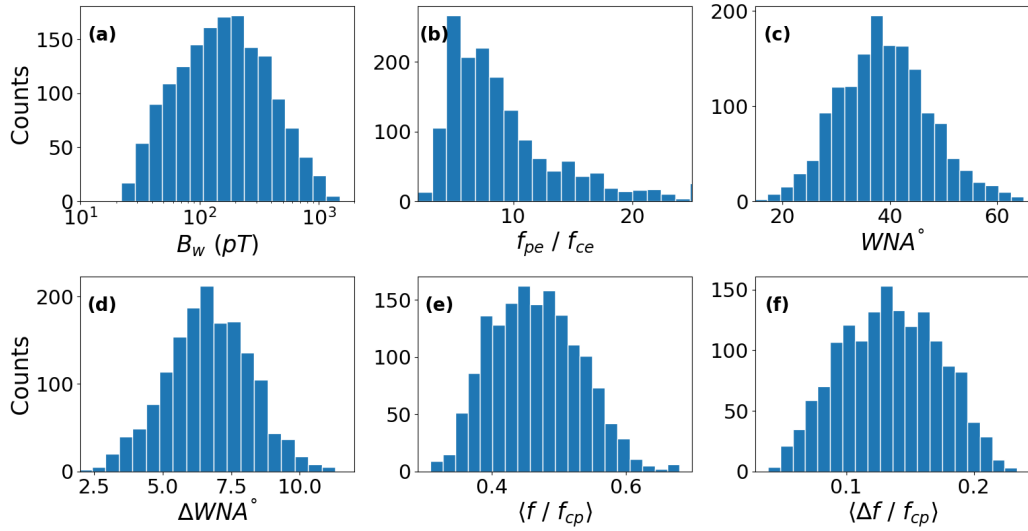


Figure 4. (a) Distributions of EMIC wave amplitudes $\sqrt{\langle B_w^2 \rangle}$, (b) f_{pe}/f_{ce} ratio, (c) mean wave normal angle, (d) width of the wave normal angle distribution, (e) mean wave frequency $\langle f/f_{cp} \rangle$, and (f) wave frequency width $\langle \Delta f/f_{cp} \rangle$.

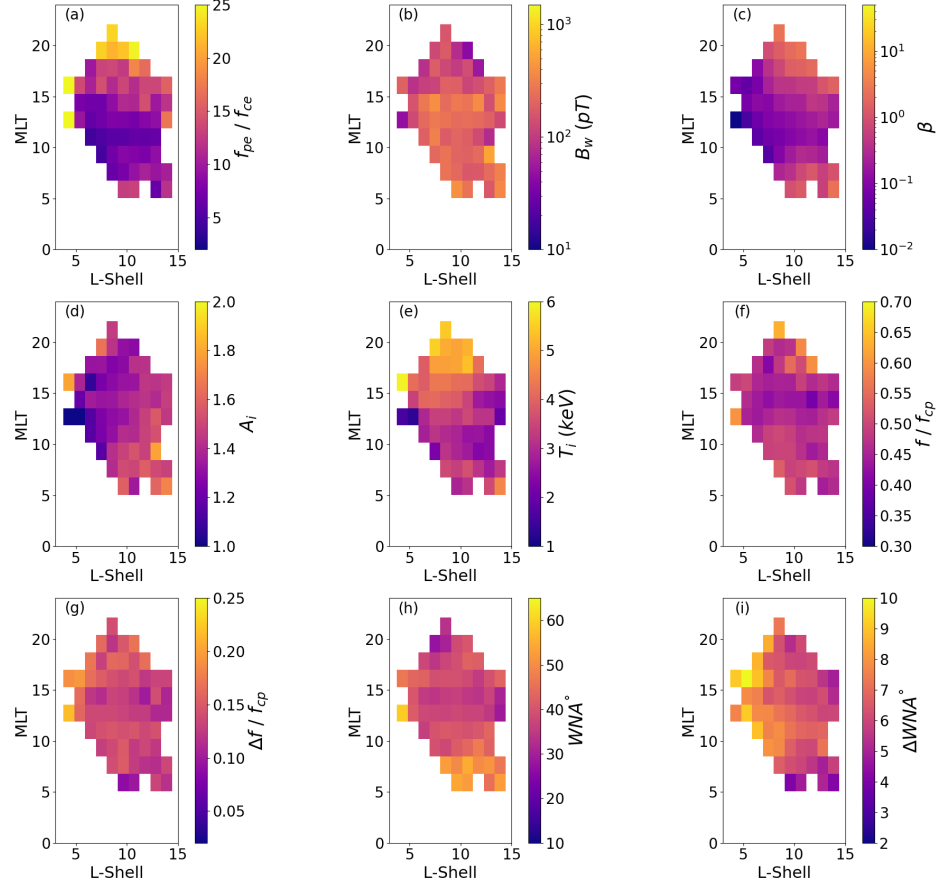


Figure 5. Distributions of main wave characteristics from Fig. 4 in (L, MLT) plane. (a) f_{pe}/f_{ce} , (b) wave amplitude B_w , (c) plasma β_i , (d) temperature anisotropy, (e) ion temperature in keV, (f) normalized wave frequency, (g) normalized width of wave frequency, (h) wave normal angle, (i) width of wave normal angle.

Figure 5 shows the spatial distribution of all wave and background plasma/magnetic field characteristics. There is a clear dawn-dusk asymmetry of f_{pe}/f_{ce} and ion temperature T_i for ULF-modulated EMIC events: f_{pe}/f_{ce} is about 10 at the dawn flank and increases to 20 at the dusk flank; T_i is about 3 keV at the dawn flank and increases to 5 keV at the dusk flank. The root mean square amplitude is slightly larger on the dawn flank, $\langle B_w \rangle \sim 200$ pT, than on the dusk flank, $\langle B_w \rangle \sim 50$ pT. Ion $\beta = 8\pi n T_i / B_0^2$ maximises at flanks, $\beta_i \sim 10$, and has a minimum at dayside and at low L , $\beta_i < 1$. Ion temperature anisotropy, the key parameter for wave generation, has a maximum at dawn flank, $A_i = T_{i,\perp} / T_{i,\parallel} \sim 1.6$. This peak of A_i most likely explains the dawn flank peak of $\langle B_w \rangle$.

Panels (h-l) in Fig. 5 show the distribution of the main wave characteristics. Mean wave frequency $\langle f \rangle / f_{cp}$ and frequency width df / f_{cp} do not vary much with MLT : for example, there is only a slightly lower $\langle f \rangle / f_{cp} \approx 0.4$ at the dusk flank, in comparison with $\langle f \rangle / f_{cp} \approx 0.5$ on the dawn-side. However, there is a clear gradient of wave normal angle with MLT : waves at the dusk flank are more field-aligned with $WNA \approx 35^\circ$ than in the dawn flank, where $WNA \approx 55^\circ$. Interestingly, the wave normal angle variation, $dWNA$, does not depend on MLT , but increases at lower L -shells, from $dWNA \sim 5^\circ$ at $L \sim 12$ to $dWNA \sim 10^\circ$ at $L \sim 5$.

Distributions of the main wave characteristics shown in Fig. 5 can be used to estimate the ion diffusion rates that would describe plasma sheet and ring current ion precipitation via resonant scattering by ULF-modulated EMIC waves. To enable the evaluation of diffusion rates, we fit the normalized wave intensity $(B_w/B_0)^2$, mean wave frequency and frequency distribution width, $\langle f \rangle/f_{cp}$ and $\Delta f/f_{cp}$, and plasma to electron cyclotron frequency ratio, f_{pe}/f_{ce} , as function of MLT and L . We use the following fitting function

$$F = a_0 + a_1 \cdot (L/10) + a_2 \cdot MLT + a_3 \cdot (L/10) \cdot MLT + a_4 \cdot (L/10)^2 \cdot MLT + a_5 \cdot (L/10) \cdot MLT^2 \quad (1)$$

that capture main L and MLT gradients of wave characteristics. Note that these fittings only work within the region of ULF-modulated EMIC wave observations: $MLT \in [5, 20]$, $L \in [5, 12]$, with two boundaries $MLT_- = 15 - L$ and $MLT_+ = 10 + L$. Table 1 shows the coefficients of these fittings.

Parameters	a_0	a_1	a_2	a_3	a_4	a_5
f_{pe}/f_{ce}	-2.32	22.79	0.75	-3.72	0.26	0.13
$B_w(\text{pT})$	0.26	-0.21	0.01	0.00	0.01	0.00
β	1.22	2.83	-0.05	-0.67	0.07	0.02
A_i	0.67	1.05	0.00	0.03	-0.01	0.00
$T_i(\text{keV})$	-0.25	5.44	0.03	-0.13	-0.34	0.02
f/f_{cp}	0.94	-0.18	-0.03	0.00	0.00	0.00
$\Delta f/f_{cp}$	0.22	-0.05	0.00	0.00	0.00	0.00
WNA°	67.06	16.19	-1.16	-5.88	0.93	0.19
$dWNA^\circ$	11.83	-8.00	0.06	0.22	0.19	-0.02

Table 1. Coefficients from fitting EMIC wave characteristics, see Eq. (1).

Using these fittings of EMIC wave characteristics, we can quantify the wave contribution to plasma sheet and ring current ion losses. For this reason, we evaluate pitch-angle diffusion rates due to cyclotron-resonant interaction with EMIC waves. We use a simplified formula by assuming the waves as field-aligned, although some of them are weakly oblique (see Summers et al., 2007, for equations of diffusion coefficients in the quasi-linear theory):

$$D_{\alpha\alpha} = \frac{\pi}{2} \frac{1}{c\beta} \frac{\Omega_{cp}^2}{|\Omega_{ce}|} \frac{1}{(E+1)^2} \frac{R(1 - \frac{x \cos \alpha}{y\beta})^2 |F(x, y)|}{\delta x |\beta \cos \alpha - F(x, y)|} e^{-(\frac{x-x_m}{\delta x})^2}$$

where $x = f/f_{cp}$, $y = kc/2\pi f_{cp}$, E is the dimensionless particle kinetic energy given by $E = E_k/(m_i c^2) = \gamma - 1$, $\beta = [E(E+2)]^{1/2}/(E+1)$, $R = B_w^2/B_0^2$ is the ratio of the energy density of the wave magnetic field to that of the background field, i.e., the relative wave power; $x_m = \langle f \rangle/f_{cp}$, $\delta x = \Delta f/f_{cp}$, and $F(x, y) = dx/dy$ is determined from the cold plasma dispersion of EMIC waves (Stix, 1962). The diffusion rate $D_{\alpha\alpha}$ evaluated at the loss-cone pitch-angle, $\alpha_{LC}(L)$, determines the rate of wave-driven ion precipitation into the atmosphere (Kennel & Petschek, 1966). This diffusion rate can be compared with the so-called strong diffusion rate (Summers & Thorne, 2003)

$$D_{SD} = \frac{9.66}{L^4} \left[\frac{4L}{4L-3} \right]^{1/2} \frac{[E(E+2)]^{1/2}}{(E+1)}$$

that determines the maximum possible precipitation rate in the diffusion regime (Kennel & Petschek, 1966; Kennel, 1969). Figure 6 shows diffusion rates $D_{\alpha\alpha}$ and $D_{\alpha\alpha}/D_{SD}$ at four ion energies and $\alpha_{LC}(L)$. At $MLT \in [5, 15]$ and $L > 10$, ULF-modulated EMIC waves provide very strong $D_{\alpha\alpha} \sim 10^{-3} \text{s}^{-1}$, above the strong diffusion limit ($D_{\alpha\alpha}/D_{SD} >$

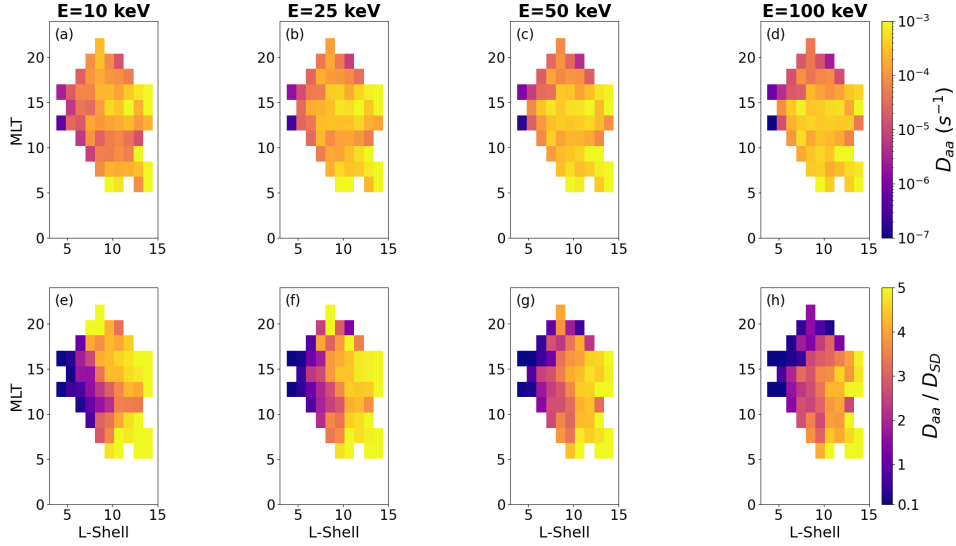


Figure 6. Distribution of pitch-angle diffusion coefficients in (L, MLT) plane at E (10, 25, 50, 100) keV (a-d) $D_{\alpha\alpha}$ distribution (e-h) $D_{\alpha\alpha}/D_{SD}$ distribution.

1). Thus, when these waves are present (i.e., when sufficiently strong ULF waves transport hot anisotropic ions and EMIC waves), they will drive the modulated ion (proton) losses for a wide energy range. Such losses can be observed as day-side proton aurora forms (e.g., Sigernes et al., 1996; Lorentzen & Moen, 2000; Berchem et al., 2003; Frey, 2007).

4 Discussion and Conclusions

In this study, we examine a specific class of EMIC waves modulated by compressional ULF waves. The likely scenario for such EMIC wave generation includes the day-side magnetopause impact by solar wind transients that drive compressional ULF waves (presumably drift mirror mode waves Rae et al., 2007; Balikhin et al., 2009; Soto-Chavez et al., 2019; Cooper et al., 2021), and these ULF waves transport the hot, transversely anisotropic ion population to lower L -shells, where the ion anisotropy is released in the form of EMIC wave generation (see examples in Loto'Aniu et al., 2009; Kitamura et al., 2021; Z. Y. Liu et al., 2022; Yin et al., 2022). This scenario is confirmed by the prevalence of ULF-modulated EMIC waves at large L -shells ($L \in [8, 12]$) on the day-side $MLT \in [10, 16]$. Therefore, we may suggest that such ULF-modulated EMIC waves constitute an additional class of EMICs, supplementing the two most investigated classes: EMICs generated on the dusk flank by plasma sheet injected ions and EMICs generated at low L -shells on the day-side by compressionally heated ions (e.g., Jun et al., 2019, 2021; N. Liu et al., 2022; Xue et al., 2022). The main feature of this new EMIC wave class is the periodicity of EMIC emission.

These ULF-modulated EMIC waves are moderately oblique ($WNA \in [30^\circ, 60^\circ]$), quite narrow-banded ($\Delta f/f \sim 0.3$ with $f/f_{cp} \in [0.4, 0.55]$), and moderately intense ($B_w \in [50, 300]$ pT). Due to their insufficiently-high wave amplitudes, these waves resonate with ions in the quasi-linear regime. The main ion population responsible for ULF-modulated EMIC wave generation is typical plasmasheet ions with energies $E_R \in [5, 15]$ keV. Due to the relatively small plasma density at high L , the frequency ratio f_{pe}/f_{ce} during ULF-modulated EMIC waves is about $\in [5, 10]$. This ratio controls the resonant energies for electrons interacting with EMIC waves, and when $f_{pe}/f_{ce} \in [5, 10]$ EMIC waves

cannot scatter relativistic or energetic electrons, but only ultra-relativistic electrons that are usually scarce in such high L -shells. Therefore, ULF-modulated EMIC waves are not effective in driving electron losses. However, these waves are very effective in scattering ions (pitch-angle diffusion rate reaches the strong diffusion limit for [10, 100]keV ions). Therefore, ULF-modulated EMIC waves can produce quasi-periodic ion precipitation contributing to day-side proton aurora (Sigernes et al., 1996; Lorentzen & Moen, 2000; Berchem et al., 2003; Frey, 2007). Further transported by ULF waves to lower L -shells, hot anisotropic ion population may generate EMICs within the outer radiation belt where these waves is expected to serve as the seed population for intense coherent EMIC waves (see discussions in Gamayunov & Engebretson, 2021, 2022).

Statistics of ULF-modulated EMIC waves demonstrate one more mechanism of direct solar wind impact on the Earth's magnetosphere (see discussions of other mechanisms in M. D. Hartinger et al., 2013, 2014; Wang et al., 2018; Wang, Nishimura, et al., 2019), which underlines the importance of including solar wind transients into models of inner magnetosphere dynamics and magnetosphere-ionosphere coupling.

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Open Research

THEMIS data is available at <http://themis.ssl.berkeley.edu>. Data access and processing was performed using SPEDAS V4.1, see Angelopoulos et al. (2019).

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Figure 1.

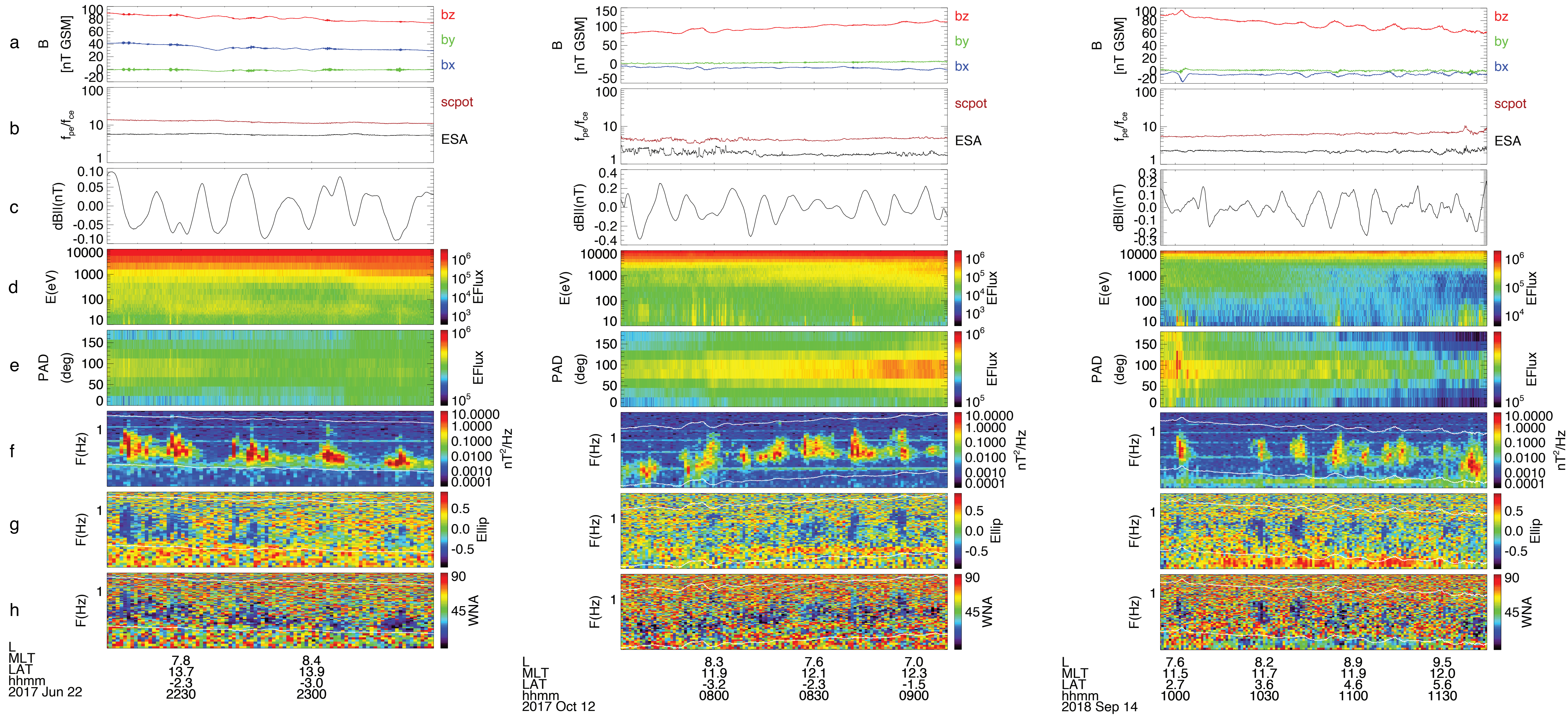


Figure 2.

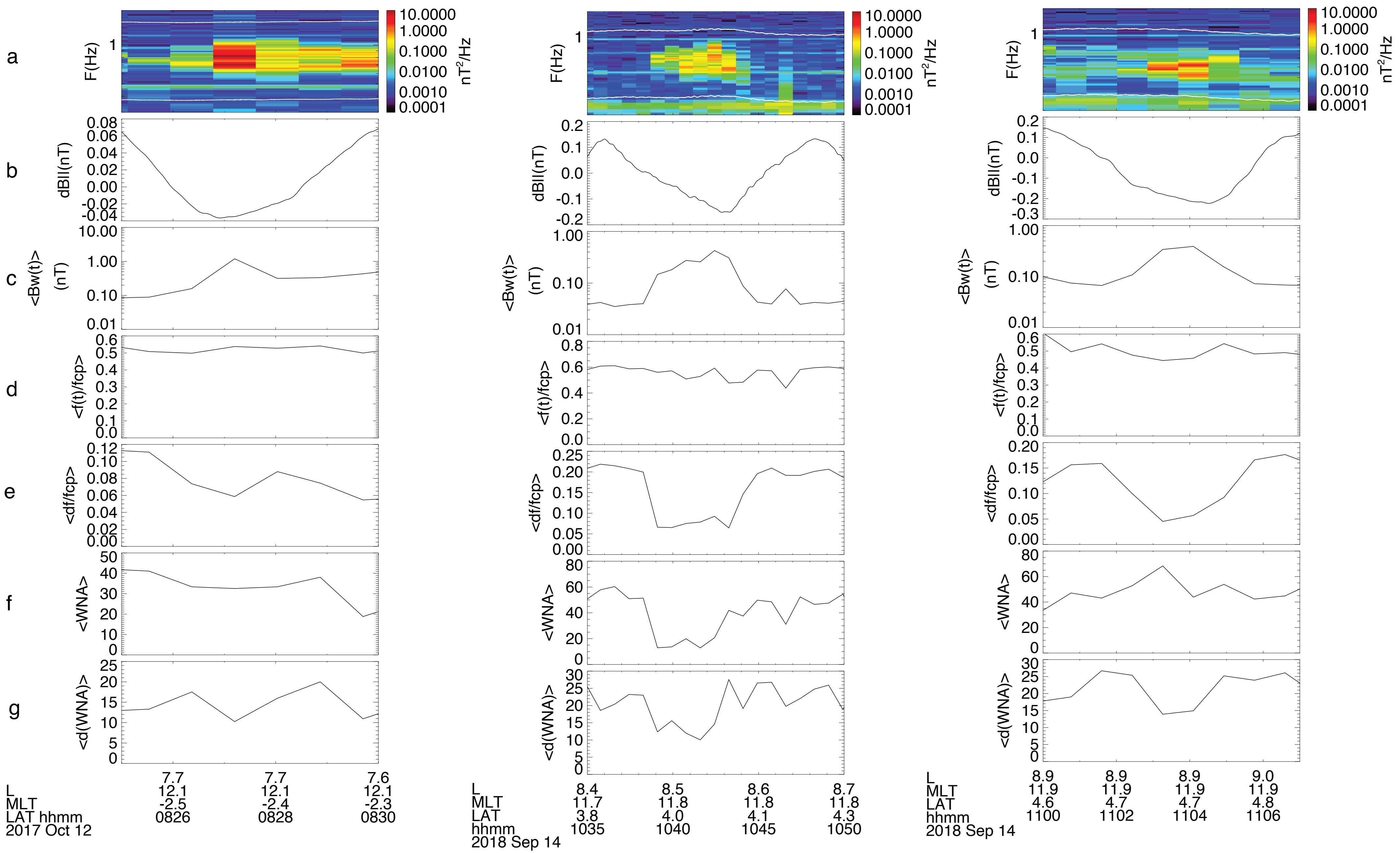
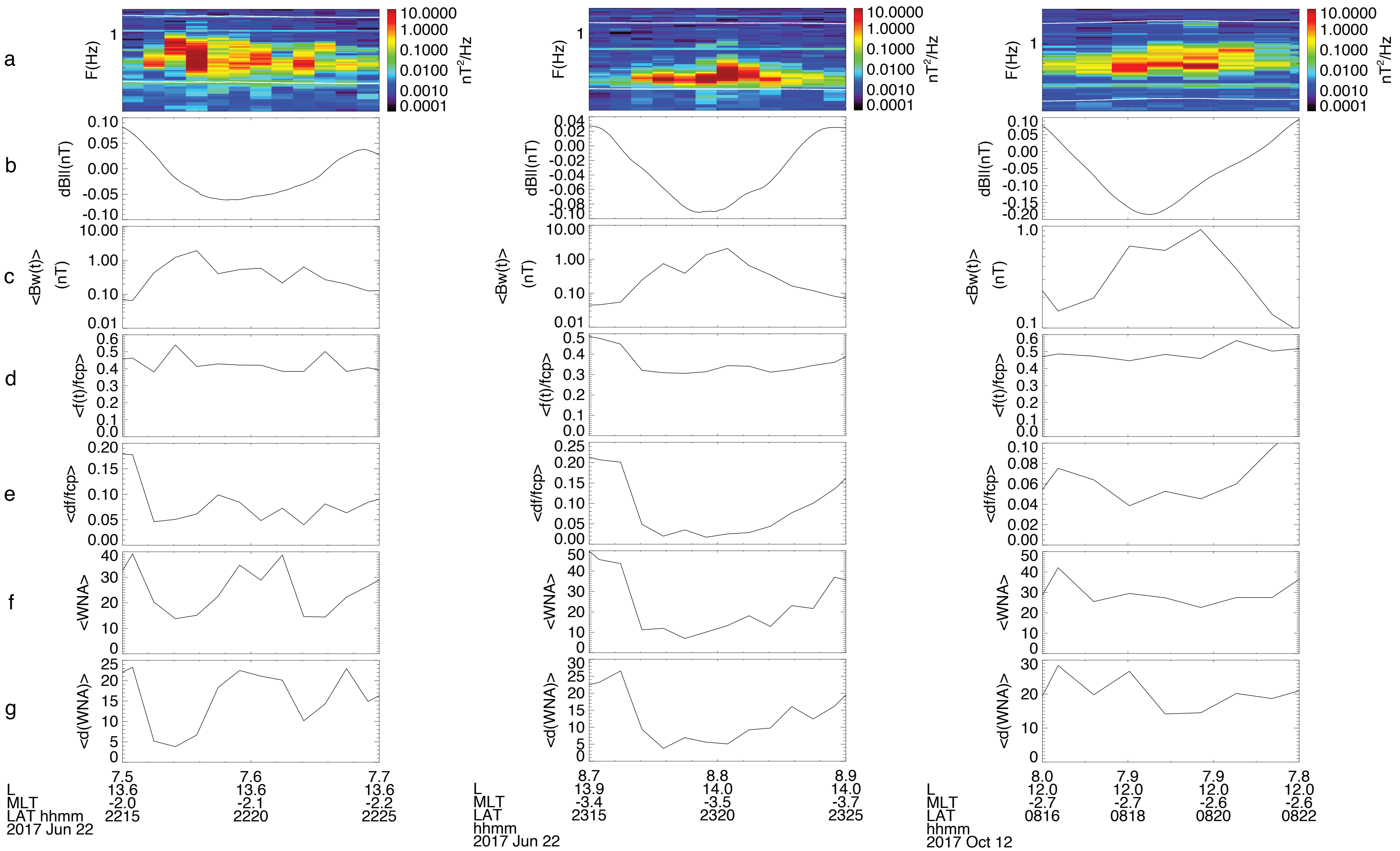


Figure 3.

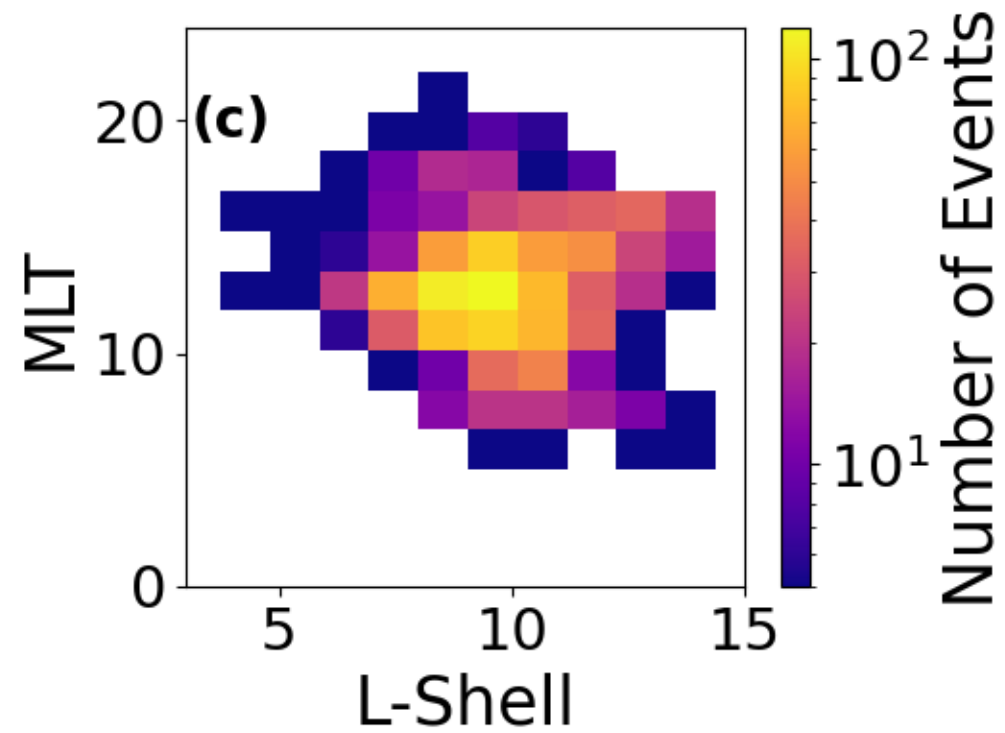
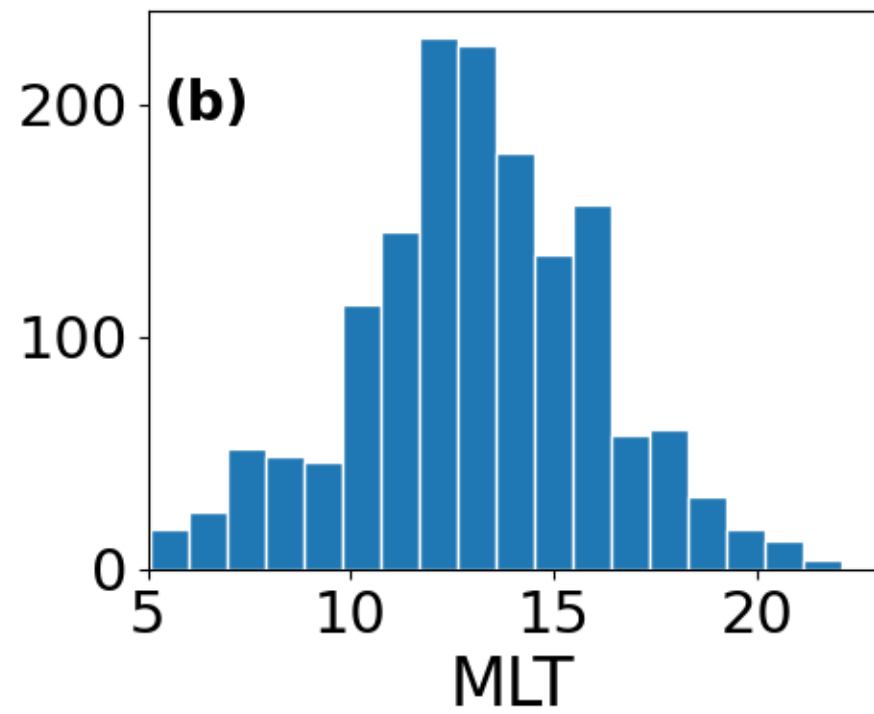
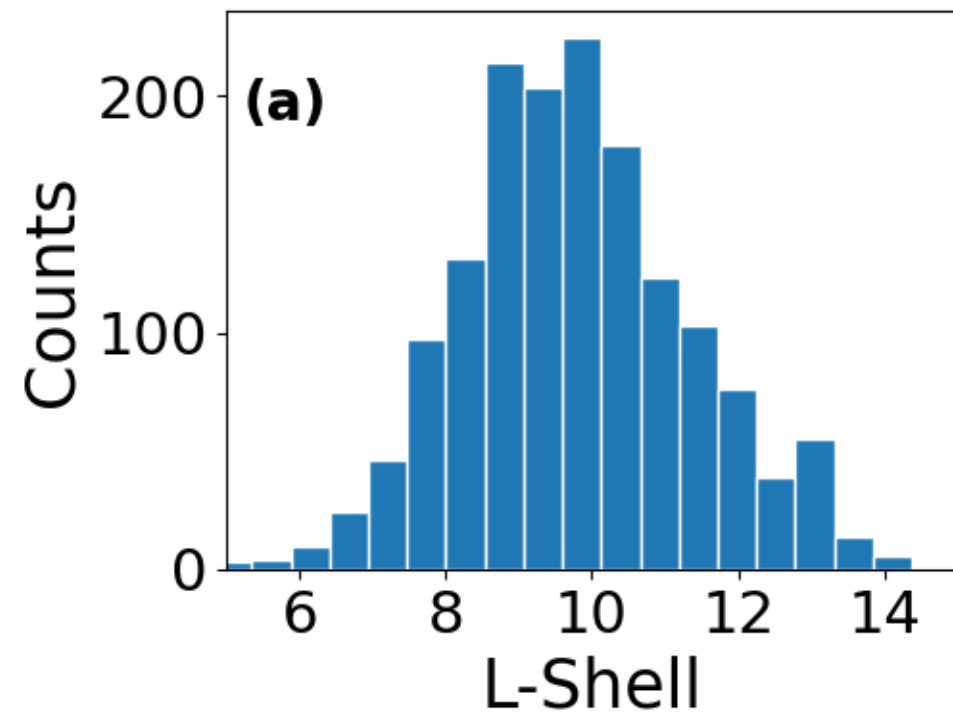


Figure 4.

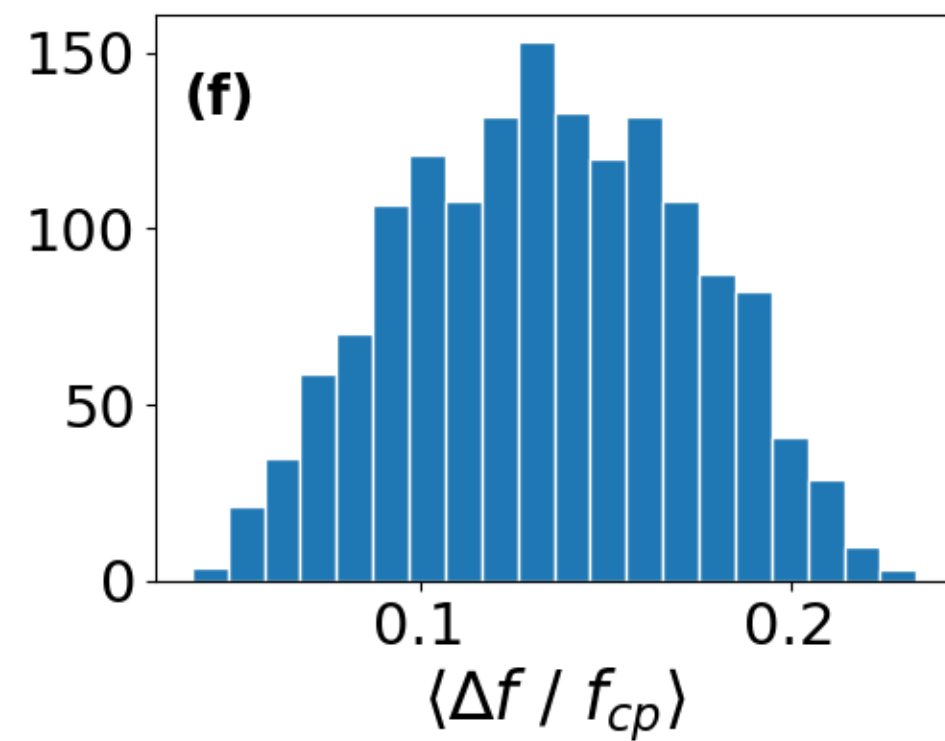
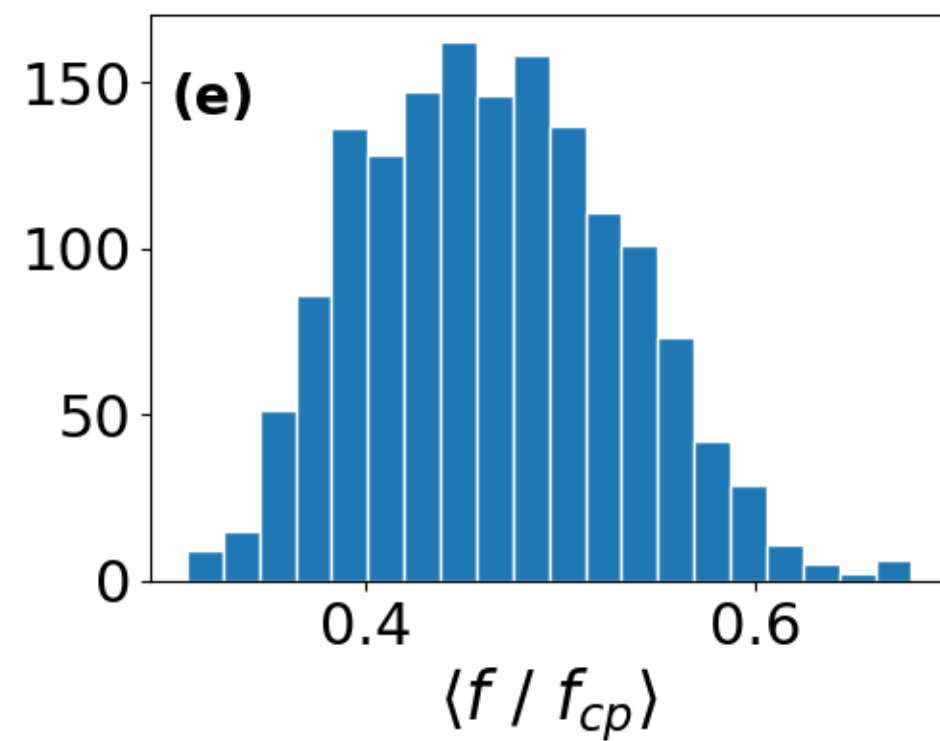
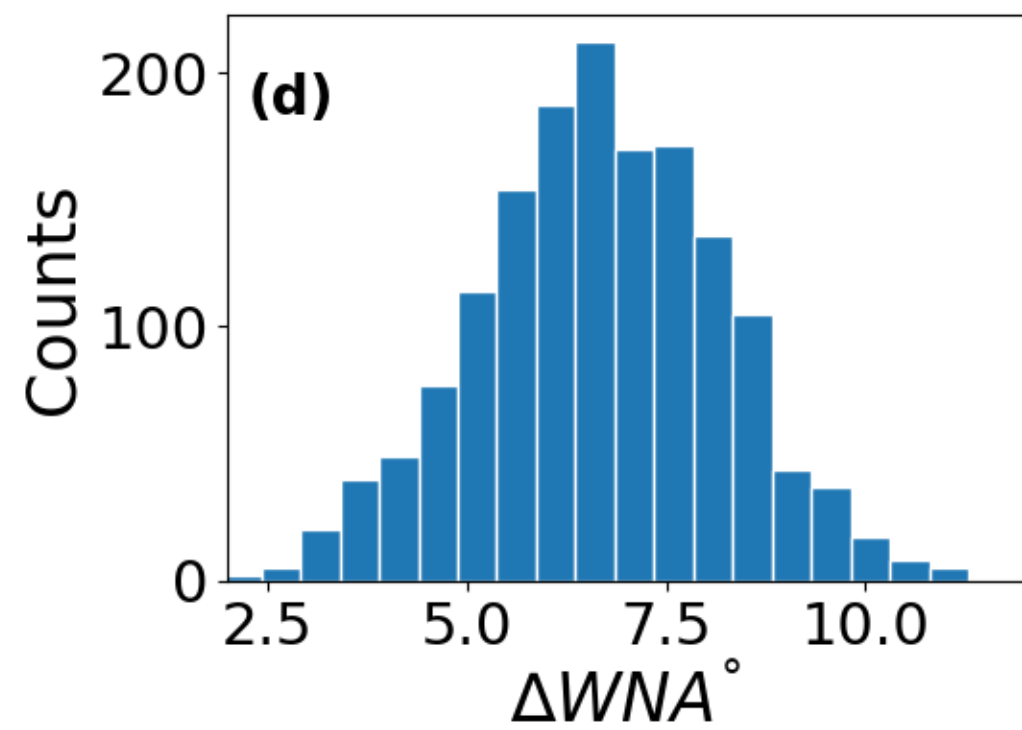
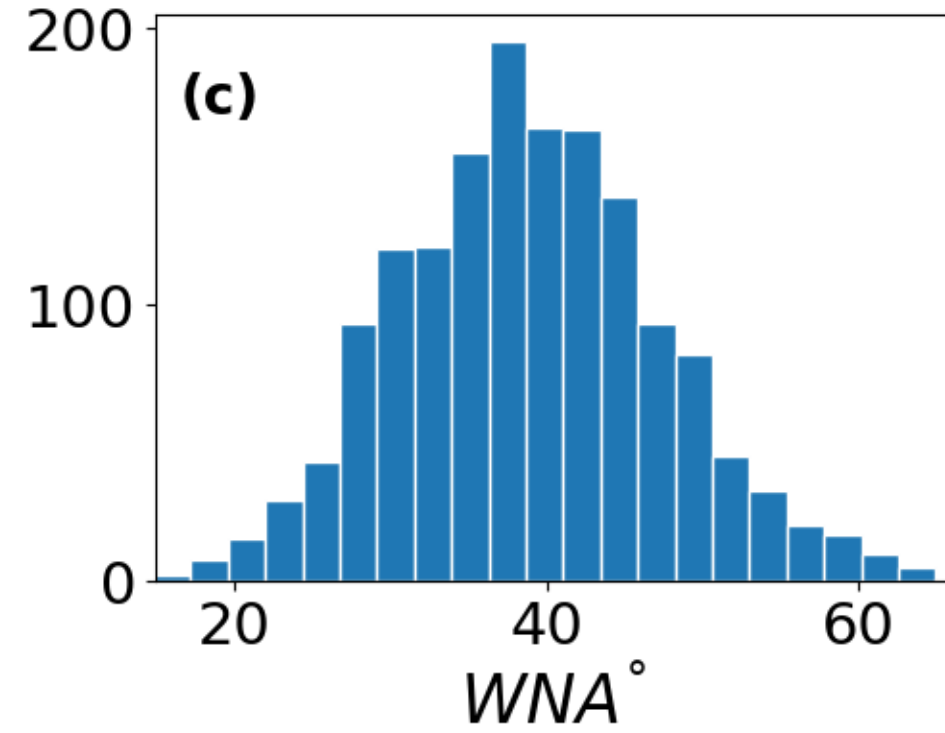
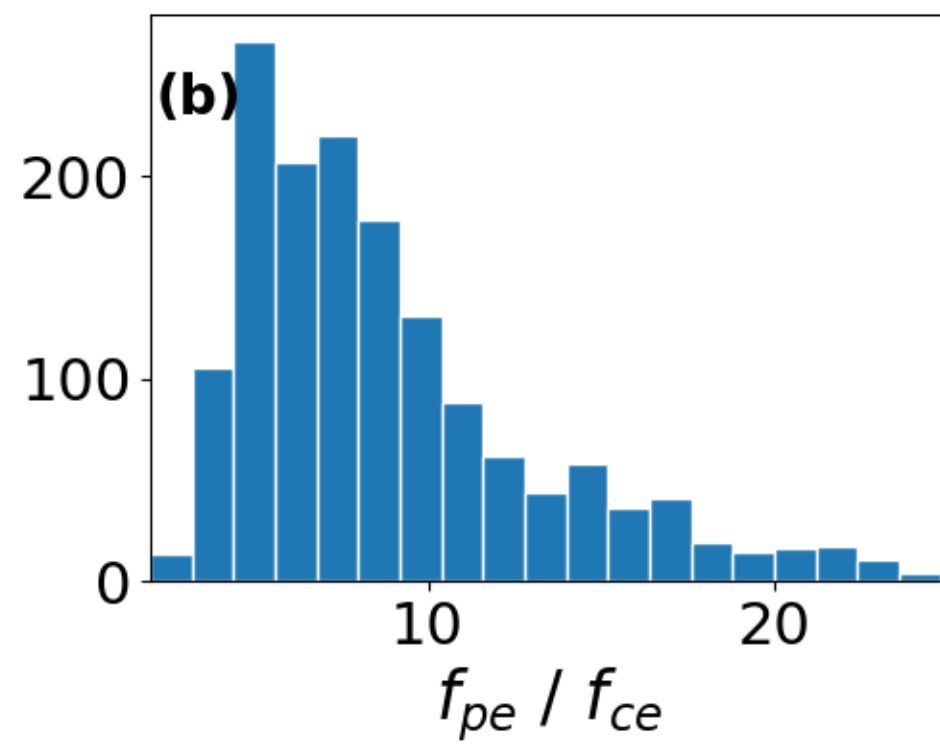
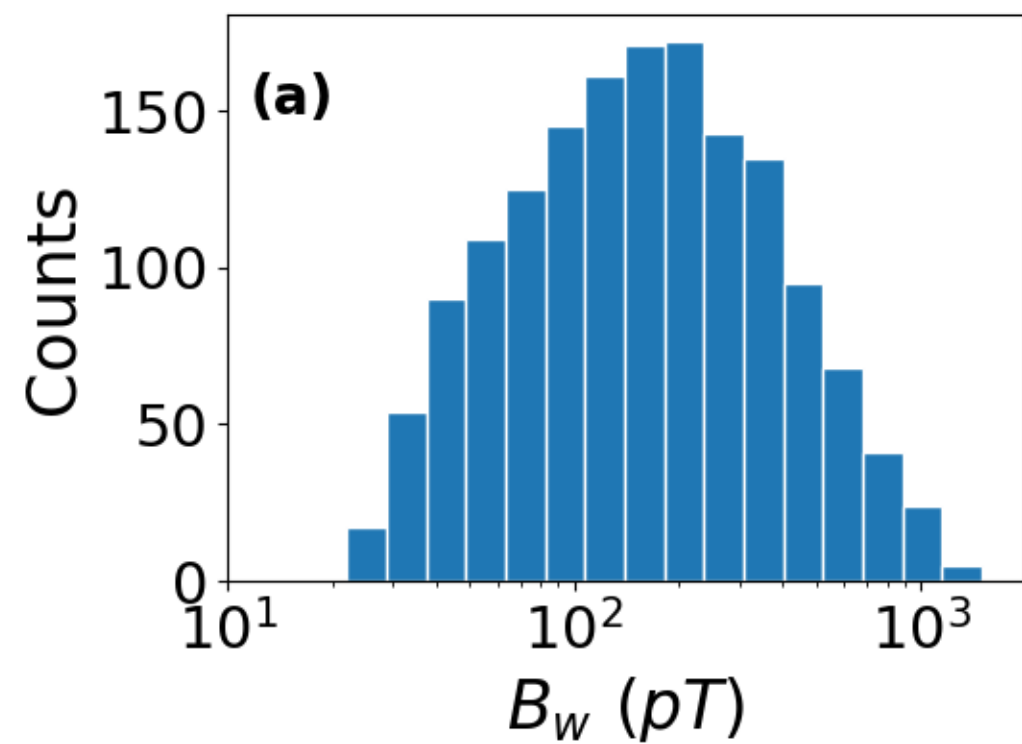


Figure 5.

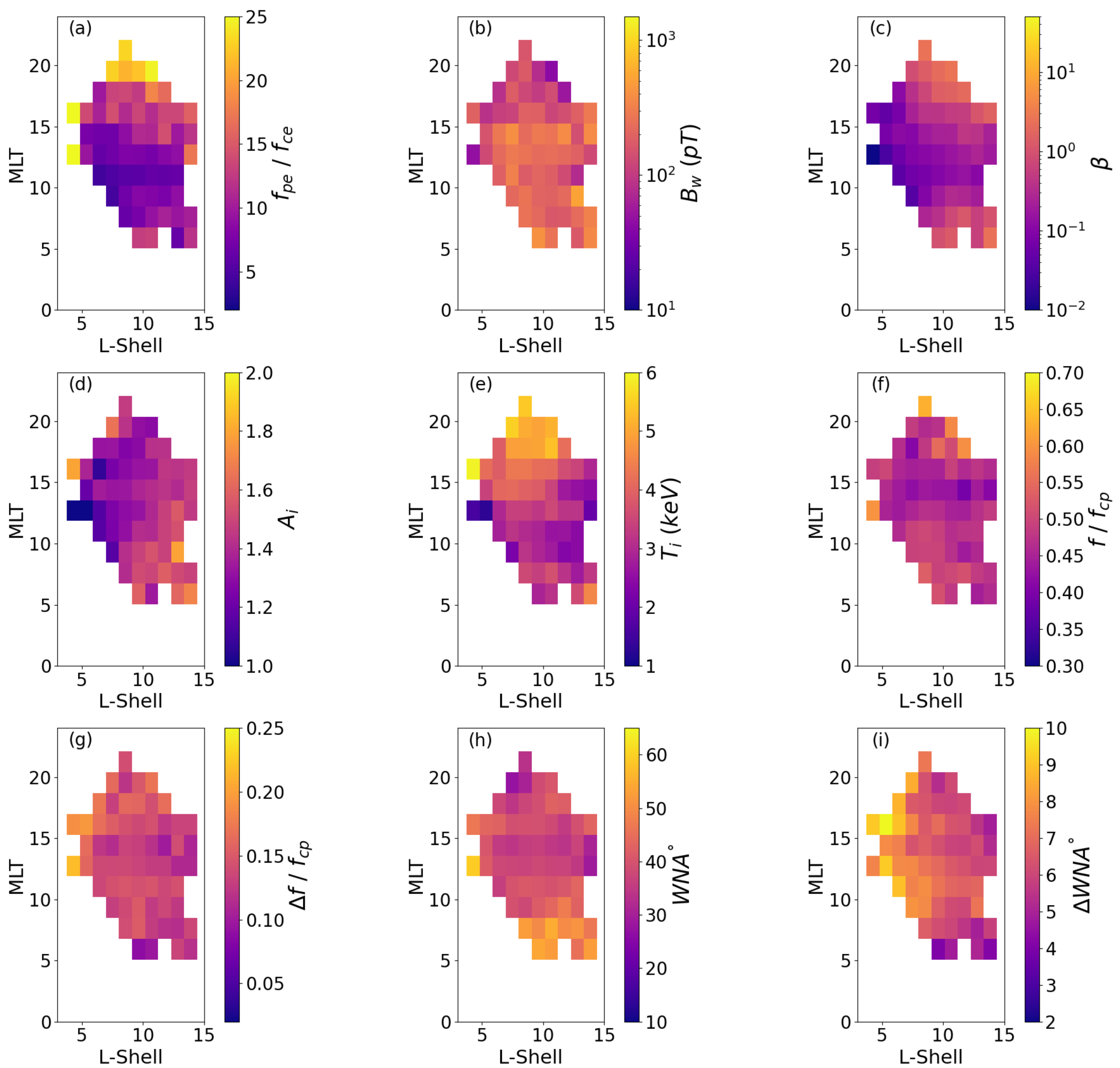


Figure 6.

