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Incorporating H-k Stacking with Monte Carlo Joint Inversion of Multiple Seismic Observables: A Case Study for the Northwestern US

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Key Points:

- We developed a new joint inversion approach that incorporates stacking of receiver function multiple phases with multiple data sets.

- The new approach reduces the trade-offs and improves the determination of deep crustal shear velocity, Moho, and Poisson's ratio.

- Application of the new method to the northwestern US produces a more accurate model that exhibits geologically coherent structures.

Keywords:

Tomography; continental crust; joint inversion; surface waves; receiver functions; H-κ stacking.

Abstract

Accurately determining the seismic structure of the deep crust of continents is crucial for understanding the geological record and continental dynamics. However, traditional surface wave methods often face challenges in solving the trade-offs between elastic parameters and discontinuities. In this work, we present a new approach that combines two established inversion techniques, receiver function H-κ stacking and joint inversion of surface wave dispersion and receiver function waveforms, within a Bayesian Monte Carlo (MC) framework to address these challenges. As demonstrated by the synthetic test, the new method greatly reduces trade-offs between critical parameters, such as the deep crustal Vs, Moho depth, and crustal Vp/Vs ratio. This eliminates the need for assumptions regarding crustal Vp/Vs ratios in joint inversion, leading to a more accurate outcome. Furthermore, it improves the precision of the upper mantle velocity structure by reducing its trade-off with Moho depth. Additional notes on the sources of bias in the results are also included. Application of the new approach to USArray stations in the Northwestern US reveals consistency with previous studies and also identifies new features. Notably, we find elevated Vp/Vs ratios in the crystalline crust of regions such as coastal Oregon, suggesting potential mafic composition or fluid presence. Shallower Moho depth in the Basin and Range indicates reduced crustal support to the topography. The uppermost mantle Vs, averaging 5 km below Moho, aligns well with the Pn-derived Moho temperature map, offering the potential of using Vs as an additional constraint to Moho temperature and crustal thermal properties.
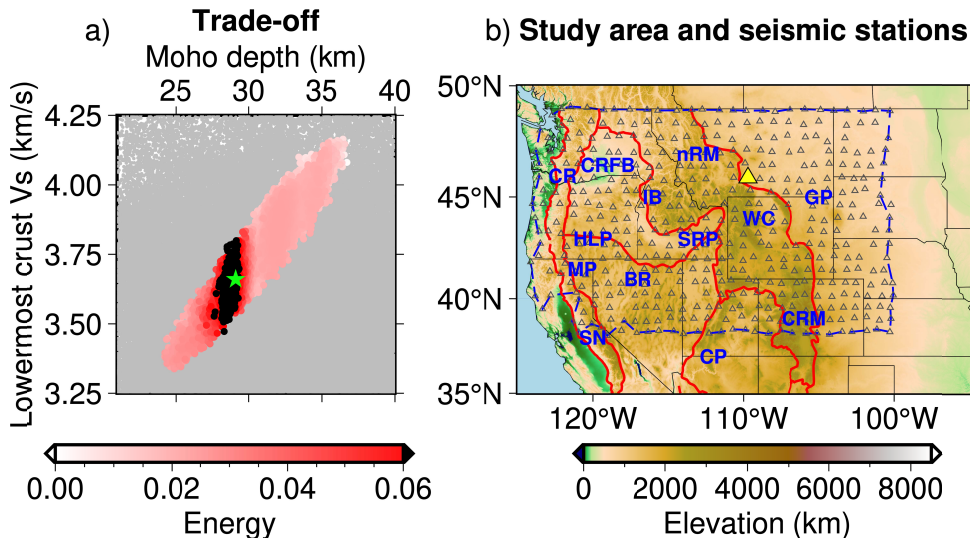
Plain Language Summary

Knowing the seismic structure of the deep crust can help us understand Earth's geological history and how continents evolve. However traditional methods of studying the deep crust face challenges due to tradeoffs that can impact accuracies of the results. In this paper, we present a new approach that combines two existing techniques intending to measure the deep crust more accurately. We tested this method using both simulations and real data and found that it works better than previous methods. We applied this method to the Northwestern US and found that the results aligned with the area's geology, suggesting that the new method is feasible to be applied on a regional scale. The new method provides a more accurate way to study the deep crust and improves the mapping of the uppermost mantle.

1 Introduction

The seismic properties of the continental deep crust are critical to the understanding of the geological history and dynamic processes of the continents. For instance, the depth from the surface to the lower boundary of the crust, i.e., Moho depth, determines the 1st-order variations in surface topography through isostasy (e.g., Schmandt et al., 2015). Seismic velocities of deep crust are often used to infer the magma distributions, or compositional and thermal anomalies (Hacker et al., 2015a; He et al., 2021; Schmandt et al., 2019); Crustal Poisson's ratio, the elastic property related to the ratio between velocities of P and S waves (Vp/Vs), is often associated with the amount of the quartz, a key mineral that dominates the strength and deformation of the lithosphere (Lowry & Pérez-Gussinyé, 2011). As a result, the deep crustal properties such as Moho, velocity, and Vp/Vs have been extensively studied using large-scale seismic arrays, for example, USArray (e.g., Ma & Lowry, 2017; Shen & Ritzwoller, 2016; Sui et al., 2022). Extracting information about the Moho and Vp/Vs ratios is commonly done by analyzing P-wave-converted phases in receiver function (RF) waveforms (Ammon et al., 1990; Langston, 1977). Zhu & Kanamori (2000) proposed a simple method that employs a grid search in the Moho depth and Vp/Vs space (H-κ) to maximize the stacked amplitude of the P-s phase and the following multiple conversions (i.e., PpPs and PpSs+PsPs, Moho-multiples hereafter) in RFs from different events. Thanks to its simplicity, this method quickly gained popularity and has been applied globally, but its dependence on a priori absolute Vs value introduces potential bias in the derived results. On the other hand, surface waves, especially with the development of the ambient noise technique over the past two decades, have proven useful in constraining crustal velocity structure (Ritzwoller et al., 2011) as Rayleigh waves are sensitive to absolute velocity. With the complementary sensitivities of RF and surface waves, the two observables are often combined to infer both absolute velocity and Moho depth (e.g., Juliá et al., 2000; Shen, et al., 2013b). However, the determination of crustal Vp/Vs ratios in such joint inversions using RF waveforms is challenging, as 1)the P-s phase alone cannot solve the trade-off between Moho depth and crustal Vp/Vs; 2) wiggles of the Moho-multiples are either too weak to be directly inverted due to low signal-to-noise ratios or are often obscured by sediments reverberations (Yu et al., 2015); 3) processing like harmonic stripping of RFs to obtain the averaged waveform further suppressed Moho-multiples. As a result, additional pre-processing is usually required to increase the signal-noise ratio (Chen & Niu, 2013) or to remove sediments-reverberations (Yu et al., 2015). Consequently, the Moho-multiples are often not used in the joint inversion with RF waveforms (Shen, et al., 2013b), leaving crustal Vp/Vs poorly constrained and can only be presumed during the inversion (e.g., Juliá et al., 2000). As crustal Vp/Vs trades off with other parameters, it results in insufficient constraints on all parameters of interest. An example of this

84   outcome for joint inversion is highlighted in Fig. 1a, which presents this trade-off based on the
85   result of a synthetic test when crustal Vp/Vs is treated as a free parameter. In this test, we only
86   accept models that fit surface wave dispersion and receiver function waveform that contains only
87   the Moho P-s phase. The scatter plot in Fig. 1a shows two crustal parameters, Moho depth and
88   lowermost crustal Vs (defined as the averaged Vs within 5 km above Moho) from the accepted
89   models. When considering crustal Vp/Vs ranging from 1.6 to 1.9 (typical for crustal rocks), the
90   resulting models exhibit considerable variation in lowermost crustal Vs values, ranging
91   approximately from 3.4 to 4.2 km/s which spans nearly all common lower crustal lithologies
92   (Hacker et al., 2015a). They leave the true uncertainties in Moho depth ~ 4-5 km, underscoring
93   the limitations of existing joint inversion methods in effectively constraining these parameters
94   without knowing the accurate crustal Vp/Vs value.

95   In this study, we propose a new approach that combines the widely used H-κ stacking method
96   with the joint inversion of RF waveforms and surface wave dispersion within a Bayesian Monte
97   Carlo (MC) sampling algorithm, aiming to simultaneously solve the trade-offs mentioned above.
98   Also shown in Figure 1a, although a broad range of models can fit the dispersion curves and RF
99   waveform, only a subset of models exhibits sufficiently high stacked H-κ energy of the three
100 major Moho-converted phases (i.e., Ps, PpPs, and PpSs+PsPs). This demonstrates that if we
101 incorporate H-κ stacked energy into the joint inversion framework, it is possible to resolve the
102 trade-offs among all three parameters simultaneously. Notably, we outline this new method and
103 demonstrate its feasibility through a comprehensive synthetic test in Section 2. Additionally in
104 Section 3, we apply the new technique to investigate the deep crustal structure in the
105 Northwestern United States, which features diverse geological settings, allowing us to assess the
106 method's effectiveness in characterizing various crustal structures. The area has been investigated
107 intensively in the past decade, providing benchmarks for the results to be compared. In Section 4,
108 we discuss the errors associated with the method and present the new features in the resulting 3-
109 D model. We particularly show how our approach additionally improves the understanding of the
110 uppermost mantle structure. Caveats and potential improvement of the method is also included in
111 this Section. We end the paper with a concise summary. We also discuss the shortcomings of this
112 method and where improvements are worthwhile.

113

114

115 **Figure 1. a)** Trade-off between Moho depth and lowermost crust Vs (averaged within 5 km
116 above Moho) observed in a joint inversion of surface wave dispersion and receiver function
117 waveform (Shen, et al., 2013b) based on a synthetic model. In this inversion, the bulk Vp/Vs of
118 the crystalline crust is set as a free parameter. Prior sampling models are plotted as the
119 background in gray color, on top of which are the accepted models from the Monte Carlo search,
120 color-coded by their H-κ stacked energy. The true value of the target model is marked by a green
121 star. **b)** Stations of the EarthScope USArray/Transportable Array (TA) used in this study are
122 shown with triangles. The main geological provinces are outlined with red contours (ref). Station
123 F18A, which is used as an example to demonstrate the new method, is marked by a yellow
124 triangle. The blue dashed line outlines the studied area for which a final 3-D crustal and
125 uppermost mantle model is made. Physiographic locations in the study are identified with
126 abbreviations: Snake River Plain (SRP), Cascade Range (CR), Columbia River Flood Basalts
127 (CRFB), Idaho Batholith (IB), Basin and Range (BR), High Lava Plains (HLP), Modoc Plateau
128 (MP), Great Plains (GP), Colorado Rocky Mountains (CRM), Colorado Plateau (CP), Wyoming
129 Craton (WC), Sierra Nevada (SN), and northern Rocky Mountains (nRM).

130 **2 Methods**

131 During the new inversion process, we aim to determine a one-dimensional (1-D) seismic
132 structure beneath each station location that effectively fits the seismic data. The 1-D model
133 employed in this study follows the methodology proposed by Shen et al. (2013b), which
134 characterizes the shallow Earth as comprising three layers: a sedimentary layer, a crystalline
135 crustal layer, and an uppermost mantle layer. Each layer is defined by a depth-dependent Vs
136 profile and is separated by discontinuities at the base of sediment and Moho. The density and Vp
137 profiles are derived from the Vs profiles. For the sedimentary layer, density, and Vp/Vs values
138 are scaled using empirical relationships established by Brocher (2005). The density scaling for
139 the uppermost mantle layer is determined using the empirical relationship introduced by Hacker &
140 Abers (2004), while the Vp/Vs ratio for the uppermost mantle is fixed at a value of 1.789. In
141 contrast to previous joint inversion studies, where the crystalline crustal Vp/Vs was either held
142 constant (e.g., Shen, et al., 2013a) or scaled from Vs (e.g., Yang et al., 2020), our approach
143 treated it as a free parameter that ranges from 1.55 to 1.95 (see Table.S1 in Supplementary
144 Material for more information about model parameterization). Furthermore, we impose
145 predetermined rules or boundary conditions to constrain the model space (see Table.S2 in
146 Supplemental Material for more details). Specifically, prior constraints are established to ensure
147 that velocity and density exhibit positive jumps across the discontinuities.

148 2.1 Monte Carlo Sampling

149 In order to incorporate the H-κ stacked energy as part of the Bayesian framework, we also
150 modify the MC search. In a Bayesian MC framework, the posterior distribution σ(m) is related to
151 the prior distribution ρ(m) through likelihood function L of any given model m:

$$\sigma(m) \propto \rho(m)L(m) \qquad (1)$$

152 To sample the posterior distribution, we created the MC chain following the flowchart in Fig. 2.
153 In this chain, a new model (m_{new}) is generated based on the last accepted model (m_{old}) and is

154 accepted or rejected according to a chance p which is determined by comparing its likelihood
155 $L(m_{new})$ to the likelihood of the last accepted model ($L(m_{old})$). For joint inversion of surface
156 wave dispersion and receiver function waveforms, likelihood ($L^S(m)$) is defined based on the
157 misfit $S(m)$ between the predicted $d(m)$ and observed data d^{obs}:

$$L^S(m) = exp\big(-0.5S(m)\big) \qquad (2)$$

158 where

$$S(m) = (d(m) - d^{obs})^T C_e^{-1}(d(m) - d^{obs}) \qquad (3)$$

159 In the new approach, we further defined an additional likelihood function for the H-κ stacked
160 energy for each newly generated model:

$$L^E(m) = exp\big(E^n(m)\big)^a \qquad (4)$$

161 Where the E^n represents the normalized stacked energy of predicted *Ps*, *PpPs*, and *PsPs+PpSs*
162 phases for all usable teleseismic events:

$$E^n(m) = \frac{1}{N * E^{ref}(m)} \sum_{i=0}^{N} w_1 RF^{[i]}\left(t_{Ps}^{[i]}(m)\right) + w_2 RF^{[i]}\left(t_{PpPs}^{[i]}(m)\right)$$
$$- w_3 RF^{[i]}\left(t_{PsPs+PpSs}^{[i]}(m)\right). \qquad (5)$$

163 Where w_k(k=1,2,3) are the weighting of *Ps*, *PpPs*, and *PsPs + PpSs* phases and are empirically
164 set to be 0.3, 0.4, and 0.3 in this study, respectively. N is the number of RF waveforms that are
165 stacked. The E^{ref} is a reference energy that is used to normalize stacked energy to be mostly
166 between 0 and 1. An ad-hoc factor a is empirically set so that the MC search is guided toward
167 maximizing the H-□ stacked energy at a similar rate of fitting other data. $t_{Ps}(m)$, $t_{PpPs}(m)$, and
168 $t_{PsPs+PpSs}(m)$ are the arrival time of *Ps*, *PpPs*, and *PsPs + PpSs* phases, predicted based on
169 model m, respectively. In traditional H-κ stacking introduced by Zhu & Kanamori (2000), the
170 arrival time is calculated based on a simple two-layer model, involving only the thickness (i.e.,
171 Moho depth) and velocity of the upper layer (i.e., crust). Later, Yeck et al. (2013) developed the
172 sequential H-κ stacking method based on this foundation. They separated the sedimentary layer
173 from the crust and constructed a three-layer model (sedimentary layer, crystalline crust layer, and
174 mantle layer). The calculation of arrival times in Yeck's approach involves the thickness and
175 velocity of both the sedimentary and crystalline crust layers. Although our model is also divided
176 into three basic layers (sedimentary layer, crystalline crust layer, and mantle layer; see Table.S1
177 model parameterization in Supplemental material), each basic layer, in fact, consists of a more
178 refined 1-D velocity profile (as shown in Fig.3a). Therefore, our arrival time calculations differ
179 slightly from traditional H-κ stacking, as shown below:

$$t_{Ps}(m) = \sum_{k=1}^{l} h_k(m) \times \left(\sqrt{\frac{1}{V_{k,s}^2(m)} - p^2} - \sqrt{\frac{1}{V_{k,p}^2(m)} - p^2} \right) \qquad (6)$$

$$t_{PpPs}(m) = \sum_{k=1}^{l} h_k(m) \times \left(\sqrt{\frac{1}{V_{k,s}^2(m)} - p^2} + \sqrt{\frac{1}{V_{k,p}^2(m)} - p^2} \right) \quad (7)$$

$$t_{PsPs+PpSs}(m) = \sum_{k=1}^{l} 2h_k(m) \times \left(\sqrt{\frac{1}{V_{k,s}^2(m)} - p^2} \right) \quad (8)$$

180   Where l is the number of layers above the Moho, while h_k, $V_{k,s}$, and $V_{k,p}$ denote the thickness, Vs,
181   and Vp of the k-th layer, respectively.

182   As an iterative approach, MC inversion needs an initial model to begin the iteration. In each
183   round of MC sampling, the initial model is independently randomly generated within the model
184   space. For each inversion, we perform 30 rounds of sampling, with each sampling iterating 8000
185   times. This means that one inversion generates 240,000 models (including all accepted and
186   rejected ones). After the whole search (30 rounds of sampling) is complete, we perform several
187   post-processing operations, including:

188   1) Removing certain models. Near the beginning of the sampling, a few models are accepted
189   before they enter the equilibrium state, so these models should be discarded based on
190   their high misfit to dispersion, receiver function waveforms, and low H-κ stacked energy.

191   2) Calculate the average of the accepted model ensemble which defines the final inverted
192   model.

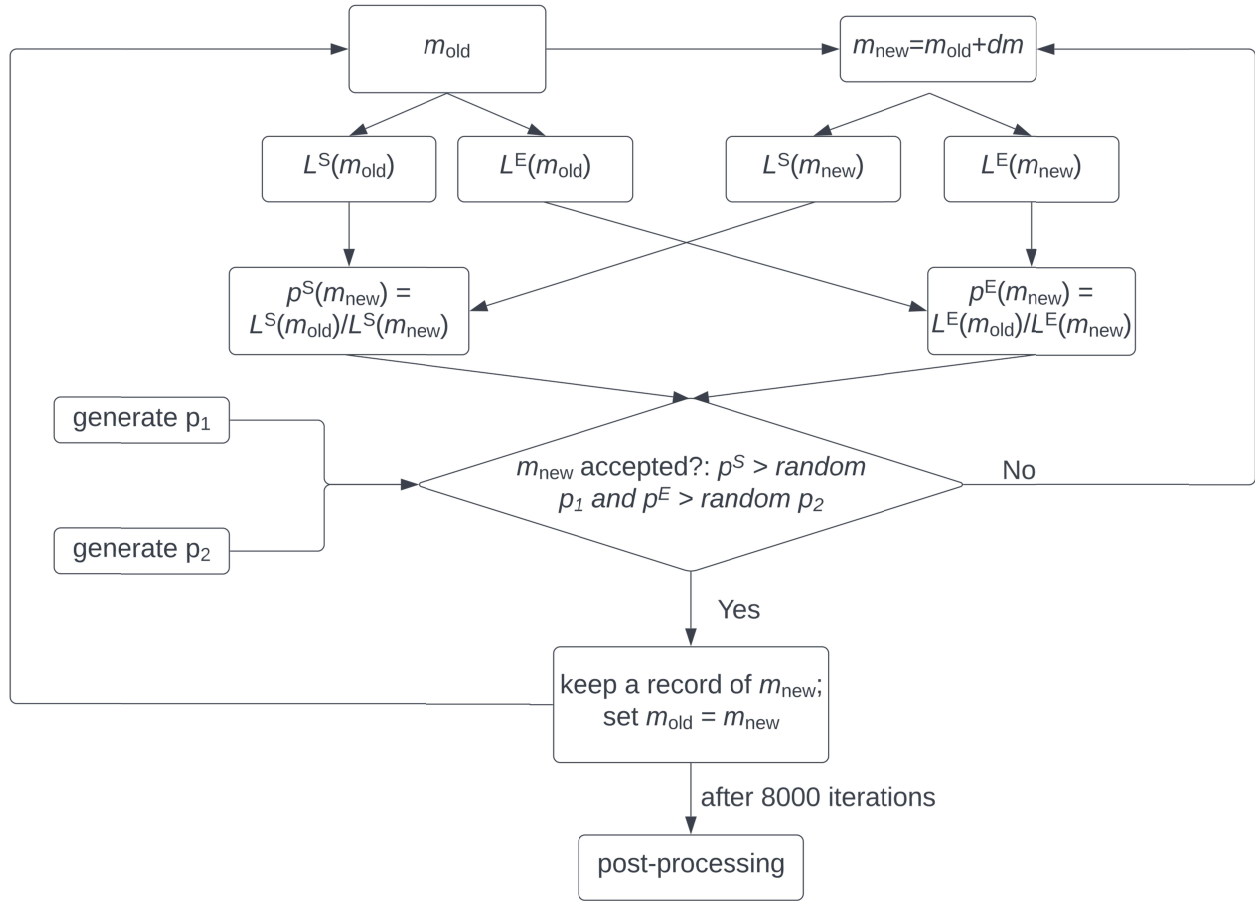193   3) Calculate the standard deviation of the ensemble.

194

Figure. 2. A flowchart of the new joint MC sampling incorporating H-κ stacking. $L^S(m)$ and $L^E(m)$ are likelihood functions associated with the misfit and the H-κ energy, respectively. p^S and p^E are the probabilities of being accepted according to misfit-related likelihood and the H-κ energy-related likelihood, respectively. The acceptance is determined by comparing p^S and p^E with randomly generated numbers between 0 and 1 (i.e., p_1 and p_2) These two numbers are independently randomly generated in every iteration. The process highlighted here begins after an initial model is generated, and 'post-processing' begins after samplings are performed on 30 different initial models.

2.2 Synthetic test

In our study, we conducted a synthetic test to evaluate the performance of the proposed approach. A target model is designed as shown by the red lines in Fig. 3a (labeled as 'target'), and the proposed approach is applied to the data generated based on this target model. This target model features a monotonically increasing crustal Vp/Vs ratio with a bulk value of ~ 1.74, a crustal thickness of ~ 29 km, and an average lowermost crustal Vs of ~ 3.66 km/s. The synthetic datasets, including ~200 RF waveforms with different ray parameters for H-k stacking (Fig.3b), surface wave dispersion (Fig.3c), and the first 10-sec RF waveform (Fig. 3d) with a ray parameter of 0.06s/km. All data are added by normally distributed random noise based on real practice (see Table.S2 in Supplemental Material for more information about noise level). When

213   applied to real data, individual RFs will be the raw RF waveforms generated by individual
214   events, and the first 10-sec RF waveform will be the representative RF that is slowness corrected
215   and azimuthally averaged from all events (e.g., Shen, et al., 2013b).

216   Fig.3 and Fig.4 present the results of the synthetic test. The ensemble average (blue line, labeled
217   as 'inverted') of the Vs model, which is considered as the final inverted model, closely resembles
218   the target model and well predicts the arrivals of Moho-converted phases, group and phase
219   velocities, and RF waveforms (Fig.3b-d). Please note that in our target model configuration, the
220   Vp/Vs ratio of the crystalline crust is not a uniform value but varies with depth (Fig.S1b) with a
221   bulk value of ~1.741. However, during the MC inversion, the Vp/Vs ratio of the crystalline crust
222   is perturbed and inverted as a single value. In other words, this new approach aims to obtain the
223   bulk Vp/Vs ratio of the crystalline crust, instead of a fine 1-D Vp/Vs structure. Consequently, in
224   theory, the Vp structure cannot be accurately resolved (Fig.3a). Using the new approach, the
225   trade-offs between lowermost crust Vs, Moho depth, and crustal Vp/Vs are greatly reduced
226   (Fig.4d-f), leading to more precise results close to the true values of the target model (Fig.4a-c).
227   This test demonstrates the feasibility of the proposed approach when applied to synthetic data.
228   We note that a small bias in Moho depth is observed, and this will be discussed with more detail
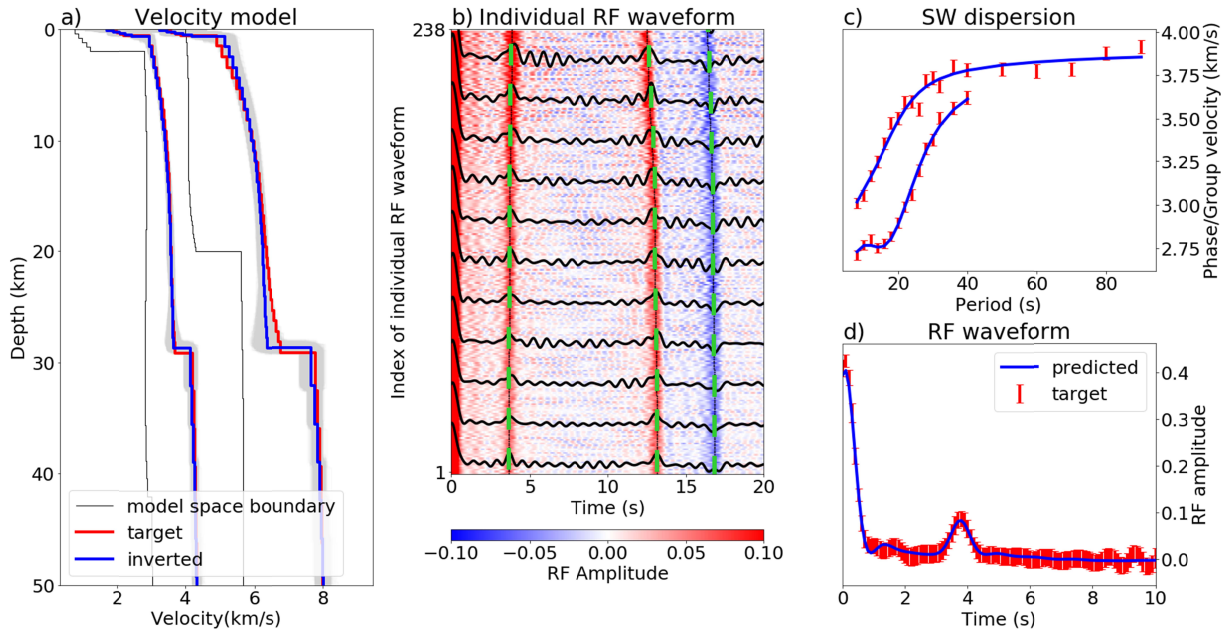229   in Section 4.1.

230

231   **Figure 3.** Inversion result of the synthetic test. **a**) S-wave and P-wave velocity models. The
232   target model (red lines, the model we used to generate the synthetic data) and the inverted model
233   ensemble (grey profiles) that was accepted by the MC sampling are presented, and the average of
234   the accepted model ensemble is shown by the blue lines, for both P and S wave profiles. The
235   model space for Vs is highlighted by two thin profiles. **b**) Data fitting to the H-κ stacked energy.
236   The black wiggles are examples of RF waveforms with small vertical green bars that denote the
237   predicted arrival time for the Moho-converted phases (e.g., Ps, PpPs, and PpSs+PsPs phase)
238   based on the inverted model (blue lines in Fig 3a). All receiver function data involved in the
239   inversion is plotted as colored backgrounds and indexed according to their slowness. **c-d**) Data

240 fitting to surface wave dispersion and RF waveform. The red bars represent the synthetic data
241 (generated from the target model) with normally distributed random noise added. The blue lines
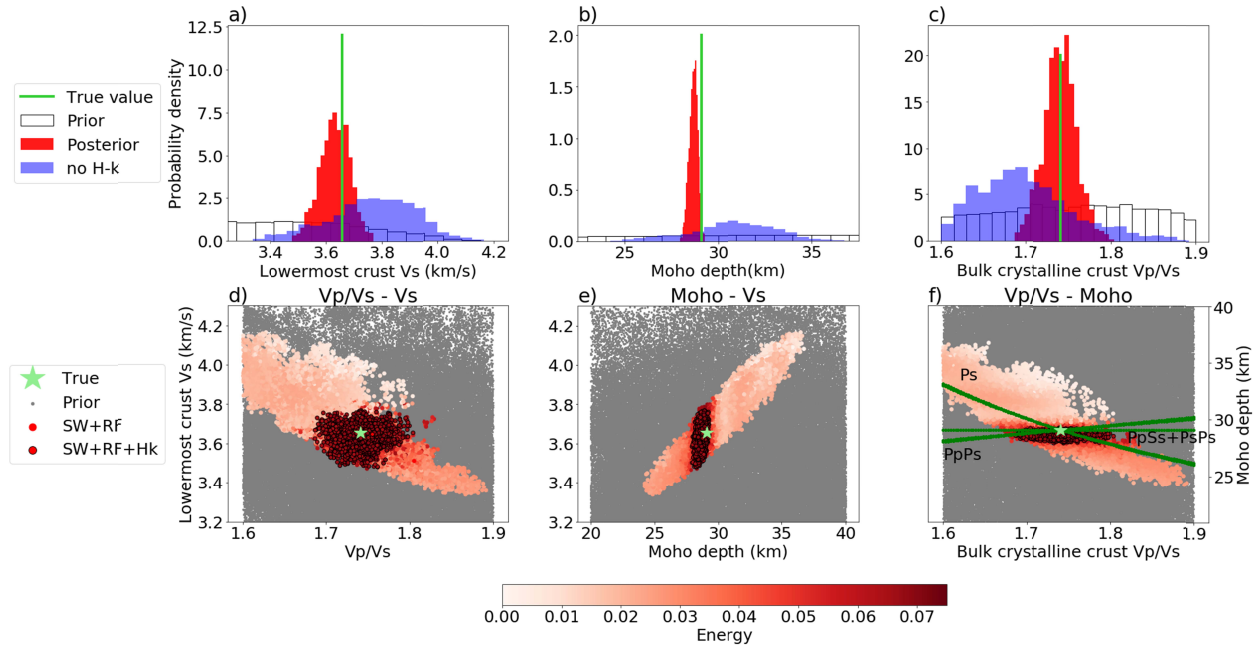242 denote the data predicted by the inverted model (blue lines in panel a).

243
244 **Figure 4. a–c)** Prior and posterior distribution of lowermost crust Vs, Moho depth, and
245 crystalline crust Vp/Vs. Prior distributions are plotted as background in white histograms. Red
246 histograms represent the posterior distribution generated by the new approach which uses surface
247 wave dispersion, RF waveform, and H-κ stacked energy. Blue histograms represent the posterior
248 distribution generated by traditional joint inversion which only uses SW dispersion and RF
249 waveform. The true value of each parameter is marked by the green vertical lines. **d)** Trade-off
250 between the lowermost crust Vs and bulk crystalline crust Vp/Vs. Each reddish dot represents an
251 accepted model, color-coded by its stacked H-κ energy. The results of the traditional joint MC
252 inversion are marked by open dots color-coded by their H-κ stacked energy. The results of the
253 new joint inversion are marked by closed dots, also color-coded by the corresponding H-κ
254 stacked energy. The green stars represent the true values of the target model. **e)** Similar to d, but
255 for the trade-off between the Moho depth and lowermost crust Vs. f) Similar to Fig d, but for the
256 trade-off between the crystalline crust Vp/Vs and Moho depth. The dark green lines represent the
257 theoretical H-κ relations between Moho depth and bulk crystalline crust Vp/Vs for different
258 Moho-converted phases (Zhu & Kanamori, 2000).

259 **3 Applying the new method to Northwestern US**

260 To demonstrate the feasibility of our new approach to real data, we applied it to ~ 450 USArray
261 stations in the northwestern US (Fig.1b), where the region has been extensively studied using
262 both H-κ stacking (Eagar et al., 2011) and surface wave-RF joint inversions (Delph et al., 2018;
263 Shen, et al., 2013a). The Rayleigh wave dispersion curves and representative RF waveforms with
264 uncertainties are collected from Shen & Ritzwoller, (2016), and the individual raw RF
265 waveforms are collected from Sui et al. (2022). The frequency content of individual RFs used for

266   H-κ stacking was chosen by the common choice of the Gaussian parameter of 2.5 (centered
267   around 1 sec). The RFs are computed from three-component seismograms using a time-domain
268   iterative deconvolution method (Ligorría & Ammon, 1999) and then undergo a 5-stage quality
269   control which removes the poor-quality data (Sui et al., 2022) After the rigorous quality control
270   scheme by Sui et al., (2022), this station retained 47 high-quality RF waveforms that can be used
271   to calculate H-κ stacked energy during the MC inversion.

272   Fig.5 shows the inversion result of an example station F18A, which is in Big Timber, MT, off
273   the Rocky Mountain front range. As shown in Fig. 5b, three major Moho-converted phases (i.e.,
274   Ps, PpPs, PsPs+PpSs) can be identified in the RF waveforms. The joint MC inversion yielded ~
275   6000 1-D models, and their average model successfully predicts the arrival times of Moho-
276   converted phases (Fig. 5b), while simultaneously fitting the dispersion and the representative RF
277   waveform (Fig. 5c-d). The posterior marginal distribution shows significant reductions in
278   uncertainty compared to the posterior distribution generated by the inversion without H-κ
279   energy: the uncertainty in crustal Vp/Vs is reduced by ~ 71%; Moho depth uncertainty is reduced
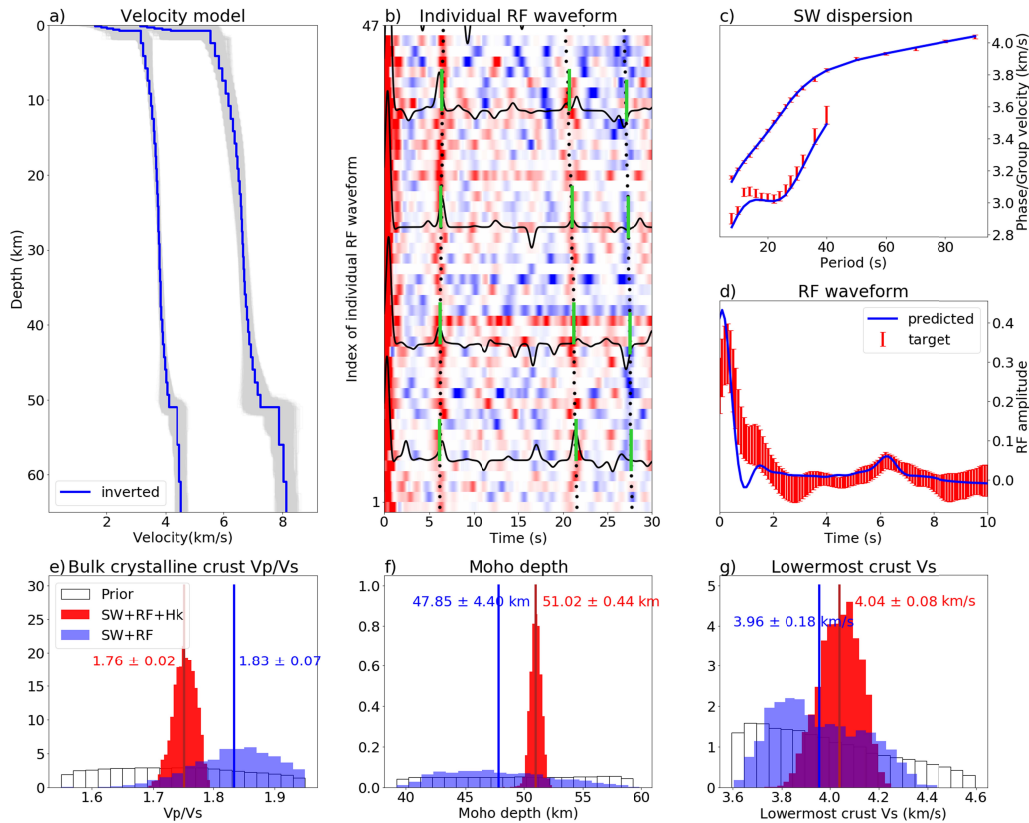280   by 90%; and lowermost crust Vs uncertainty is also reduced by more than 50%.

281

Figure 5. Result for USArray station F18A from the new approach. **a-d**) Similar to Fig.2a-d; **e-**
g) Similar to Fig.3a-c. The red and blue vertical lines represent their respective mean, with the
specific numerical values (mean +/- standard deviation) labeled next to them.

285   Out of the ~ 450 stations in the study region with all three data types, meaningful results were
286   successfully produced for more than 70% of them, except for those in the Great Plains due to
287   complications arising from the thick sedimentary cover that generates reverberations and masks

288   the Moho-converted phases that we aim to use. Those impacted stations often have higher misfit
289   and low stacked energy and are not used for further analysis. The resulting 1-D models were then
290   combined to form a 3-D seismic model for the crust and uppermost mantle. As this study focuses
291   on how the combination of H-κ stacked energy helps constrain the deep crustal structures
292   (including Moho), the presentation of the results is primarily focused on the corresponding
293   parameters.

294   As shown in Fig 6, the Vp/Vs map reveals an average Vp/Vs value of ~ 1.77 for the crystalline
295   crust, with variations highly correlated with tectonic boundaries. High Vp/Vs is found near the
296   High Lava Plain (e.g., S. Oregon), which is also connected with relatively high Vp/Vs along the
297   Snake River Plain. The most prominent low Vp/Vs is seen in southern Idaho, northern Oregon,
298   and Washington, encompassing the Idaho Batholith and along the northern Cascades. Both the
299   Moho depth map and lowermost crust Vs map exhibit a west-east dichotomy. The thinnest crust
300   is observed in regions such as the Basin and Range and Columbia River Flood Basalts, while the
301   thicker crust is observed in the Great Plains, Wyoming Craton, and Colorado Rocky Mountains.
302   The western region exhibits lower velocities, except for a relatively higher velocity in the
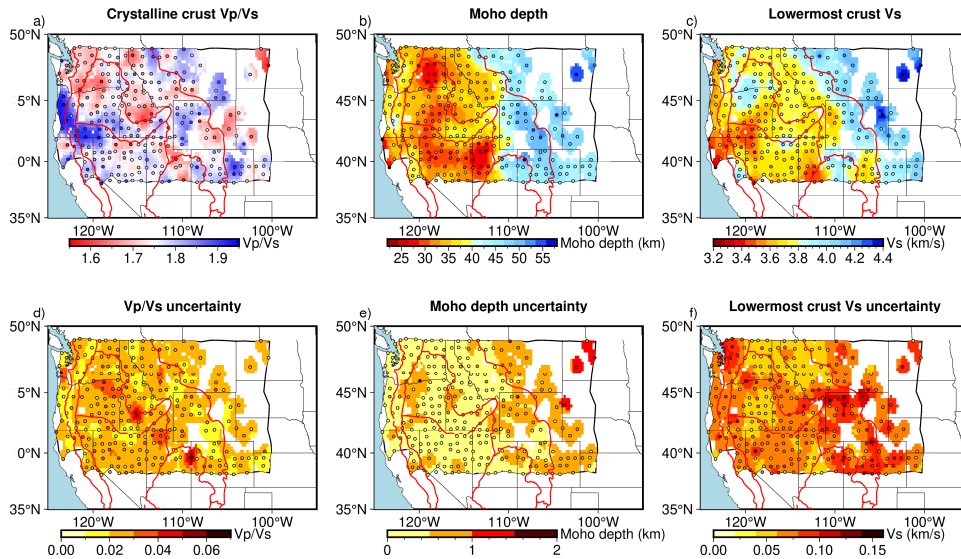303   Columbia River Flood Basalt compared to its surroundings.

304

Figure 6. Crustal architecture of the NW US. derived from the new approach **a)** Bulk Vp/Vs of
crystalline crust, **b)** Moho depth, and **c)** averaged Vs within 5 km above the Moho. **d-f)**
Corresponding 1-standard deviation of the posterior distributions.

4 Discussion and conclusion

4.1 Systematic errors

310   Model errors include systematic and nonsystematic errors. The nonsystematic errors should
311   encompass model fluctuations and will be controlled predominantly by errors in the data and
312   trade-offs between model parameters at different depths **(**Shen & Ritzwoller, 2016) Specifically,
313   our method yields average uncertainties (1-sigma) in crustal thickness of ~ 0.5 km (Fig. 4c),
314   representing a substantial improvement over previous joint inversion results that did not involve

315 H-𝜅 stacked energy (e.g., Shen, et al., 2013a) , with uncertainties of ~4 km). This improvement
316 can be attributed to including PpPs and PsPs+PpSs phases in the inversion process. Furthermore,
317 the more precise determination of Moho depth reduces the uncertainties in the lowermost crustal
318 Vs to ~0.07 km/s, a 30% reduction compared to the uncertainties reported by Shen, et al. (2013a)
319 (~0.1 km/s). In this section, we mainly discuss the systematic errors.

320 Systematic errors come from the assumptions and the method itself. Shen & Ritzwoller (2016)
321 introduced the traditional MC joint inversion method, and they elucidated three pivotal factors
322 linked to systematic errors, which are 1) the scaling of density from Vs; 2) the choice of Q in the
323 mantle; and 3) the scaling relationship between Vp and Vs. Given that our approach is rooted in
324 their method, it inherits these problems to some extent. Regarding the first two factors, Shen &
325 Ritzwoller (2016) conducted an exhaustive discussion, thus obviating the necessity for further
326 elaboration in this context. The third factor is that they were unable to constrain Vp/Vs, and
327 therefore had to set it as a prior parameter. Our novel approach addresses this issue by
328 incorporating H-𝜅 energy into inversion. However, the inclusion of the H-𝜅 data introduces yet
329 another layer of systematic error. The MC inversion involves obtaining a set of models that can
330 reasonably fit the data (i.e., with a misfit below a critical value and H-𝜅 energy above a critical
331 value) and then using their average as the final result, instead of selecting the model that fits the
332 data 'best' (i.e., smallest misfit or highest energy). This strategy is employed due to the
333 recognition that the presence of errors in the data can lead to an overfitting of the model to these
334 errors when opting for the 'best-fitting' model. It is worth noting that as long as the errors in data
335 are completely random and unbiased, this strategy itself should not introduce systematic errors.

336 However, some biases remain when H-𝜅 energy is incorporated into the joint inversion. The
337 essence of H-𝜅 stacking is to fit the arrival times of different phases by searching for the model
338 associated with the maximum energy. This operation relies on the underlying assumption that the
339 maximum energy (amplitude) corresponds precisely to the true arrival time of each Moho-
340 converted phase. However, this assumption does not always hold true. In instances where a thin
341 low-velocity sedimentary layer is present (such as the target model in the Section 2.2 synthetic
342 test), the Moho-converted phases (particularly the PpPs and PsPs+PpSs phases) may be
343 contaminated by additional reverberations generated by other discontinuities (e.g., the bottom of
344 sedimentary layer or/and velocity changes in the lower crust) given that individual phases are
345 limited in frequency. This contamination to Moho converted phases causes the waveform
346 distortion that shifts the maximum energy or generates an asymmetric phase (e.g., Fig. 7).
347 Consequently, the maximum energy no longer coincides with the true arrival time, as shown in
348 Fig.7g-i. As a result, the final inverted model becomes biased, manifesting as a shallower Moho
349 or/and higher Vs (to generate shorter arrival times). It's worth noting that this systematic error
350 primarily manifests in the estimates of Moho depth and Vs, with minimal impact on Vp/Vs – this
351 can be observed in both the posterior distribution (Fig.4a-c) and the trade-off plots (Fig. 4d-f).
352 This also aligns with the perspective presented in Zhu & Kanamori's paper for H-𝜅 stacking
353 (2000), which suggests that bias in Vs primarily affects the estimation of Moho depth with a
354 lesser impact on Vp/Vs.

It can be noticed that in cases where the sedimentary layer is sufficiently thick, the issue of maximum energy shift no longer persists (Fig.7d-f). In such scenarios, the additional reverberations from near-surface structures will arrive later to the extent that they are separated from the Moho-converted phases. However, even in this circumstance, an asymmetry problem remains. In a simple two-layer model comprising a crust and a mantle layer with constant velocities, the shape of the Moho-converted phase is symmetric with respect to the theoretical arrival time (Fig.7a-c). However, when contaminated by additional reverberations, the Moho-converted phases are not symmetric anymore even though the arrival of the maximum energy might not be affected. As indicated in Fig.7d-f, the energy of the left side (associated with shorter travel times) of the PpPs and PpSs+PsPs phases is stronger than that on the right side (related to longer travel times). In such cases, the MC search will tend to favor the models that can predict shorter arrival times (manifested as higher Vs or/and thinner Moho), despite the maximum energy remaining aligned with the true arrival.
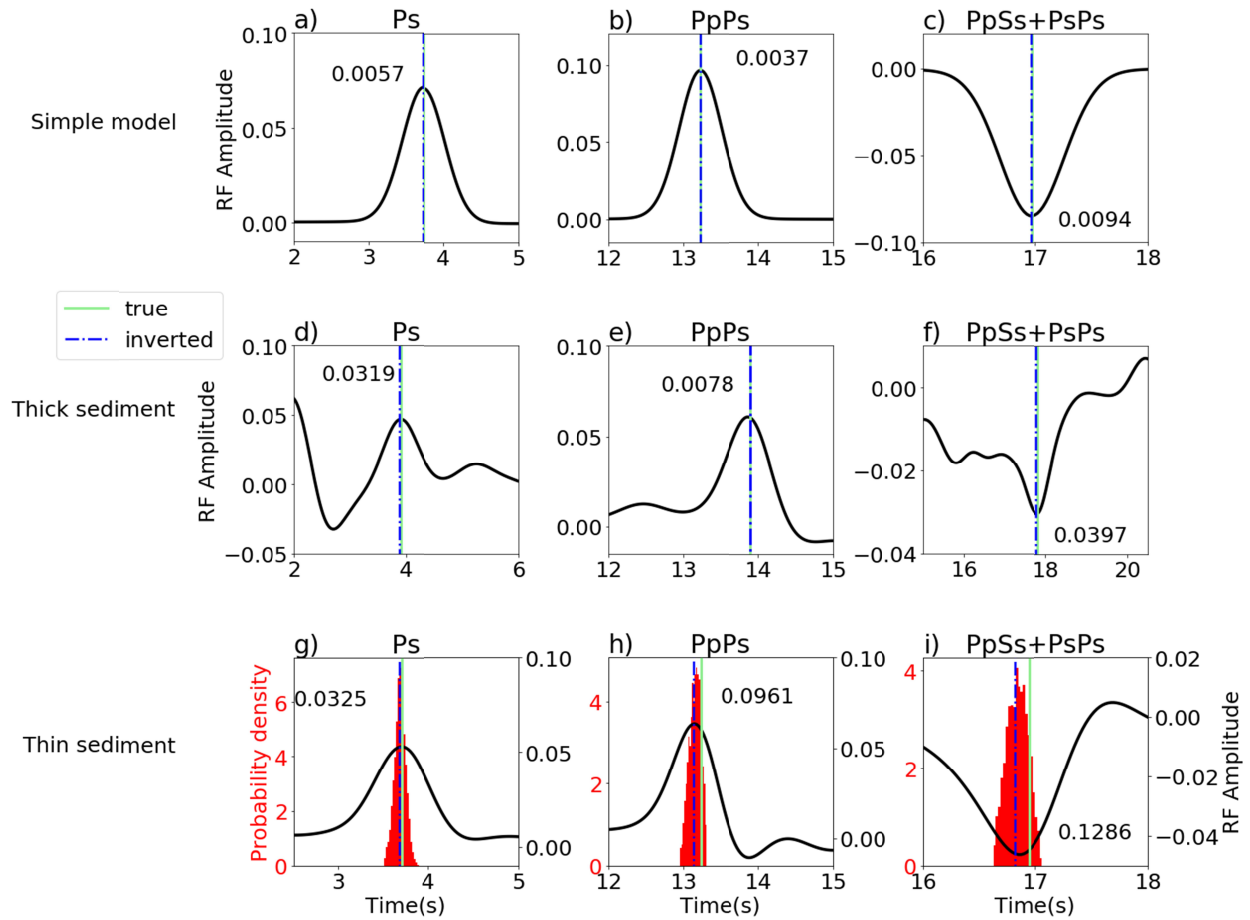

Figure 7. Noiseless synthetic RF waveforms with a ray parameter of 0.04 s/km. **a)** - **c)** Ps, PpPs, and PpSs+PsPs phases of RF waveform that are generated based on a simple two-layer model that consists of a 40-km-thick crust layer with Vs of 3.5 km/s and a 160-km-thick mantle layer with Vs of 4.3 km/s, respectively. **d)** - **f)** Similar to panels a-c, except that they are generated based on a more complex model with a thicker sediment layer (2.6km). **g)** - **i)** Similar to panels

374   d-f, except that they are generated based on the target model used in the synthetic test in Section
375   2.2, which has a thin sediment layer (0.6km). The green vertical bars represent the true arrival
376   times of targeting Moho-converted phases (i.e., Ps, PpPs, and PpSs+PsPs), and the blue vertical
377   bars represent the arrival times calculated based on the final inverted model. Note that the true
378   arrival times of the Moho-converted phases do not correspond to the maximum energies in the
379   waveform due to interference of other phases, especially in the case of thin sediments. The
380   differences between the true (green) arrival times and inverted (blue) arrival times are labeled by
381   black text (unit is sec) in each plot. The arrival times calculated based on each accepted model
382   are plotted as the red background histograms in g-i. Note that phases based on the simple model
383   are symmetric and the maximum energy corresponds to the theoretical arrivals of the Moho
384   multiples. All three corresponding models can be found in supplemental materials (Fig.S2).

385   Assessed by the difference between the true arrival and the arrival predicted based on the
386   inverted model, the bias introduced by the asymmetrical phases is significantly smaller than the
387   bias introduced by the maximum energy shift. We also did the same synthetic test using the
388   model with a thick sedimentary layer and the simple two-layer model, respectively (see Fig.S4 &
389   Fig.S5 in the supplemental material for more information on inversion results). The noise level is
390   set the same as it is in section 2.2. The difference between the true Moho depth and the inverted
391   Moho depth is 0.43 km, and 0.17 km for the thin and thick sediment model tests, respectively.
392   For the simple two-layer model, the test reveals a 0.13 km difference in Moho depth, probably
393   from random noise we added to the data. The 1-sigma of the Moho depth is 0.23km for the test
394   with a thin sediment model, ~ 50% of the systematic bias. This indicates that the potential
395   systemic errors might exceed the random errors for certain stations with sedimentary cover and
396   make the uncertainties presented underestimated.

397   **4.2 Benchmark of the resulting model**

398   The map views of the Vp/Vs from selective previous studies (Ma & Lowry, 2017; Sui et al.,
399   2022 and EARS, the EarthScope Automated Receiver Survey, Crotwell & Owens, 2015, Trabant
400   et al., 2012) are plotted in Fig.8 for comparison. It should be noted here that the Ma & Lowry,
401   2017 and EARS results are for the bulk crust, while our result and Sui et al. (2022) are for the
402   crystalline crust. Over, the general variations in the Vp/Vs map are consistent, but the new result
403   reveals more pronounced and geologically correlated variations (e.g., the contrast between the
404   Snake River Plains and Idaho Batholith). The result from the EARS project is fully automatically
405   generated using the classic H-κ stacking method. This automatic processing uses a less strict
406   quality control scheme compared with other studies, generating a more mosaic map affected by
407   the data noise. It also treats crust as a simple single-layer model, which also introduces bias due
408   to the effects of the sedimentary layer (Yeck et al., 2013). Sui's result (Fig. 8b) is derived using
409   sequential H-κ stacking (Yeck et al., 2013) which treats the sedimentary layer and crystalline
410   crust separately. The sequential H-κ stacking reduces the influence of the sediment layer, and
411   their map features very similar patterns to our result. The map from Ma & Lowry (2017) is
412   obtained by a joint inversion of Bouguer gravity anomalies and seismic receiver functions. It is
413   worth noting that the gravity data in that study are used to indirectly constrain the Vp/Vs, which
414   depends on a general relationship between density and Vp/Vs. As crustal rocks vary, this

415 relationship may not hold true everywhere. Our study, in contrast, directly constrains the Vp/Vs
416 and eliminates the need to assume such a Vs-density relationship, leaving gravity an independent
417 metric for estimating density separately in the future. In addition, results from the three previous
418 studies are subject to the assumption in crustal Vs or Vp, which may introduce biases and
419 uncertainties. In comparison, our approach addresses these limitations by simultaneously
420 constraining both the velocity structure and Vp/Vs ratio, resulting in a significant reduction in
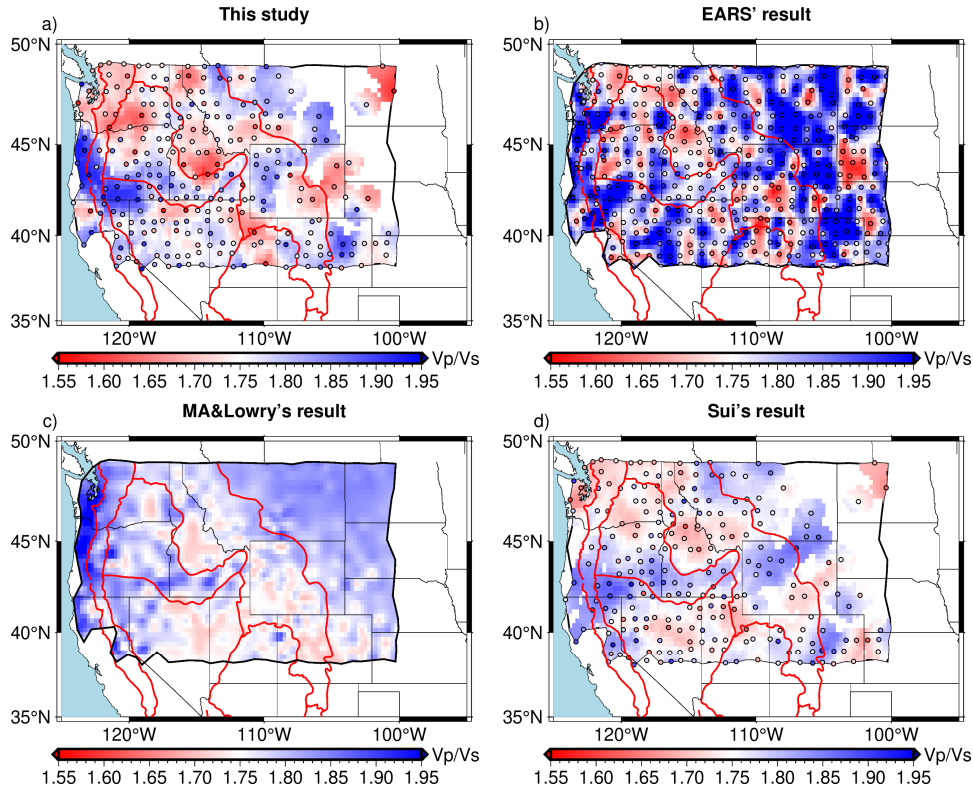421 uncertainty and trade-offs.

423 **Figure 8.** Comparison of Vp/Vs maps from different studies. **a**) Bulk Vp/Vs of crystalline crust
424 obtained in this study. **b**) Bulk Vp/Vs of the crust (including both the sediment layer and
425 crystalline crust) derived from the automatically processed H-k stacking (EARS, Crotwell et al.,
426 2005, Trabant, et al., 2012). The Vp/Vs values are depicted using the same color scale to
427 highlight the general consistency and differences in details from various approaches. **c**) Bulk
428 Vp/Vs of the crust (including both the sediment layer and crystalline crust layer) constrained by
429 RFs and gravity data (Ma & Lowry, 2017). **d**) Bulk Vp/Vs of crystalline crust derived through
430 sequential H-κ stacking (Sui et al., 2022).

431 The map view of lowermost Vs and Moho depth of Shen & Ritzwoller's 2016 model (SR2016)
432 are plotted in Fig.9 for comparison. The SR2016 model is obtained by the traditional MC
433 inversion using surface wave data and the first 10-s averaged RF waveform, assuming the bulk
434 Vp/Vs ratio of the crystalline crust is 1.75. Compared with the SR2016 model, the Moho depth is
435 generally thinner, and it exhibits a stronger contrast in crustal thickness between the tectonically
436 thinned (rifted) western United States and the stable central/eastern United States. For example,
437 ~ 5 km thinner in the Basin and Range, Columbia River Flood Basalt, and High Lava Plain are

438 observed. It also indicates a discernible decrease in the lowermost crust Vs, with an average
439 reduction of ~ 4% when compared with the SR2016 model, especially in regions like Modoc
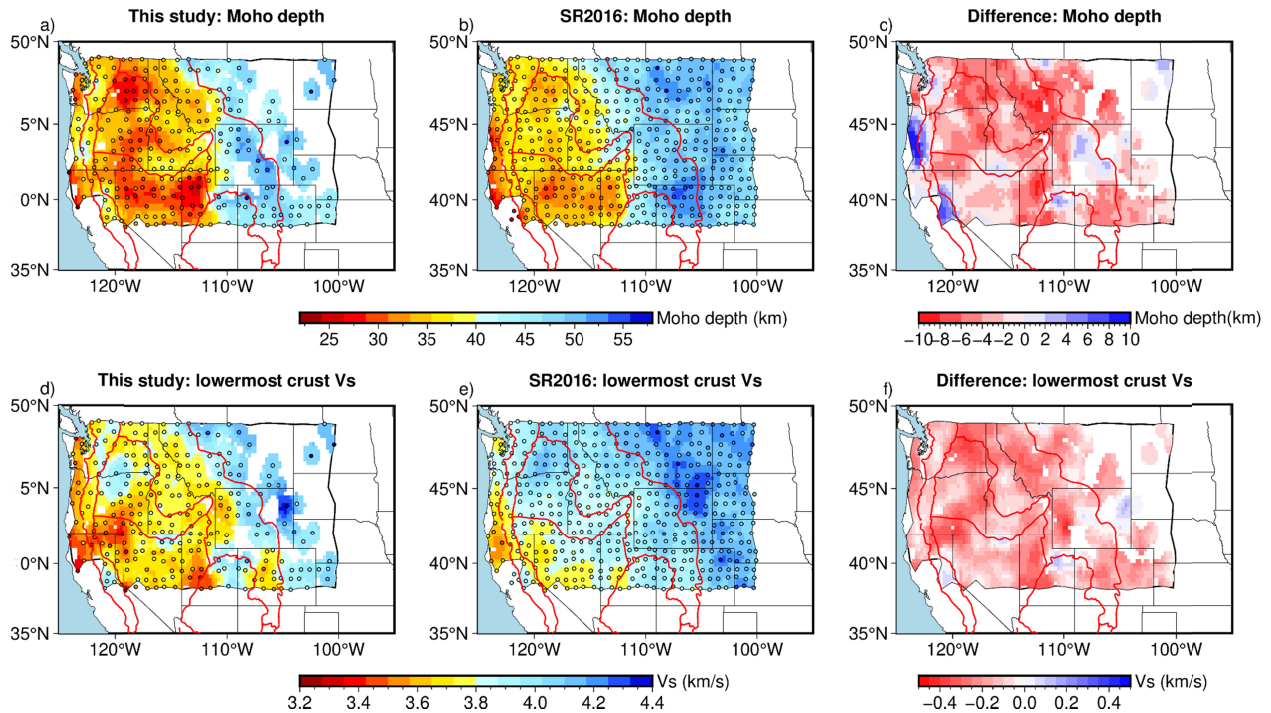440 Plateau, and the boundary between Colorado Plateau and Basin and Range.

441

Figure 9. Comparison of Moho depth (**a-c**) and lowermost crust Vs (**d-f**) with SR2016 model.
Panels from the left column to the right column are the results of this study, the SR2016 model,
and the difference between them (This study – SR2016), respectively.

4.3 Other improvements and implications

446 Seismic attributes are influenced by various factors such as temperature, chemical composition,
447 the presence of partial melting, or fluids. Therefore, conversely, seismic models can be used to
448 infer these factors.

449 One notable feature in the Vp/Vs map is the high Vp/Vs ratios in the crystalline crust of coastal
450 Oregon. The Vp/Vs ratios, ranging from ~ 1.85 to ~1.95, stand out as particularly high for crustal
451 rocks (Christensen & Mooney, 1995). Several possible mechanisms may produce such elevated
452 Vp/Vs ratios. These include: 1) mafic composition; 2) the existence of the cracks and fractures
453 that lower the Vs; 3) the existence of fluid (e.g., melt) that lowers the Vs than to Vp; It has been
454 speculated that this region might be accreted to the main continent during the early Eocene and
455 may bear distinct crustal composition than other regions (Wells et al., 2014). Additionally,
456 careful receiver function analysis has identified a layer bearing slab-bearing fluids at deep crustal
457 depths that might be the subducted oceanic crust (Hansen et al., 2012). Vp/Vs ratios in such a
458 layer are estimated to be as high as ~ 2, which can significantly contribute to elevated bulk
459 crustal Vp/Vs measurements.

460 The new Moho depth result also imparts some new insights. The observation of reduced crustal
461 thickness beneath the Basin and Range region suggests a diminished contribution of crustal
462 support to the topography through isostasy, indicative of greater dynamic support from the
463 underlying mantle. Additionally, a stronger contrast in crustal thickness between Basin and
464 Range and adjacent tectonic provinces such as Colorado Plateau also predicts greater
465 Gravitational Potential Energy (GPE) differences (e.g., Bahadori et al., 2022), which leads to a
466 different GPE-induced stress field.

467 Another improvement from the new approach is the uppermost mantle Vs. Uppermost mantle Vs
468 can be used to infer the temperature and possible distribution of partial melting (e.g., Hansen et
469 al., 2015; Porter & Reid, 2021). However, the depth-velocity trade-off of surface waves often
470 leads to the correlation between uppermost mantle Vs and Moho depth, as demonstrated by the
471 synthetic test in Section 2 (Fig 10a). Due to this significant trade-off, few studies utilize the
472 topmost mantle Vs for mapping the Moho temperature. Instead, much research on mantle
473 temperature focuses on a greater depth, where it is believed that the influence of crustal thickness
474 uncertainties is relatively small (e.g., below 50 km in Rau & Forsyth, 2011). In studies related to
475 Moho temperature, Pn velocity is often utilized (e.g., Boyd, 2020; Schutt et al., 2018). However,
476 with the incorporation of H-κ stacked energy, the accepted model ensemble results in a greatly
477 reduced trade-off between Moho depth and uppermost mantle Vs, and consequently, a better-
478 constrained uppermost mantle Vs (Fig. 10a). In this synthetic test, the accepted models obtained
479 through the new approach exhibit a 67% reduction in uppermost mantle Vs uncertainty (0.03
480 km/s) compared to the case without incorporating H-κ stacked energy (0.09 km/s, Fig. 10a). As a
481 result, application of the new method to NW US yields an improved uppermost mantle image.
482 As depicted in Fig.10b, the new model exhibits relatively faster Vs beneath the Columbia River
483 Flood Basalt, northern Rocky Mountains, Wyoming Craton, and part of the Basin and Range.
484 Slower uppermost mantle Vs is seen near the High Lava Plain, northeast of Basin and Range, the
485 Yellowstone hotspot track, Modoc Plateau, and the Cascadia region. Compared to the SR2016
486 model (Fig. 10c), the new result shows a generally slower uppermost mantle Vs in the
487 northwestern US, except in certain regions such as the northern Cascades, northern Sierra
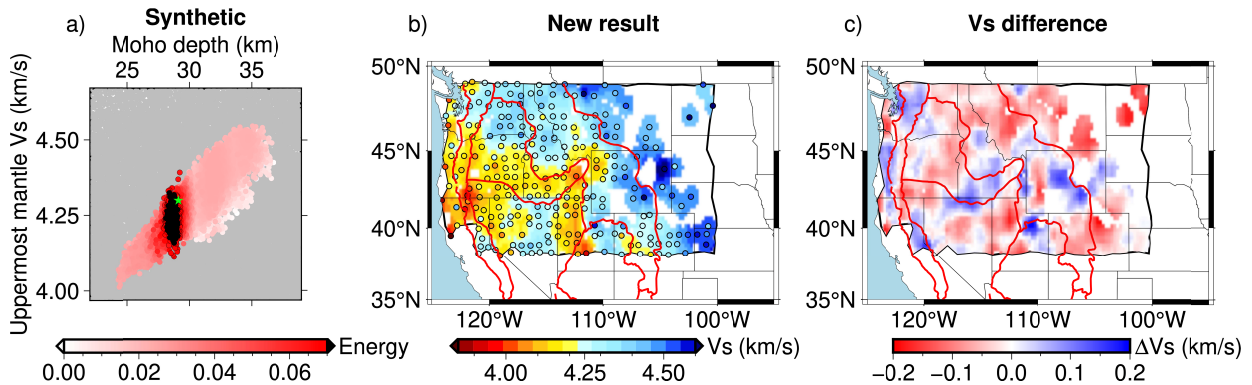488 Nevada, southern Modoc Plateau, Wyoming Craton, and the northern margin of the Colorado
489 Plateau.

490

491   **Figure 10.** Improvements in uppermost mantle structures. **a**) Trade-off between Moho depth and
492   uppermost mantle Vs (averaged Vs within 5 km below Moho), similar to Fig. 1a; **b**) Map view of
493   uppermost mantle Vs of our new result; **c**) Map view of the differences (new result - SR2016)
494   between our newly obtained uppermost mantle Vs and that of the SR2016 model.

495   Given that the trade-off between topmost mantle Vs and Moho depth has been reduced, the more
496   accurate Vs has the potential to be used to constrain the Moho temperature, and the usage of Vs
497   to constrain uppermost mantle temperature is no longer limited to depths much greater than
498   Moho. In the new map, the overall variation is consistent with the Pn-derived Moho temperature
499   map (Schutt et al., 2018) where the low Vs is found in regions with Moho temperature > 800 °C
500   (e.g., Yellow stone hotspot track and Cascadia). In some places, discrepancies appear, e.g., the
501   Wasatch Fault zone in central-West Utah, where the uppermost mantle Vs is low, but the Pn-
502   derived Moho temperature is not high. However, the low Vs is consistent with the high
503   geothermal heat flux in this area (Blackwell et al., 2011), indicating that the new Vs map
504   provides a useful constraint to build future Moho temperature models.

505   **4.4 Caveats of the work and potential refinements**

506   The extraction of RFs was performed using the traditional time-domain iterative method, as
507   described in section 3, without further processing. Also, the following quality control only
508   removes some low-quality data but cannot solve the asymmetric problem caused by the
509   interference of sediment-reverberations. One possible solution is to use higher-frequency RFs to
510   separate the Moho-converted phases and sediment-reverberations since the low-velocity
511   sedimentary layer can result in low-frequency reverberations. A more direct solution is to find a
512   way of removing the sediment-reverberations from the RFs. Yu et al. (2015) proposed an
513   approach to effectively remove the sediment reverberations and decipher the Moho-converted
514   phases. If this approach can be applied to the RFs that we used in MC inversion, the asymmetric
515   problem may be solved.

516   In this work, only the crystalline crust Vp/Vs is set as a free parameter, and the Vp/Vs ratio in
517   the sedimentary layer is simply scaled from the Vs ratio (Brocher, 2005). One possible future
518   improvement of the method is to perform the sedimentary-layer phases and reverberations in a
519   sequential H-k stacking (e.g., Yeck et al., 2013) and include it in the joint MC inversion.
520   Additionally, for the crystalline crust, only the bulk average Vp/Vs is resolved by the data, and it
521   lacks depth sensitivity for investigating the deep crustal structure. The lower crust has been the
522   center of the debate on the composition and evolution of the continental crust in general (e.g.,
523   Hacker et al., 2015b). To better understand its Vp/Vs ratio, it is thus important to incorporate
524   additional constraints. Lin et al., (2012) and others have made observations of the Rayleigh wave
525   local amplification and show that it provides additional sensitivity to the Vp and density that is
526   different from the phase and group velocities or H/V ratios. If such data can be incorporated in
527   the joint Monte Carlo inversion, additional sensitivity to the particular depth of the crust and
528   possible resolution to the deep crustal structure (e.g., Vp/Vs or density) can be obtained.

529   **4.5 Summary**

530   In this paper, we present a novel method that incorporates the traditional H-κ stacking into the
531   MC inversion of surface waves and receiver function waveforms to constrain the architecture of
532   crust and uppermost mantle seismic structure. The feasibility of the new method is demonstrated
533   by synthetic tests and further enhanced by the additional application to the USArray data in NW.
534   US. We summarize our findings below:

535   1. The new approach greatly reduces the trade-offs between lowermost crust Vs, Moho
536   depth, and bulk Vp/Vs ratio of the crystalline crust, eliminating the requirement of
537   assuming crustal Vp/Vs in joint inversions and resulting in more accurate results.
538   2. In addition to crustal structures, the new approach also enhances the accuracy of upper
539   mantle velocity structure by reducing the trade-off between Moho and upper mantle Vs.
540   3. Certain reverberations caused by thin sedimentary layers can contaminate the Moho-
541   converted phases by introducing an apparent shift, leading to a mismatch between the
542   maximum energy and the true arrival time. In such cases, the results may introduce bias,
543   primarily affecting the estimation of Vs and Moho depth.
544   4. When the sedimentary layer is thick enough, some reverberations generated by this
545   sedimentary layer are sufficiently separated from the Moho-converted phases to the
546   extent that there is no energy shift, but the Moho-converted phases are still affected to the
547   point of asymmetry. As a result, there exists a small bias in the obtained result, but much
548   lower than that caused by the apparent maximum energy shift due to sediment
549   contamination.
550   5. After applying the new method to ~ 450 USArray stations in NW US, map views of the
551   key crustal parameters (i.e., lowermost crust Vs, Moho depth, and bulk Vp/Vs of
552   crystalline crust) show general consistency with some previous studies but also reveals
553   additional new features.
554   6. The noticeable high Vp/Vs ratios in the crystalline crust of coastal Oregon suggest the
555   possible presence of mafic composition or the existence of fluid or cracks.
556   7. The new Moho depth result suggests reduced crustal support in the Basin and Range
557   region, with greater dynamic mantle support and significant Gravitational Potential
558   Energy differences compared to adjacent tectonic provinces.
559   8. The uppermost mantle Vs (averaged within 5 km below the Moho) map exhibits good
560   consistency with the Moho temperature map derived from Pn velocity, providing new
561   potential for using Vs to constrain the Moho temperature and crustal thermal properties.

562   Looking forward, through improved data processing techniques (e.g., removing sediment-related
563   reverberations), the issue of the maximum energy shift present in this new approach may be
564   resolved. Moreover, by incorporating other observables (e.g., local amplification data), the depth
565   resolution for Vp/Vs can be further enhanced, thereby obtaining more accurate deep crustal
566   structures. More accurate seismic structures, in turn, can offer valuable implications in other

567 areas of Earth science. These potential improvements warrant future investigations after the
568 initial effort summarized in this paper.

Acknowledgments

Open Research

581 The seismic data (including raw data for both surface wave observables and receiver

582 functions) are downloaded from Incorporated Research Institutions for Seismology

583 (IRIS, http://ds.iris.edu/ds/nodes/dmc/data/). The Vp/Vs ratios of Earthscope Automated

584 Receiver Survey (EARS) are downloaded from IRIS

585 (http://ds.iris.edu/ds/products/ears/#TOOLS) The three key parameters of each station

586 in our study can be found in the supplemental material. The seismic model is scheduled

587 to be available to the public at Earthscope Earth Model Collaborations

588 (https://ds.iris.edu/ds/products/emc-earthmodels/) after the manuscript is published.

589

590

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