

1 **A modified scheme for wind farm parameterization in WRF considering**
2 **the impact of the floating wind turbine on waves**

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10 **Key Points:**

- 11 • A wind turbine module is implemented in the spectral wave model that
12 accounts for the energy dissipation caused by the inertial forces.
- 13 • High-resolution wave model is replaced by a machine learning model and
14 implemented in the Weather Research and Forecasting model.
- 15 • Consideration of turbine-induced changes in momentum flux is key to the
16 parameterizing floating wind farms.

17 **Abstract**

18 A new scheme is developed for floating wind farm parameterization (FWFP) in the Weather
19 Research and Forecasting (WRF) model. The impacts of the side columns of a
20 semi-submersible floating wind turbine on waves are firstly parameterized in the spectral
21 wave model (SWAN) where the key idea is to consider both inertial and drag forces on side
22 columns. A machine learning model is trained using results of idealized high-resolution SWAN
23 simulations and then implemented in the WRF to calculate the frictional velocity at the turbine
24 site. This frictional velocity is passed to the Fitch wind farm parameterization to form the FWFP.
25 The difference between our new scheme and the original Fitch scheme in a realistic case is
26 investigated using a coupled atmosphere-wave model. Results indicate that the FWFP can
27 increase total power output of wind farms by over 5% in the high wind speed stage due to
28 significant wave height attenuation caused by large-scale floating turbines. The turbulent
29 kinetic energy decreases within the wind farm, with the greatest drop of $0.4 \text{ m}^2 \text{ s}^{-2}$ at the top of
30 the turbine. The impact of the new scheme can spread to the top of the atmospheric boundary
31 layer. The proposed new scheme will help forecast wind energy and explore the potential
32 impacts of large floating wind farms.

33 **Plain Language Summary**

34 The global offshore wind power development is moving from offshore to deeper waters, where
35 floating offshore wind turbines have advantage over bottom fixed offshore wind turbines.
36 However, current wind farm parameterization schemes in mesoscale models are not
37 applicable to floating turbines. In this study, we propose a floating wind farm
38 parameterization scheme that accounts for the attenuation of the significant wave
39 height by floating turbines. By comparing with the original wind farm
40 parameterization, the results indicate that the new scheme has a significant impact on
41 the wind speed deficits as well as the turbulent kinetic energy.

42 1. Introduction

43 Wind farms could have a great impact on the environment, including wind speed,
44 turbulent kinetic energy (TKE), temperature, humidity, and other atmospheric parameters (Fitch,
45 2015; Siedersleben et al., 2018). This impact is not suitable to be investigated with the
46 computational fluid dynamics (CFD) models and large-eddy simulation (LES) model due to
47 great computational expense and feedback effects that cannot be captured by high-resolution
48 non-meteorological microscale models alone. Engineering wake models also lack the relevant
49 physical processes that are important for large scale wind farms or wind farm clusters with
50 hundreds of turbines or more (Emeis, 2010). Currently, an important tool for studying wind
51 farms is mesoscale models with a wind farm parameterization. In mesoscale models, there are
52 two different methods to parameterize the wind farm: implicit and explicit methods. Previous
53 results have shown that explicit methods represent the wind farm effects in a more physically
54 consistent way and lead to more realistic results (Fitch et al., 2013; Fitch, 2015). In addition, the
55 explicit methods have the advantage of accounting for the interaction of wind speeds with the
56 surface below (Du et al., 2017; Vanderwende & Lundquist, 2016). The explicit methods
57 parameterize the wind farm effect as a momentum sink on the mean flow and as a source of
58 TKE (Abkar and Porté-Agel, 2015; Blahak et al., 2010; Fitch et al., 2012; Pan & Archer, 2018;
59 Redfern et al., 2019; Volker et al., 2015). Most of parameterizations are conducted in the free,
60 open-source Weather Research and Forecasting (WRF) model, which already includes the
61 Fitch wind farm parameterization in its release (Fitch et al., 2012).

62 The installed capacity of offshore wind energy has been continuously increasing (Diaz et
63 al., 2020). Unlike onshore wind farms, offshore wind farms affect the waves and thus the
64 roughness length of the surrounding surface. Changes in the roughness length in turn affect the
65 wind field through momentum transfer between the atmosphere and the waves, and previous
66 studies have found that an impact of the wave field on the wind field can reach into the height of
67 the turbine (AlSam et al., 2015; Jenkins et al., 2012; Kalvig et al., 2014; Paskyabi et al., 2014; ;
68 Porchetta et al., 2021; Wu et al., 2020; Yang et al., 2014; Zou et al., 2018). There is a complex
69 interaction between wind and waves. Wind turbines influence waves in two ways: 1) through a
70 reduced wind stress as a consequence of the kinetic energy extraction by the turbines
71 (Christensen et al., 2013) and 2) through the interaction with the wind turbine pole due to
72 reflection, diffraction and drag dissipation. The global offshore wind power development is
73 moving from offshore to deeper waters, where floating offshore wind turbines have advantage
74 over bottom fixed offshore wind turbines in water depths greater than 50 m (Diaz et al., 2020;
75 Roddier et al., 2010). Floating offshore wind turbines can have a substantial impact on waves
76 due to floating platforms, which in turn leads to major changes in roughness length of ocean
77 surface, requiring modifications of the current wind farm parameterization scheme used in
78 mesoscale meteorological models.

79 The influence of wind farm structures on waves has been investigated in only a few studies.
80 Ponce de Leon et al. (2011) used the Simulation WAVes Nearshore (SWAN) model to study
81 the impact of an offshore wind farm on nearby waves. Since the monopile foundations included
82 in their study could not realistically be resolved, each monopile foundation was represented as a
83 dry point (land) in the model. They found that the simulated monopiles acted as obstacles
84 blocking the propagation of wave energy and slightly altering the wave direction. Alari &
85 Raudsepp (2012) found that the impact of the wind turbine on the significant wave height
86 (SWH) was very marginal, with changes of the SWH smaller than 1% at areas shallower than
87 10 m depth. Molen et al. (2014) conducted sensitivity experiments to study the influence of
88 turbine spacing and size of wind farm on the SWH, and found that the SWH could be reduced
89 by up to 9.58%. McCombs et al. (2014) evaluated the impact of an offshore wind farm on
90 waves in Lake Ontario using a coupled wave-hydrodynamic model. In the study, the offshore

91 wind farm was simulated by applying a transmission coefficient in the wave model and adding
 92 a quadratic friction term to the momentum equations of the hydrodynamic model in the area of
 93 the proposed wind farm. The results indicated that the wave heights in coastal areas will be
 94 minimally affected with changes of SWH predicted to be less than 3%.

95 These previous studies simulate the wind turbine in the model as a dry grid point, which
 96 has two limitations, 1) the model resolution is too high to implement for large-scale offshore
 97 wind farm scenarios, 2) it can only represent the diffraction effects, however, wave forces
 98 include drag and inertial forces (Isaacson, 1979; Morison et al., 1950). By parameterizing both
 99 the drag and inertial forces in the numerical model, the impact of the offshore wind turbine/farm
 100 on the waves can be analyzed more accurately. Previous studies also discussed the impact of
 101 bottom fixed wind turbines on waves, while the impact of floating offshore wind turbines on
 102 waves needs to be re-evaluated due to the significant structural differences between floating and
 103 bottom fixed wind turbines.

104 In this study, a floating offshore wind farms parameterization scheme in the WRF Model
 105 is developed to represent the effect of the offshore wind farm on surface waves. In Section 2, the
 106 wave energy dissipation due to the inertial forces of waves is implemented in SWAN. The
 107 model configuration and results of high-resolution idealized simulations are presented in
 108 Section 3. In Section 4, we propose a machine learning module used to fit the effect of wave
 109 inertial forcings represented in high-resolution SWAN simulations. Section 5 describes how the
 110 floating wind farm parameterization scheme is implemented in the WRF, and presents the
 111 results and the analysis of the wind speed deficit, power output, and the influence of the new
 112 scheme on the turbulent kinetic energy. The conclusion is given in Section 6.

113 2. Parameterization of the wave inertial force in SWAN

114 2.1 SWAN

115 SWAN is a third-generation phase-averaged spectral wave model (Booij et al., 1999). The
 116 model propagates offshore wave conditions, input at the model boundaries as either integrated
 117 parameters or spectra, across a user defined grid of bathymetry to the region of interest. The
 118 evolution of the wave energy density spectrum in space and time is calculated by solving the
 119 action balance equation. This equation includes source terms for energy input into the model
 120 (from wind), dissipation (from white capping and shallow-water effects) and redistribution (via
 121 triad and quadruplet interactions). Shallow water and depth-limited processes including
 122 refraction, bottom friction and depth-induced breaking are accounted, and diffraction in SWAN
 123 is represented by a phase-decoupled approach (Holthuijsen et al., 2003). Further details on the
 124 physical processes in SWAN can be found in the SWAN User Manual (The SWAN team,
 125 2023).

126 The rate of change of the action density N at a single point is governed by the action
 127 balance equation,

$$\frac{\partial N}{\partial t} + \frac{\partial}{\partial x} C_x N + \frac{\partial}{\partial y} C_y N + \frac{\partial}{\partial \sigma} C_\sigma N + \frac{\partial}{\partial \theta} C_\theta N = \frac{S_{tot}}{\sigma} \quad (1)$$

$$N(\sigma, \theta) = \frac{E(\sigma, \theta)}{\sigma} \quad (2)$$

128 where E is energy density, σ is the relative radian frequency, θ is propagation directions, C_x
 129 and C_y are the propagation velocities of action density in two-dimensional geographical space,
 130 C_σ and C_θ are the propagation velocities in spectral space, S_{tot} is the non-conservative

131 source/sink term that represents all physical processes which generate, dissipate, or redistribute
 132 wave energy.

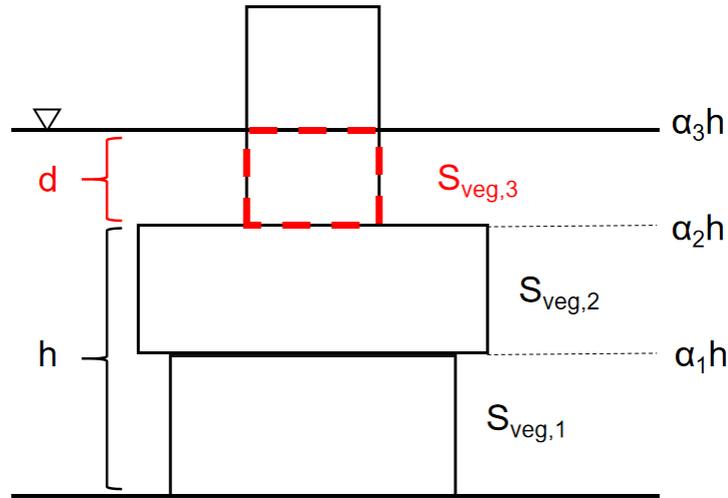
133 In the shallow water region, seven basic processes contribute to S_{tot} :

$$S_{tot} = S_{in} + S_{nl3} + S_{nl4} + S_{ds,w} + S_{ds,b} + S_{ds,br} + S_{ds,veg} \quad (3)$$

134 where S_{in} denotes wave growth by the wind, S_{nl3} and S_{nl4} indicate nonlinear transfer of
 135 wave energy through three-wave and four-wave interactions, respectively. The wave decay due
 136 to whitecapping, bottom friction, depth-induced wave breaking and vegetation are denoted by
 137 $S_{ds,w}$, $S_{ds,b}$, $S_{ds,br}$ and $S_{ds,veg}$, respectively.

138 2.2 Wave damping due to the inertial forces

139 SWAN has a function to include wave damping over a vegetation (VEG) field at variable
 140 depths. A popular method of expressing the wave dissipation due to vegetation is the cylinder
 141 approach suggested by Dalrymple et al. (1984). In this approach, energy losses are calculated as
 142 actual work carried out by the vegetation due to plant induced forces acting on the fluid,
 143 expressed in terms of a Morison type equation. Two modifications convert the VEG module
 144 into the semi-submersible floating wind turbine module. The energy dissipation in each vertical
 145 layer is calculated separately, and the total energy dissipation is equal to the sum of the
 146 dissipation across all layers up to the still water level (Figure 1). The first modification then is
 147 that the module only needs to calculate the results of $S_{veg,3}$ (the red dashed box in Figure 1) and
 148 set d (column draft depth) to a constant ($d=20$ m is used in this paper).



149
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Figure 1. Layer schematization for vegetation

151 Another important modification of the VEG module concerns the energy dissipation due
 152 to wave forces. In the VEG module, the wave force is derived from the drag force in a Morison
 153 type equation with the inertial forces neglected. Since the vegetation is assumed to be a cylinder
 154 with a small diameter, the drag force is considered to be dominant. However, for the floating
 155 offshore wind turbine, the diameter of the cylinder cannot be neglected compared to the
 156 wavelength. The wave forces become more complex and require the consideration of inertial
 157 forces. The equation for the energy dissipation due to inertial forces can be derived from the
 158 work of Morison et al. (1950).

$$D = \int_{-(h+d)}^{-h} F_{iner} \cdot u dz = \int_{-(h+d)}^{-h} C_M \rho \frac{\pi b^2}{4} \frac{\partial u}{\partial t} \cdot u dz \quad (4)$$

159 where C_M is the inertial force coefficient, b is the cylinder diameter. Based on Kobayashi et al.
160 (1993), the formula for $\partial u / \partial t$ is derived as below

$$u = \frac{gkH}{2\omega} \frac{\cosh[k(h+d+z)]}{\cosh[k(h+d)]} \quad (5)$$

$$\frac{\partial u}{\partial t} = \frac{gkH}{2} \frac{\cosh[k(h+d+z)]}{\cosh[k(h+d)]} [\delta c_2 + (\delta - \varepsilon)c_3] \quad (6)$$

161 where ω is the wave angular frequency, H is the wave height, k is the wave number, $h+d$
162 is the water depth, d is the draft depth (Figure 1).

163 The equations for the other parameters are as follows,

$$\varepsilon = \frac{C_D b H}{9\pi} \cdot c_5 \quad (7)$$

$$\delta = \varepsilon \cdot c_4 \quad (8)$$

$$c_2 = \frac{\sinh k h \sinh[k(h+d)] - k h \tanh kd}{\cosh kd} \quad (9)$$

$$c_3 = k(h+d+z) \tanh[k(h+d+z)] - kd \tanh kd \quad (10)$$

$$c_4 = \frac{2kd + \sinh 2kd}{2k(h+d) + \sinh[2k(h+d)]} \quad (11)$$

$$c_5 = \frac{\sinh 3kd + 9 \sinh kd}{(2kd + \sinh 2kd) \sinh[k(h+d)]} \quad (12)$$

164 Substitution of Eqs. (5), (6) and (10) into Eq. (4) yields

$$D = \frac{C_M \rho \pi b^2 k (gH)^2}{16\omega \cosh^2[k(h+d)]} [\delta c_2 \frac{\sinh 2kd + 2kd}{4} + (\delta - \varepsilon) \frac{2kd \cosh 2kd - \sinh 2kd - kd \tanh kd (\sinh 2kd + 2kd)}{8}] \quad (13)$$

165 Substitution of Eqs. (7) and (8) into Eq. (13) yields

$$D = \frac{C_M C_D \rho b^3 k g^2 H^3}{144\omega \cosh^2[k(h+d)]} [c_4 c_5 c_2 \frac{\sinh 2kd + 2kd}{4} + c_5 (c_4 - 1) \frac{2kd \cosh 2kd - \sinh 2kd - kd \tanh kd (\sinh 2kd + 2kd)}{8}] \quad (14)$$

166 Waves can be described by a joint distribution of wave height, period (or frequency) and
167 direction. A Rayleigh distribution often gives a satisfactory characterization of the random
168 variation in wave height (Mendez & Losada, 2004). The Rayleigh probability density function
169 is related to wave height,

$$H^3 = \int_0^{\infty} H^3 p(H) dH \quad (15)$$

$$\int_0^{\infty} H^3 p(H) dH = \frac{3\sqrt{\pi}}{4} H_{rms}^3 \quad (16)$$

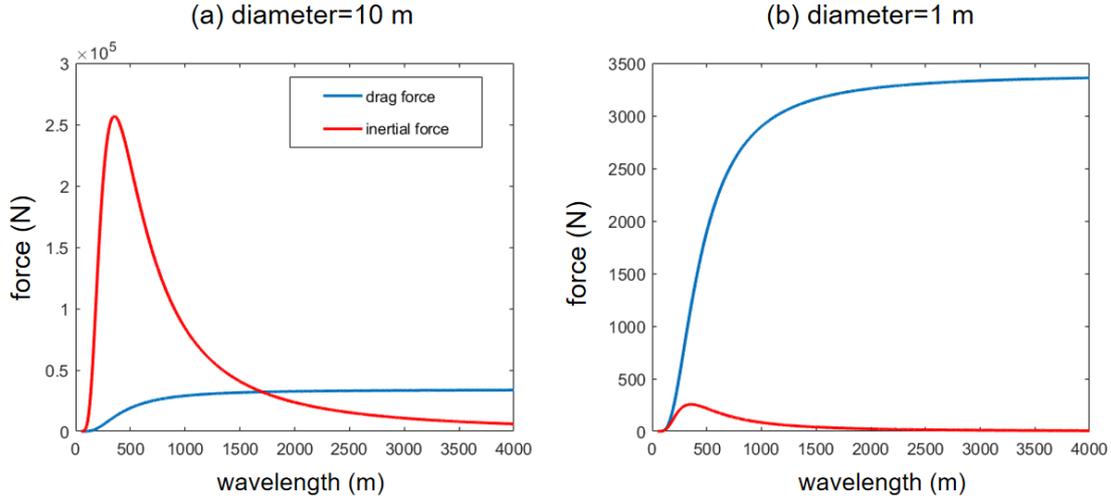
170 where $p(H)$ is the Rayleigh probability density function, H_{rms} is the root-mean-square wave
171 height. Substitution of Eqs. (15) and (16) into Eq. (14) and dividing by the bulk density of the
172 fluid yields

$$D = \frac{C_M C_D b^3 g k N}{144\omega \cosh^2[k(h+d)]} \frac{3\sqrt{\pi}}{4} H_{rms}^3 [c_4 c_5 c_2 \frac{\sinh 2kd + 2kd}{4} + c_5 (c_4 - 1) \frac{2kd \cosh 2kd - \sinh 2kd - kd \tanh kd (\sinh 2kd + 2kd)}{8}] \quad (17)$$

173 The root-mean-square wave height and the total wave energy have such a relationship,
 174 $H_{rms}^2 = 8E_{tot}$, and substituting it into Eq. (17) yields,

$$D = \frac{1}{8} \sqrt{\frac{\pi}{72}} \frac{C_M C_D b^3 g k}{\omega \cosh^2[k(h+d)]} [2c_4 c_5 c_2 (\sinh 2kd + 2kd) + c_3 (c_4 - 1) [2kd \cosh 2kd - \sinh 2kd - kd \tanh kd (\sinh 2kd + 2kd)]] E_{tot}^{3/2} \quad (18)$$

175 Eq. (18) is the equation calculating the energy dissipation due to the inertial force. In the
 176 study, the magnitudes of the inertial force and the drag force are calculated and compared for
 177 the cylinders with diameters of 10 m and 1 m.



178 **Figure 2.** Inertial forces (red solid line) and drag forces (blue solid line) for cylindrical
 179 diameters of (a) 10 m and (b) 1 m (incident wave height of 3 m, drag coefficient of 1.2, draft depth
 180 of 20 m, water depth of 80 m)
 181

182 The case is set with the incident SWH of 3 m, the drag coefficient of 1.2, the draft depth of
 183 20 m, and the water depth being 80 m. When the cylinder diameter is 10 m (Figure 2a), the
 184 average wavelength of the incident wave is within 1700 m, which makes the inertial force larger
 185 than the drag force. However, when the cylinder diameter is 1 m (Figure 2b), the inertial force is
 186 always smaller than the drag force. As the wavelength increases (the scale becomes smaller),
 187 the drag force becomes larger relative to the inertial force, which is consistent with the
 188 assumption of the VEG module that the inertial force could be neglected, but the inertial force
 189 can not be ignored for the side column of the floating offshore wind turbine. Thus the VEG
 190 module in SWAN is modified to include the inertial force to be applicable for the floating wind
 191 turbine.

192 3. Idealized high-resolution simulations

193 As shown in Section 2, the floating offshore wind turbine module is developed for SWAN,
 194 and its impact on waves is examined using high-resolution numerical experiments in this
 195 section.

196 The rectangular domain of the idealized high-resolution experiments is shown in Figure 3,
 197 with 100×200 cells, a horizontal resolution corresponding to the column diameter of 10 m, and
 198 a water depth of 50 m. The position of the column is at the center of the computational domain.
 199 The incident SWH is 3 m, the mean wave period is 12 s, propagating from east to west, and the
 200 shape of the spectra is from the JONSWAP spectrum. Because of the small computational
 201 domain, the model uses stationary computation which converges after several time steps.

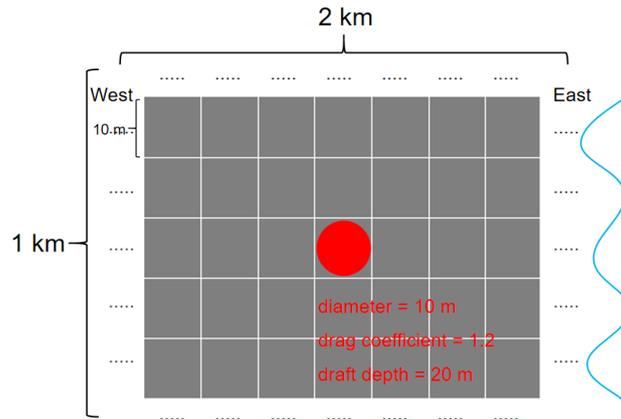


Figure 3. Experimental design of high-resolution idealized simulations (SWH=3 m, mean wave period=12 s, and depth=50 m)

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205 Two experiments are conducted, one to study the influence of the column on the waves
206 caused only by the drag force (ExpDragS), and the other to examine the influence caused by
207 both the drag force and the inertial force (ExpInerS). It can be noted that when the energy
208 dissipation is caused by the drag force only, the SWH attenuation is only ~ 0.2 m (Figure 4a),
209 and the "wake" phenomenon occurs in the wave field. The angle of the mean wave direction is
210 shifted by about 1° around the column and the horizontal distribution is symmetrical along the
211 axis $y=0$ (Figure 4d). The mean wave length is increased by about 10 m (Figure 4g). When the
212 inertial forces are taken into account, the energy dissipation is larger, which makes the SWH
213 attenuation more significant, which is about 1.4 m (Figure 4b), indicating an attenuation of 50%
214 SWH. The mean wave direction deviation around the column is also relatively large, reaching
215 about 5° (Figure 4e), and the mean wave length is about 24 m longer (Figure 4i) than that of
216 ExpDragS.

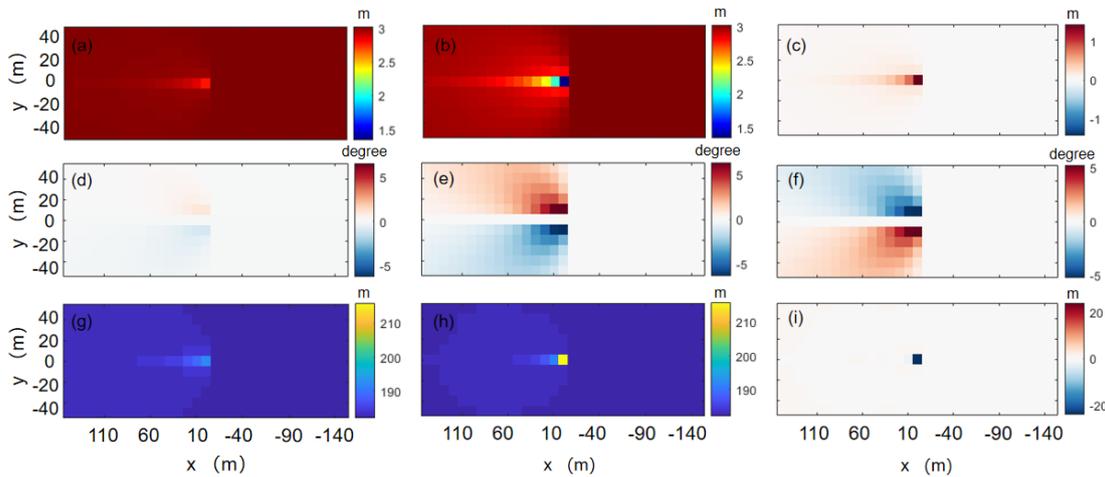


Figure 4. Significant wave height of (a) ExpDragS and (b) ExpInerS, (c) difference in significant wave height, (d) mean wave direction deviation of ExpDragS and (e) ExpInerS, (f) difference in mean wave direction deviation, (g) mean wave length of ExpDragS, and (h) ExpInerS, (i) difference in mean wave length

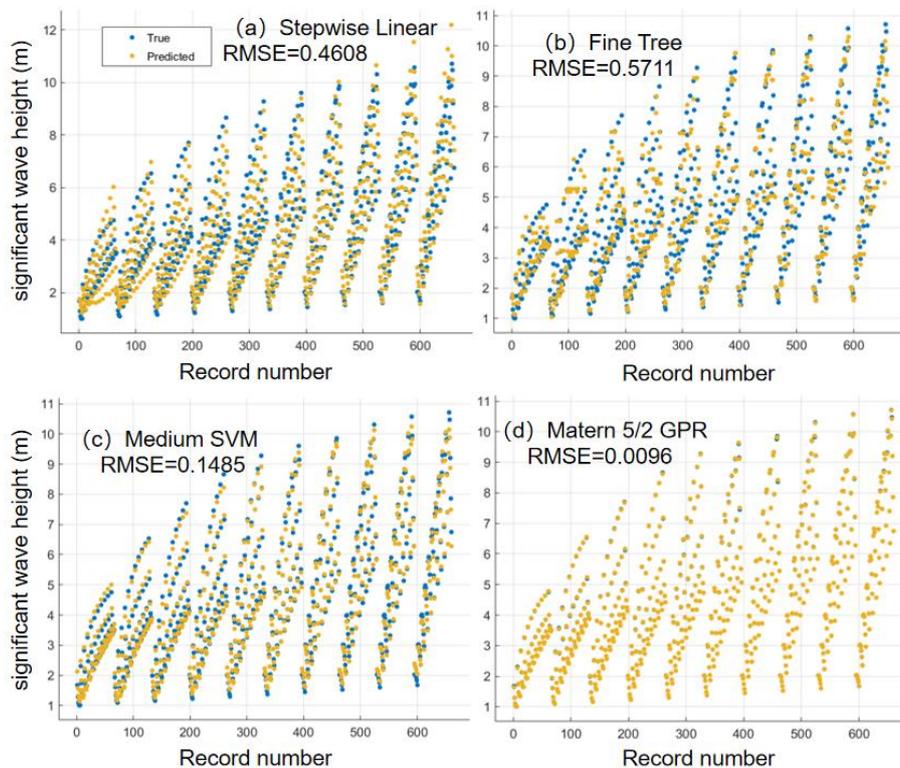
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222 4. Machine learning parameterization

223 The results of the idealized high-resolution SWAN simulations in Section 3 show the
224 impact of the floating offshore wind turbine's side columns on the waves, including the SWH
225 attenuation, symmetrical changes of mean wave direction, and an increase in the mean wave
226 length. However, it is computationally expensive to run a ~ 10 m resolution SWAN model.

227 The use of machine learning (ML) for better parametrizing unresolved processes in
 228 mesoscale and climate models has gained much attention recently (O’Gorman & Dwyer, 2018;
 229 Gettelman et al., 2020; Seifert & Rasp, 2020). With the rise of scientific machine learning and
 230 its broad application in the geosciences, the design of parametrizations using ML algorithms has
 231 become a trend in model development. To build an appropriate model, a large amount of data is
 232 needed for training. Nevertheless, the observational data on the impact of the floating offshore
 233 wind turbine on waves are scarce. As a result, the outputs of the high-resolution SWAN
 234 simulations in Section 3 are employed to train the ML model.

235 From the equations in Section 2, we can note that when the inertial force coefficient, drag
 236 force coefficient, and cylindrical diameter are determined, the energy dissipation caused by the
 237 wave force is only related to the water depth, incident SWH, and mean wave period (or peak
 238 period). We design a series of ideal experiments with different water depths, incident SWH, and
 239 mean wave periods. The SWH is taken from 2 m to 12 m with 1 m interval. The peak wave
 240 period is from 7 s to 12 s with an interval of 1 s, and the water depth is selected from 53 m to 98
 241 m with an interval of 5 m. This has a total number of 660 ($11 \times 6 \times 10$) experimental groups.
 242 We then use these model data to train several machine learning (regression) models with the
 243 input of incident SWH, water depth, and peak wave period, and the output of SWH after energy
 244 dissipation. These models can be classified into four main categories: linear regression models,
 245 tree models, support vector machines (SVM), and Gaussian process regression (GPR). As
 246 shown in Figure 5, the GPR model with the Matern 5/2 kernel (covariance) function is the most
 247 reasonable, with a minimum root mean square error (RMSE) of 0.0096 m (Figure 5d). The
 248 model can be coupled with CFD, LES models and mesoscale meteorological models to predict
 249 the effect of the floating offshore wind turbine side columns on waves without the need for
 250 high-resolution SWAN simulations.



251 **Figure 5.** Response results of four typical regression models: (a) Stepwise linear regression (b)
 252 Fine tree (c) Medium SVM (d) Matern 5/2 Gaussian process regression
 253

254 5. Parameterization in a mesoscale model

255 5.1 Implementation of parameterization in WRF

256 The Fitch wind-farm parametrization (Fitch et al., 2012), which has been implemented in
 257 the WRF model, is the most widely used method to simulate large wind farms. The important
 258 point in the derivation of the Fitch equation is that the rate of loss of kinetic energy in the grid
 259 cell is equal to the kinetic energy loss due to the wind turbine in the grid,

$$-\frac{1}{2} N_{ij} \Delta x \Delta y \rho C_T |V|_{ijk}^3 A_{ijk} = \Delta x \Delta y (z_{k+1} - z_k) \rho |V|_{ijk} \frac{\partial |V|_{ijk}}{\partial t} \quad (19)$$

260 where $|V|_{ijk}$ is the horizontal wind speed, N_{ij} is the number of turbines per square meter, ρ
 261 is the air density, C_T is the thrust coefficient of a wind turbine, $\Delta x, \Delta y$ are the horizontal grid
 262 size in the zonal and meridional directions respectively, z_k is the height at model level k , A_{ijk}
 263 is the cross-sectional rotor area of one wind turbine bounded by model levels $k, k+1$ in grid
 264 cell i, j .

265 For a semi-submersible floating wind turbine, the SWH around the turbine is considerably
 266 affected. As a result, the roughness of ocean surface nearby is also changed. The change in the
 267 kinetic energy due to changes in the momentum flux in the surface layer should be taken into
 268 account for the loss of kinetic energy in the grid cell. Therefore, in the simulation with
 269 semi-submersible floating wind turbines applied, Eq. (19) can be modified

$$-\frac{1}{2} N_{ij} \Delta x \Delta y [\rho C_T |V|_{ijk}^3 A_{ijk} - \Delta \tau \cdot S |V|_{ijk} (z_{k+1} - z_k)] = \Delta x \Delta y (z_{k+1} - z_k) \rho |V|_{ijk} \frac{\partial |V|_{ijk}}{\partial t} \quad (20)$$

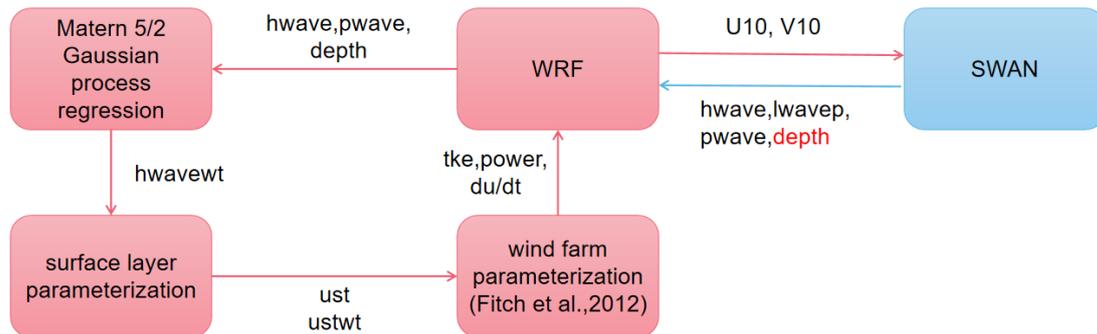
270 where S is the area occupied by the floating platform. $\Delta \tau = \rho(u_{*,wt}^2 - u_*^2)$ is the change in the
 271 momentum flux due to the turbine. $u_{*,wt}$ is the frictional velocity at location of the turbine and
 272 u_* is the frictional velocity unaffected by the turbine. A new equation for the momentum
 273 tendency term is given as

$$\frac{\partial |V|_{ijk}}{\partial t} = - \frac{N_{ij} [\frac{1}{2} C_T |V|_{ijk}^2 A_{ijk} + (u_{*,wt}^2 - u_*^2) S (z_{k+1} - z_k)]}{(z_{k+1} - z_k)} \quad (21)$$

274 It should be noted that Eq. (21) applies only to the heights between the bottom of the rotor
 275 area and 100 m (top of the surface layer). The momentum flux term in Eq. (21) can be omitted
 276 when z_{k+1} is greater than 100 meters. In addition, the new parameterization calculates the
 277 momentum tendency below the bottom of the rotor area, i.e., only the momentum flux term is
 278 retained in Eq. (21).

279 The variables exchanged between WRF and SWAN is shown in Figure 6. WRF provides
 280 10-m surface wind (U10, V10) to SWAN, whereas SWAN returns SWH (hwave), peak wave
 281 length (lwavep), and peak wave period (pwave) to WRF. This variable exchange is
 282 implemented in the WRF model. The trained GPR model needs water depth as the input, thus
 283 we implement SWAN to provide water depth to WRF. Specifically, we incorporate the GPR
 284 model into the surface layer parameterization module of WRF. As a result, the SWH affected
 285 by the floating offshore wind turbine (hwavewt) can be calculated directly in the surface layer
 286 parameterization module to obtain the roughness length, frictional velocity, and other variables.
 287 The frictional velocity at the location of the wind turbine (ustwt) and the frictional velocity

288 unaffected by the turbine (ust) are input to the existing wind farm parameterization module in
 289 WRF to make the parameterization module suitable for floating offshore wind farms.



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Figure 6. Flow chart of floating offshore wind farms parameterization implemented in the COAWST model

293 5.2 Model configuration

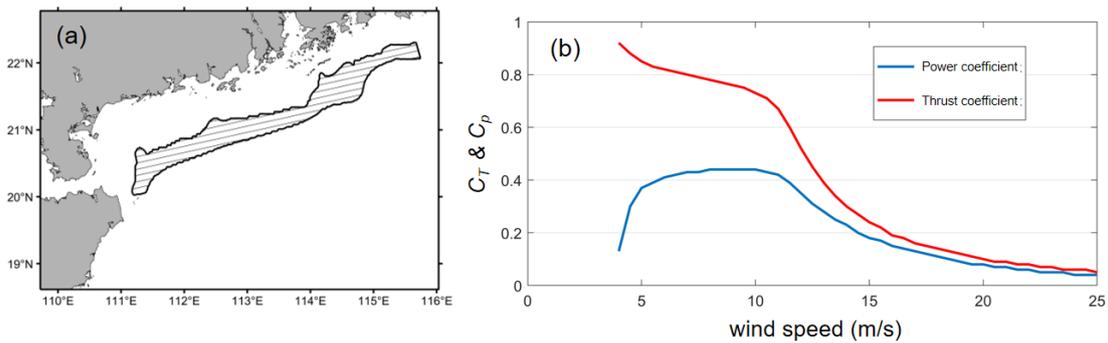
294 The new parameterization is tested in the Coupled
 295 Ocean-Atmosphere-Wave-Sediment Transport (COAWST) modeling system (Warner
 296 et al., 2008; Warner et al, 2010). This coupling system comprises four components,
 297 including the atmospheric model (WRF) and the spectral wave model (SWAN), which
 298 are connected by The Model Coupling Toolkit (MCT). The other components of
 299 COAWST are not activated in this study.

300 Initial and lateral boundary conditions for the WRF model are obtained from the
 301 global forecasting system (GFS) NCEP FNL analysis data with horizontal resolution
 302 of 1° . The WRF model has a horizontal grid resolution of 8 km, with the center
 303 located at 21.98°N , 115.94°E . There are 275×194 grid cells in the horizontal domain
 304 (Figure 7a), 47 eta levels in the vertical direction, where 23 levels are below 1000 m
 305 and 15 levels intersect the rotor region. The vertical grid spacing at levels spanned by
 306 the wind turbine rotor is about 14 m. The major physical parameterization schemes
 307 are summarized in Table 1. The wind farm is located in the northern South China Sea
 308 at the water depths between 50 and 63 m (Figure 7b). The turbine spacing is about 1
 309 km. The thrust and power coefficients of the LEANWIND 8 MW reference turbine
 310 (LW) are presented in Figure 7c. Other main technical parameters of the LW wind
 311 turbine are shown in Table. 2 (Desmond et al., 2016).

312 We use the same model domain and horizontal grid for SWAN as that in the
 313 WRF model. The corresponding parameterization schemes are shown in Table 1. The
 314 spectrum is discretized using 24 logarithmically-spaced frequency bins from 0.04 to
 315 1.00 Hz and 36 directional bins with 10° spacing. The boundary conditions are taken
 316 from the WaveWatch III (WW3) model (WW3DG, 2019). The nonstationary mode of
 317 SWAN is used and the effects of quadruplet nonlinear wave-wave interactions are
 318 taken into account. In this fully coupled model simulation, SWAN runs with a time
 319 step of 60 s, and the WRF model runs with a time step of 36 s. The time interval for
 320 data interchange among the models is set to 600 s. The total simulation time is 4 days
 321 (i.e., from 00 UTC on 1 January to 00 UTC on 5 January 2019), with SWAN starting
 322 from the initial steady state. A reference simulation (control run, referred as
 323 WRF-CTL) is performed without the wind farm. Another simulation (WRF-Fitch) is
 324 conducted with the Fitch wind farm parameterization. A third simulation
 325 (WRF-FWFP) is performed with the new proposed floating wind farm parameterization
 326 (FWFP).

327 Table.1 Major physical parameterization schemes used in COAWST.

	Physics options	Parameterization scheme
WRF	Microphysics	Single-Moment 6-class (Hong & Lim, 2006; Hong et al., 2006)
	Longwave Radiation	Rapid Radiative Transfer Model (Mlawer, 1997)
	Shortwave Radiation	Dudhia (Dudhia, 1989)
	Surface Layer	MYNN (Nakanishi & Niino, 2009)
	Land Surface	thermal diffusion (Duhia, 1996)
	Planetary Boundary Layer	Mellor-Yamada-Nakanishi-Niino 2.5-level (Nakanishi & Niino, 2009)
	Cumulus Parameterization	Grell-Freitas ensemble (Grell & Freitas, 2014)
	Roughness Parameterization	CORE-Talyor-Yelland (Taylor & Yelland, 2001)
SWAN	Depth-induced wave breaking	Constant (1.0, 0.73) (Battjes & Janssen, 1978)
	Bottom friction	Madsen (0.05) (Madsen et al., 1988)
	Wind input	Komen (Komen et al., 1984)
	Whitecapping	Komen (Komen et al., 1984)



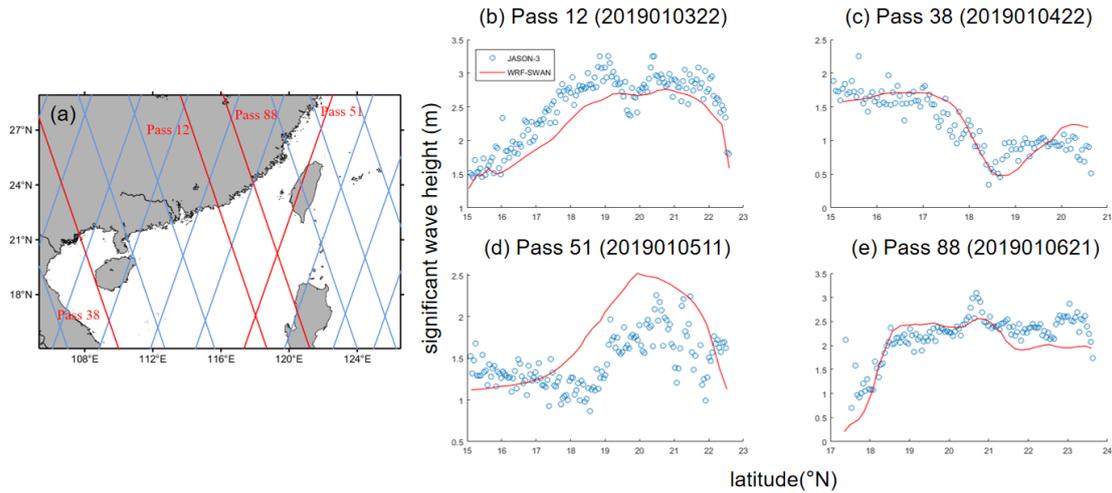
328 **Figure 7.** (a) location of wind farm (shaded area), (b) the thrust and power coefficients curves of
 329 the LW 8 MW wind turbine
 330

331 Table.2 Main technical parameters of the LW wind turbine.

Parameters	Value
Rated power	8 MW
Rotor diameter	164 m
Turbine hub height	110 m
Cut in wind speed	4 m/s
Cut out wind speed	25 m/s

332 5.3 Model validation

333 To validate SWAN results, the simulated SWH is compared with observations of
 334 the satellite data Jason-3 (Lillibridge, 2019) (Figure 8). The model is also run for an
 335 additional 2 days for further validation. It is evident that the model generally performs
 336 well on the wave simulation for the satellite tracks (Pass 38 and Pass 88). The SWH
 337 in the model is a bit underestimated on the track Pass 12 and overestimated on the
 338 track Pass 51. Generally, the model results have a reasonable performance.



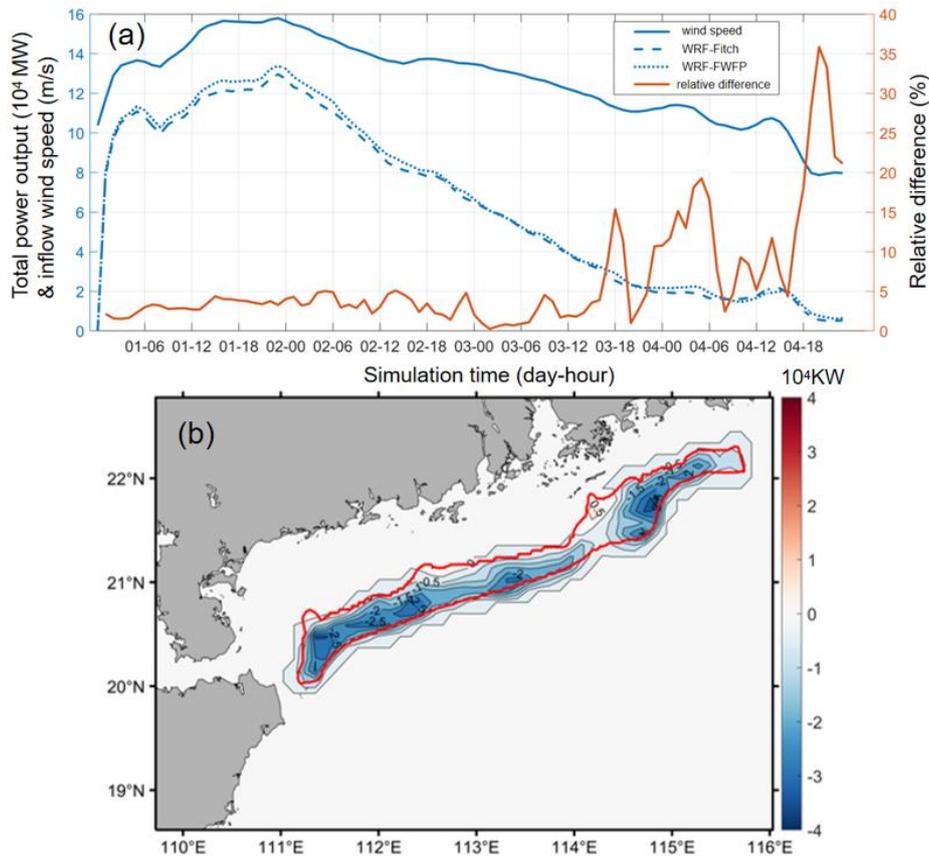
339 **Figure 8.** (a) Ground track of the *Jason-3* satellite from 00 UTC on 1 January to 00 UTC on 7
 340 January in the study region. (b) Comparison of SWH between model results and *Jason-3* altimeter
 341 data.
 342

343 5.4 Simulation results

344 In this section, the differences in power output, wind speed deficits, and TKE
 345 between the FWFP and Fitch schemes are analyzed in a realistic case using COAWST.

346 5.4.1 Power output and wind speed deficits

347 As the inflow wind speed decreases, the total power output of the experiments is
 348 reduced (Figure 9). The total power output of the FWFP scheme can be increased by
 349 up to 5.68 GW compared to the Fitch scheme. The relative difference is close to 5% in
 350 the high wind speed stage and increases to a maximum of 35% as the wind speed
 351 decreases, which is also related to the wind direction. It can also be seen that the
 352 power output of the WRF-FWFP is consistently larger than that of the WRF-Fitch,
 353 and the horizontal distribution of the difference is presented in the 84 h-averaged
 354 results (Figure 9b). FWFP does not directly modify the power output equation in the
 355 Fitch scheme. It only modifies momentum tendency terms. However, it should be noted
 356 that the change of momentum tendency terms also has a considerable effect on the
 357 power output.

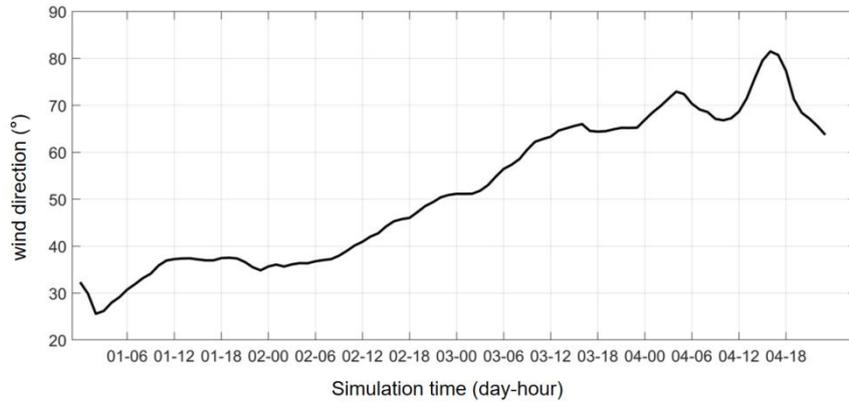


358
 359 **Figure 9.** (a) Time series of total power output, inflow wind speed and relative error of total
 360 power output. (b) Power output difference is averaged over a period time from 12 UTC on 1
 361 January to 00 UTC on 5 January, and the red solid line indicates the outer boundary of the wind
 362 farm.

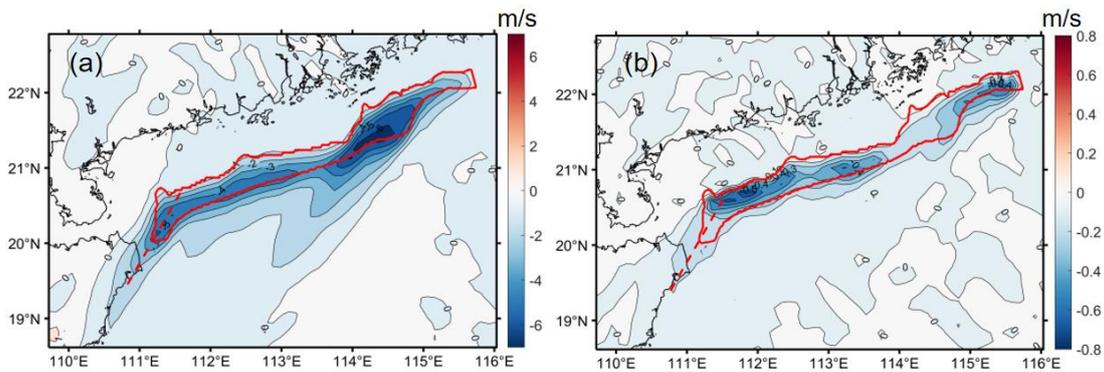
363 A small change in wind direction from 12 UTC on 1 January to 18 UTC on 1
 364 January, and this period is after the spin-up of 12 h, so the following analysis is based
 365 on this period (Figure 10). The FWFP scheme reduces the momentum with a
 366 maximum value of 6.5 m/s, which is a reduction 43% at the hub height level (Figure
 367 11a). Behind the wind farm, the wind speed deficit extends a long wake. A 2 m/s
 368 (13%) deficit reaches 60 km from the downstream edge of the wind farm (20.03°N,
 369 111.19°E). Previous studies found that wakes behind offshore wind turbines and farms
 370 are expected to be much longer than behind onshore wind turbines and farms due to
 371 the smaller aerodynamic roughness length and turbulence intensity (~50 km) (Emeis
 372 et al., 2016; Lundquist et al., 2019). We find that the wind speed deficit at hub height
 373 in the WRF-Fitch case is larger than that of the WRF-FWFP (Figure 11b), which
 374 helps to explain why the power output is greater in our FWFP scheme. Eq. (21)
 375 indicates that the FWFP takes into account the fact that the frictional velocities at the
 376 turbine locations are lower at this moment. The FWFP also has a slight impact on the
 377 wind-farm wakes.

378 Vertical profiles of wind speed deficits in WRF-FWFP case also show similar
 379 characteristics to WRF-Fitch case. The wind farm induces a maximum wind speed
 380 deficit of up to 5 m/s at the hub height, and the wind speed deficit spreads throughout
 381 the atmospheric boundary layer (ABL), including downstream of the wind farm
 382 (Figure 12a). A wind speed deficit of 1 m/s can extend up to the top of the ABL.
 383 Figure 12b shows the clear differences that occur within the wind farm, with the Fitch
 384 scheme overestimating the wind speed deficit within the ABL compared to the FWFP

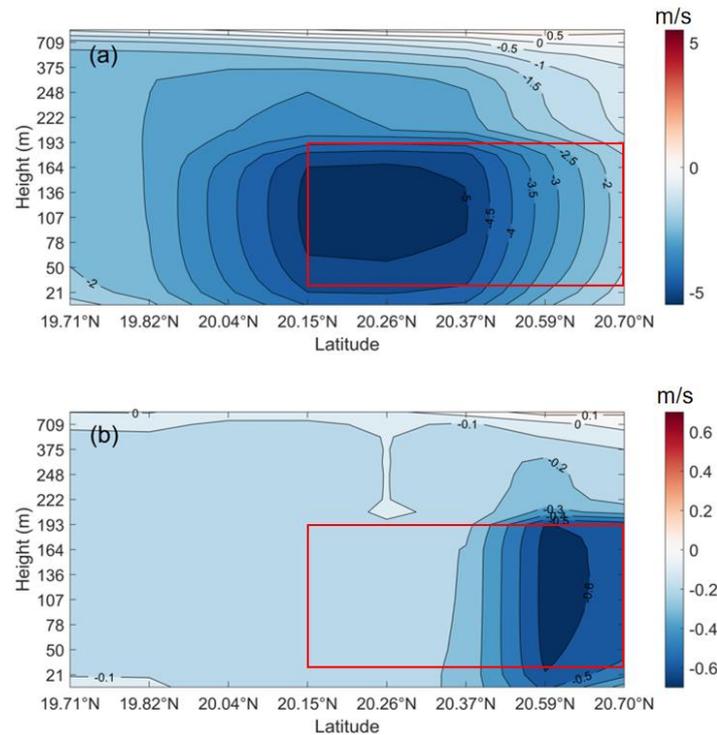
385 scheme, which is most pronounced in the rotor area with a maximum value of 0.6 m/s.
 386 The top of the turbine to the top of the ABL and the wind-farm wakes also have an
 387 effect with values of 0.1 to 0.2 m/s. The difference between the two schemes
 388 decreases rapidly at heights above the top of the turbine (sparsity in the contours).



389 **Figure 10.** Time series of wind direction at hub height within the wind farm (northerly wind
 390 direction is 0° and easterly wind direction is 90°)
 391



392 **Figure 11.** Horizontal wind speed differences at the hub height level between (a) WRF-FWFP and
 393 WRF-CTL cases and (b) WRF-Fitch and WRF-FWFP cases, averaged from 12 UTC on 1 January
 394 to 18 UTC on 1 January. The red solid line indicates the outer boundary of the wind farm, and the
 395 dashed red lines indicate a cross section analyzed further.
 396

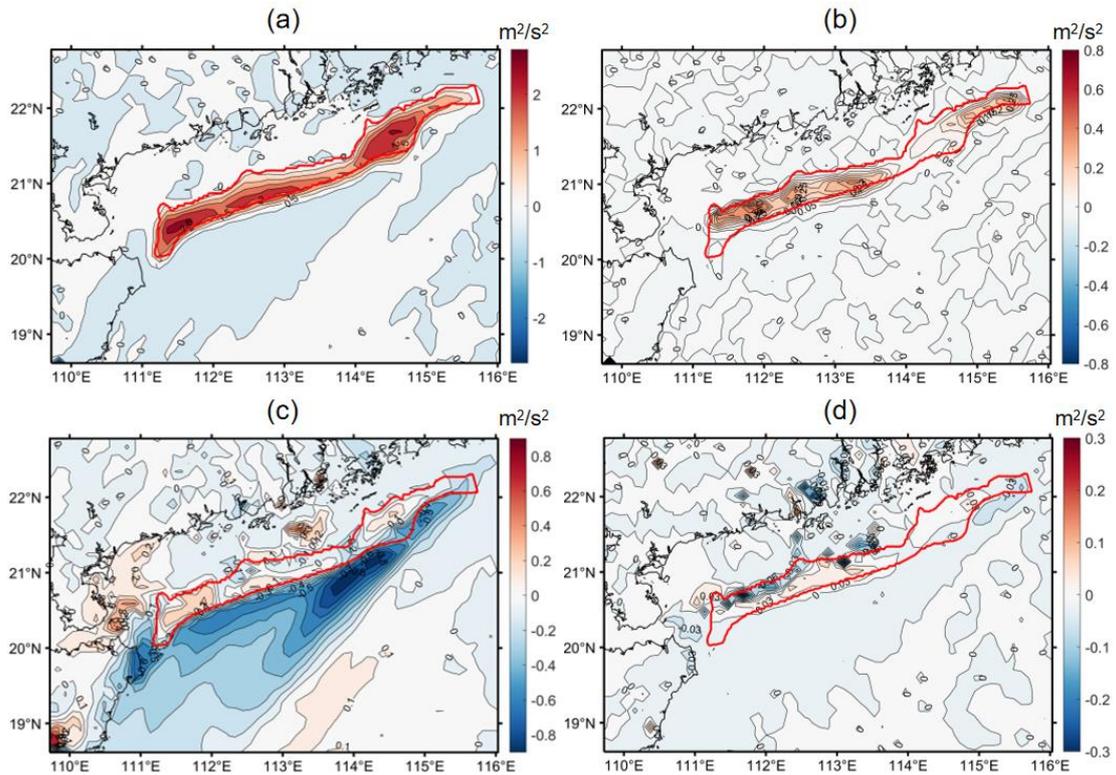


397
 398 **Figure 12.** Vertical transect of the wind speed differences between (a) WRF-FWFP and WRF-CTL
 399 cases and (b) WRF-Fitch and WRF-FWFP cases, averaged from 12 UTC to 18 UTC on 1 January
 400 along the dashed red lines in Figure 11. The red solid lines indicate the rotor area.

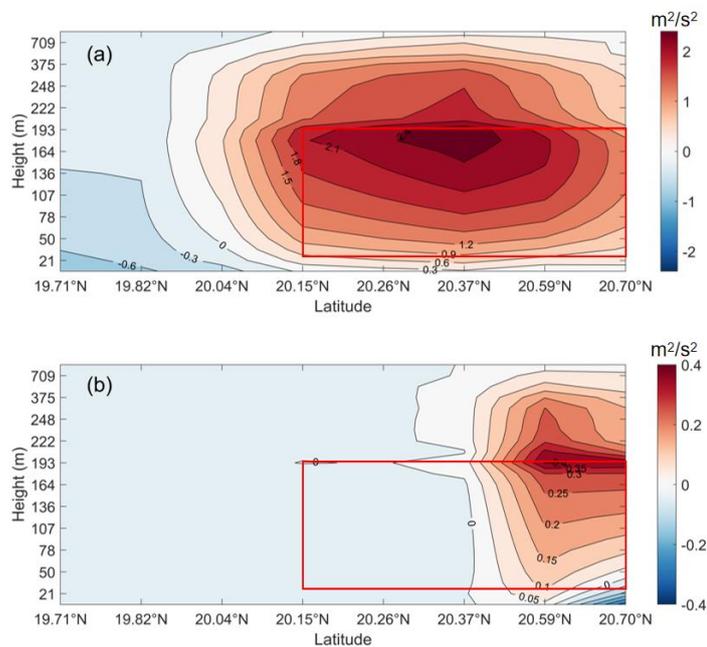
401 5.4.2 TKE

402 The generation of TKE within the wind farm is largely restricted to the farm area,
 403 and decays rapidly downstream despite the advection of TKE. A maximum increase
 404 of TKE of $2.4 \text{ m}^2\text{s}^{-2}$ at the top of the turbine is seen within the wind farm (Figure 13a).
 405 The WRF-FWFP case produces a smaller TKE within the wind farm compared to the
 406 WRF-Fitch case, with a maximum reduction of $0.8 \text{ m}^2\text{s}^{-2}$ (Figure 13b). The
 407 distribution of horizontal TKE differences is highly similar to that of horizontal wind
 408 speed differences (Figure 11b), indicating that the wind shear may dominate the TKE
 409 distribution. The reduction in the TKE of $0.3 \text{ m}^2\text{s}^{-2}$ continues to extend more than 80
 410 km downstream near the surface (Figure 13c). However, there is little difference in
 411 between the WRF-Fitch and the WRF-FWFP in the downstream near the surface
 412 (Figure 13d), with most of differences occurring only within the wind farm. The
 413 reduction in TKE near the surface in the downstream in WFP-Fitch (Figure 13c) is
 414 due to a wind speed deficit and a corresponding reduction in wind shear in the lower
 415 levels of the wake, resulting in a decrease in shear production in TKE and the
 416 reduction in the TKE is no higher than at the top of the turbine (Fitch et al., 2012).

417 As the wind speed deficits, the increase in TKE spreads to the top of the ABL
 418 which is above the wind farm, with a rise of $0.3 \text{ m}^2\text{s}^{-2}$ reaching a height of nearly 709
 419 m (Figure 14a). At the top of the turbine, the maximum increase in TKE is $2.4 \text{ m}^2\text{s}^{-2}$.
 420 Above the top of the turbine, the increase in TKE decreases with height, and below
 421 the top of the turbine it increases with height. The difference in TKE between the
 422 WRF-Fitch and the WRF-FWFP appears within the local wind farm and is consistent
 423 with the location of the difference in wind speeds (Figure 14b). Compared to the
 424 WRF-FWFP, WRF-Fitch overestimates the TKE generated throughout the ABL, with
 425 the TKE at the top of the wind turbine being the most overestimated ($0.4 \text{ m}^2\text{s}^{-2}$).



426
 427 **Figure 13.** Horizontal TKE differences at the top of the turbine between (a) WRF-FWFP and
 428 WRF-CTL cases and (b) WRF-Fitch and WRF-FWFP cases, near the surface between (c)
 429 WRF-FWFP and WRF-CTL cases and (d) WRF-Fitch and WRF-FWFP cases, averaged from 12
 430 UTC on 1 January to 18 UTC on 1 January, and the red solid line shows the outer boundary of the
 431 wind farm



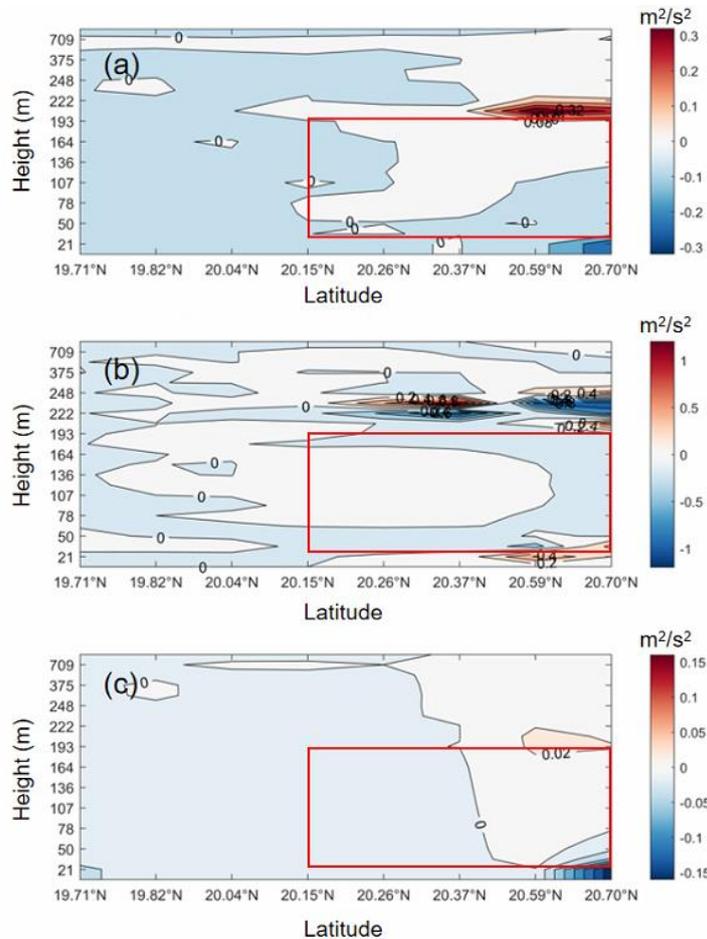
432
 433 **Figure 14.** The same as in Figure 12, but for TKE

434 The TKE budget is then examined. The TKE per unit mass, expressed as $q^2/2$ in
 435 the MYNN model, is predicted by the following equation for a dry atmosphere:

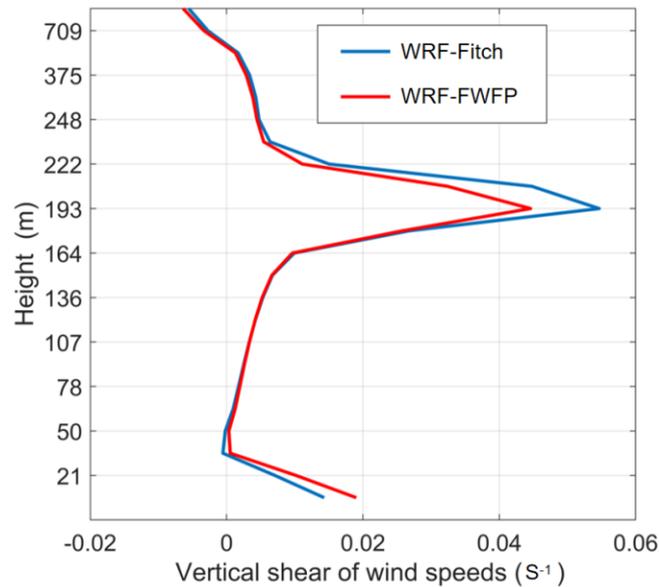
$$\frac{d(q^2/2)}{dt} = P_s + P_b + P_v + P_d \quad (22)$$

436 where P_s is the shear production term, P_b is the buoyancy production term, P_v is the
 437 vertical transport and pressure distribution term, and P_d is the dissipation term. The
 438 details about the equations can refer to Janji (2001).

439 The largest source of the difference in TKE at the top of the turbine is shear
 440 generation (Figure 15a), with the TKE at 235 m still making a positive contribution to
 441 this difference through vertical transport. The other source is dissipation term, which
 442 is the major source of TKE differences in the rotor area. The variation in TKE near the
 443 surface within the wind farm is more complex, with the shear production term, the
 444 vertical transport term, and the dissipation term all being important sources, while the
 445 production of TKE by buoyancy is negligible compared with the other terms (not
 446 shown). At the location of 20.59°N, 111.57°E, the vertical shear of the wind speed is
 447 not only the largest at the top of the turbine for both WRF-Fitch and the WRF-FWFP,
 448 but the difference between the two cases is also the greatest at the top of the turbine
 449 (Figure 16). Specifically, the wind shear is 0.056 s^{-1} for WRF-Fitch and 0.0446 s^{-1} for
 450 WRF-FWFP. This result can actually be inferred from Figure 12b, which shows that
 451 although the maximum value of the difference in wind speed deficit between the two
 452 cases is in the rotor area, this difference varies slightly with height, and the height at
 453 which the variation with height is most pronounced is at the top of the turbine,
 454 followed by the bottom of the rotor area. The smaller wind shear results in the smaller
 455 TKE.



457 **Figure 15.** Vertical transect of the differences in the TKE budget components between WRF-Fitch
 458 and WRF-FWFP cases: (a) shear generation (b) vertical transport (c) dissipation, averaged from 12
 459 UTC on 1 January to 18 UTC on 1 January along the dashed red lines in Figure 11a and 11c. The
 460 red solid line indicates the rotor area.



461 **Figure 16.** Profile of the vertical shear of wind speeds at the location 20.59°N, 111.57°E, averaged
 462 from 12 UTC on 1 January to 18 UTC on 1 January
 463

464 6. Conclusions and discussion

465 Parameters of the column is modified in the VEG module of SWAN to include
 466 the effect of the inertial force to make it suitable for the application of the side column
 467 of a floating offshore wind turbine. At the same time, a series of idealized
 468 high-resolution SWAN simulations are conducted to investigate the dissipation of
 469 wave energy induced by the side columns of floating turbines. It is found that under
 470 certain conditions, the side columns of floating turbines can attenuate more than 50%
 471 of the significant wave height (SWH), and a wave "wake" phenomenon occurs with a
 472 recovery length of ~ 1 km. The mean wave direction is also affected, with a
 473 symmetrical change of about 5° around the side columns, and the mean wave length
 474 increases by more than 20 m. The idealized SWAN simulations and theoretical
 475 analyses show that the attenuation of the SWH becomes smaller with the increase of
 476 the water depth and is enhanced with the increase of the peak wave period. A total of
 477 660 groups of experiments consisting of different incident SWHs, water depths, and
 478 peak wave periods are conducted, and the results of these idealized simulations are
 479 used to train a Gaussian process regression (GPR) model with the Matern 5/2 kernel.
 480 This model can predict the attenuated SWH due to the side columns of the floating
 481 turbine with a given water depth, peak wave period, and incident SWH.

482 The GPR model is implemented in the WRF and the Fitch wind farm
 483 parameterization scheme is modified to form a floating wind farm parameterization
 484 scheme (FWFP). The FWFP modifies the equations for the momentum tendency term
 485 because floating structures affect SWH, then the momentum tendency term must also
 486 account for changes in surface layer momentum fluxes due to changes in SWH. The
 487 difference of the results between the original Fitch scheme and our new FWFP
 488 scheme is analyzed in a realistic simulation using a coupled atmosphere-wave model.

489 Compared with the Fitch scheme, the FWFP scheme increases the total power output
490 with a maximum increase of ~ 5.68 GW. The relative difference is close to 5% in the
491 high wind speed stage. This is due to the fact that the FWFP scheme takes into
492 account the change in roughness of ocean surface, the Fitch scheme overestimates the
493 wind speed deficit within the wind farm. The impacts spread to the atmospheric
494 boundary layer (ABL) and the wakes, but are most pronounced in in the rotor area,
495 which can be up to 0.6 m/s, suggesting a 15 to 24% reduction in wind speed deficits.
496 The impact of the FWFP on the turbulent kinetic energy (TKE) near the surface in the
497 downstream of the wind farm is marginal, and it mainly influences the TKE within the
498 wind farm (including the ABL). The Fitch scheme overestimates the TKE generation
499 compared to the FWFP scheme, with the maximum value of $0.4 \text{ m}^2\text{s}^{-2}$ overestimated
500 at the top of the turbine. Because the FWFP diminishes the vertical wind shear at the
501 top of the turbine, which in turn reduces the TKE generated.

502 Note that a decrease in SWH does not necessarily increase the wind speed in
503 surface layer. In this study, we chose the roughness length parameterization scheme
504 proposed by Taylor & Yelland. (2001), which is a complex iterative computational
505 method where the frictional velocity and roughness length are dependent on each
506 other. The FWFP scheme is only applicable to semi-submersible floating wind
507 turbines because the wind turbine occupying a larger area can induce a significant
508 change in roughness length. In contrast to most sites onshore, the roughness length of
509 the surface offshore is not static, but changes dynamically with sea state. In order to
510 better evaluate the power output of offshore wind farms and their impacts on the
511 environment, it is necessary to improve the offshore wind farms parameterization.

512 **Data availability statement**

513 The NCEP FNL analysis can be download for free at website <https://rda.ucar.edu/datasets/ds083.0/> (NECP, 1999) [Dataset], WW3 can be download at <https://www.ncei.noaa.gov/thredds-ocean/catalog/ncep/nww3/catalog.html> (WW3DG, 2019),
515 and Jason-3 can be obtained from <https://www.ncei.noaa.gov/products/jason-satellite-products> (Lillibridge, 2019). COAWST is freely available online (<https://github.com/DOI-USGS/COAWST>) (Warner et al., 2010).

519 **Acknowledgements**

520 This study is supported by funds from Shenzhen Science and Technology Innovation
521 Committee (WDZC20200819105831001) and the Guangdong Basic and Applied
522 Basic Research Foundation (2022B1515130006). SC is also supported by the
523 Scientific Research Start-up Fund (QD2021021C).

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