

# Clouds and radiatively induced circulations

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In the atmosphere, there is an intimate relationship between clouds, atmospheric radiative cooling/heating, and radiatively induced circulations at various temporal and spatial scales. This coupling remains not well understood, which contributes to limiting our ability to model and predict clouds and climate accurately.

Cloud liquid and ice particles interact with both shortwave (SW) and longwave (LW) radiation, leading to cloud radiative effect (CRE). The CRE includes perturbations of the radiative fluxes at the top of the atmosphere (TOA) and the surface, as well as perturbations of the radiative cooling profile within the atmosphere. The effect of clouds that results in atmospheric radiative heating or cooling that is distinct from the clear-sky radiative cooling profile will be termed the CRE on atmospheric heating, or CRE-AH. The CRE-AH can significantly modify the horizontal and vertical gradients of the diabatic heating profile, inducing circulations at various scales in the atmosphere. In turn, circulations govern cloud formation and evolution processes and therefore the properties and distribution of clouds.

This chapter explores advances in research of the coupling between clouds and radiatively induced circulations and identify the paths forward. The chapter is organized into three sections. Section 1 discusses the relationship between clouds and tropospheric diabatic circulations in which condensate and precipitation are produced. Section 2 focuses on low clouds and shallow radiatively induced circulations in the boundary layer and lower free troposphere. Section 3 focuses on tropical high clouds and the circulations induced by the CRE-AH in these clouds. All the radiatively induced circulations discussed in the three sections are illustrated in Fig. 1.

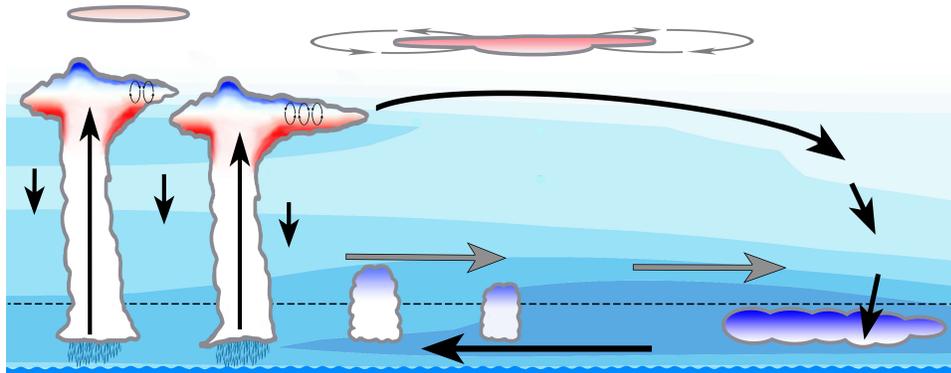


Figure 1: Illustration of the radiatively induced circulations discussed in this chapter, including tropospheric diabatic circulations (thick, black arrows, see Section 1), large-scale shallow circulations (thick, black arrows in the boundary layer and thick, grey arrows in the lower free troposphere, see Section 2), mesoscale circulations of tropical high clouds (thin, grey arrows, see Section 3), and small-scale convective motions within the anvils (thin, black arrows, see Section 3). The thin, dashed line marks the top of the boundary layer, which is located at altitudes of about 1–2 km. The background shading represents the clear-sky radiative cooling. The shading within the clouds indicates the CRE-AH. Blue indicates radiative cooling and red indicates radiative heating.

## 33 1 Clouds and tropospheric diabatic circulations

34 The relationship between clouds and tropospheric diabatic circulations is  
35 two-way. On the one hand, clouds are formed in the atmosphere as wa-  
36 ter vapor condenses within the moist, convective branch of these diabatic  
37 circulations. On the other hand, the perturbation in the diabatic heating  
38 profile due to the CRE-AH can feed back on to weaken or strengthen the  
39 circulations in which clouds form and evolve. In this section, we will review  
40 progresses in our understanding of this coupling, particularly in the context  
41 of the tropospheric diabatic circulations that underlie the atmospheric water  
42 cycle.

43 Following directly from the fact that cloud condensates are produced  
44 within the atmospheric water cycle, understanding of cloud behaviors may  
45 be obtained by studying the atmospheric water cycle. As a metric of the  
46 strength of the atmospheric water cycle, let us use the rate of condensation  
47 of water vapor in the atmosphere, i.e. the rate (in  $\text{kg kg}^{-1} \text{s}^{-1}$ ) at which  
48 water vapor is transformed into condensate at a given location in the atmo-  
49 sphere. The condensation rate by itself does not dictate the percentage of  
50 condensates that remain in the atmosphere as clouds rather than falling to  
51 the surface as precipitation. But, if we assume that the percentage of cloud  
52 condensates (out of the total condensates) does not change under small per-  
53 turbations of the climate, we will be able to obtain a first-order constraint  
54 on clouds based on the constraint on the condensation rate.

55 To formulate a constraint on the condensation rate—hereafter denoted  
56 by  $m_{\text{cond}}$ , we consider the moisture budget in the atmosphere following  
57 Schneider et al. (2010). In the free troposphere, a balanced water vapor  
58 budget in steady state is maintained between condensation and vertical ad-  
59 vection of water vapor, i.e.

$$[m_{\text{cond}}] = -[\omega \partial_p q], \quad (1)$$

60 where  $\omega$  is the pressure velocity,  $p$  is pressure, and  $q$  is the specific humidity.  
61 The notation  $[\cdot]$  indicates that the variable between the brackets is averaged  
62 horizontally over a sufficiently large domain for which horizontal advection  
63 of water vapor into/out of the domain can be neglected. The entire globe  
64 and the tropics are examples of such a domain. Equation (1) however applies  
65 only to the free troposphere; in the boundary layer, the source of moisture  
66 that results from surface evaporation must be considered. Below, we will  
67 first focus on the free troposphere and then touch upon the complications  
68 of the boundary layer toward the end of the section.

69 In a moist convecting atmosphere, vertical advection of water vapor is  
70 upward and mostly carried out by moist convection. The updrafts inside  
71 moist convective regions are saturated with water vapor above the lifted  
72 condensation level (LCL). Thus,

$$[m_{\text{cond}}] \sim -[\omega_{\uparrow} \partial_p q_{\text{sat}}]_{\text{conv}} \sim -[\omega_{\uparrow}]_{\text{conv}} [\partial_p q_{\text{sat}}]_{\text{conv}} \quad (2)$$

73 above the LCL (c.f. Eq. 5 in Schneider et al., 2010). Here  $q_{\text{sat}}$  is the satura-  
74 tion specific humidity,  $\omega_{\uparrow}$  is the upward component of the pressure velocity,  
75 and  $[\cdot]_{\text{conv}}$  indicates that the variable between the square brackets is averaged  
76 over moist convective regions within the domain only.

77 Over this domain, an overturning diabatic circulation can be constructed  
78 as consisting of a moist ascending branch in which latent heat is released  
79 as water vapor condenses forming condensates and precipitation (see the  
80 upward arrows in the deep convective clouds in Fig. 1) and a dry descending  
81 branch regulated by radiative cooling (see the downward arrows in clear air  
82 in Fig. 1). A nice illustration of such an overturning diabatic circulation  
83 is Fig. 10.3 in Wallace and Hobbs (2006). Following Yano et al. (2002),  
84 Zelinka and Hartmann (2010), Bony et al. (2016), Dinh and Fueglistaler  
85 (2017, 2019), we seek to estimate the convective mass flux  $[\omega_{\uparrow}]_{\text{conv}}$  as

$$[\omega_{\uparrow}]_{\text{conv}} \sim -[\omega_{\text{rad}}], \quad (3)$$

86 where

$$[\omega_{\text{rad}}] \sim \frac{[Q_{\text{rad}}]}{[\sigma]} \quad (4)$$

87 is the radiative subsidence mass flux,  $Q_{\text{rad}}$  is the radiative cooling rate,  
88  $\sigma$  is the static stability, and  $T$  is atmospheric temperature. Furthermore,  
89 by assuming that the saturation specific humidity within moist convective  
90 regions scales with the domain average profile ( $[\partial_p q_{\text{sat}}]_{\text{conv}} \sim [\partial_p q_{\text{sat}}]$ ), we  
91 obtain

$$[m_{\text{cond}}] \sim \frac{[\partial_p q_{\text{sat}}]}{[\sigma]} [Q_{\text{rad}}]. \quad (5)$$

92 Equation (5) indicates that the condensation rate depends on the radiative  
93 cooling rate as well as the factor

$$[f] = \frac{[\partial_p q_{\text{sat}}]}{[\sigma]}, \quad (6)$$

94 which is a function of atmospheric temperature. The atmospheric water  
95 cycle can be considered as driven by atmospheric radiative cooling, but

96 processes that affect the vertical profile of temperature can affect the con-  
97 densation rate and potentially clouds as well.

98 The linkage between tropospheric diabatic circulations and clouds as out-  
99 lined above has been used to explain how clouds would change following an  
100 increase in atmospheric CO<sub>2</sub> concentration and subsequent global warming.  
101 The responses of the water cycle and clouds to the radiative forcing from  
102 CO<sub>2</sub> increase consist of two components (Dinh and Fueglistaler, 2017): (i)  
103 rapid adjustment (Gregory et al., 2004) which occurs in the atmosphere in-  
104 dependently of surface temperature changes and (ii) a slower response that  
105 follows surface warming. Climate models consistently predict that global  
106 precipitation and cloud water decrease during rapid atmospheric adjust-  
107 ment (see Dinh and Fueglistaler, 2019 and references therein). Dinh and  
108 Fueglistaler (2019) explained that the weakening of the atmospheric water  
109 cycle and decrease in cloud water are driven by the decrease in atmospheric  
110 radiative cooling, a direct result of the CO<sub>2</sub> increase. Atmospheric radiative  
111 cooling decreases because the added CO<sub>2</sub> enhances the total atmospheric  
112 absorption of the LW radiation emitted by the surface. On the other hand,  
113 the slow response following surface warming shows increases in tropical rain  
114 rate and high cloud water content (Larson and Hartmann, 2003). These  
115 changes under warming are driven by an increase in atmospheric radiative  
116 cooling, which is largely associated with increased water vapor and increased  
117 emission of LW radiation by water vapor at higher atmospheric tempera-  
118 tures. Further research is needed to confirm whether the increase in cloud  
119 water holds globally and to investigate the differences in the responses of  
120 tropical and extra-tropical clouds to warming.

121 The radiative cooling constraint on tropospheric diabatic circulations  
122 has been shown useful in evaluating the radiative climate feedback of tropi-  
123 cal high clouds. Given that the convective mass flux is constrained by  
124 the radiative cooling ( $[Q_{\text{rad}}]$ ) following Eqs. (3) and (4), it can be expected  
125 that tropical convection and convective anvil clouds detrain near the level  
126 in the upper troposphere where  $[Q_{\text{rad}}]$  decreases rapidly with height. For  
127 the Earth’s atmosphere,  $[Q_{\text{rad}}]$  is governed to a large extent by water vapor,  
128 whose vertical profile and radiative effect depend strongly on atmospheric  
129 temperature. Hartmann and Larson (2002) therefore proposed that the at-  
130 mospheric temperature at which the LW radiative emission and atmospheric  
131 radiative cooling by water vapor become inefficient remains the same regard-  
132 less of surface temperature. It follows that the temperature at the detrain-  
133 ment level and therefore the emission temperature of tropical anvil clouds  
134 remain constant as the surface warms; the clouds absorb more upwelling LW  
135 radiation from a warming surface and atmosphere below but emit the same

136 amount of LW radiation. This “fixed anvil temperature” (FAT) hypothesis  
137 therefore implies a positive climate feedback of tropical anvil clouds.

138 The original FAT hypothesis does not account for the increased static  
139 stability ( $[\sigma]$ ) at the level where  $[Q_{\text{rad}}]$  decreases rapidly with height. In a  
140 follow-up work, Zelinka and Hartmann (2010) calculated the convergence  
141 profile of tropical tropospheric diabatic circulations from the vertical gra-  
142 dient of  $[\omega_{\text{rad}}]$  using the clear-sky  $[Q_{\text{rad}}]$  profile (see Eq. 4). They found  
143 that the peak of the convergence profile shifts upward as the surface warms,  
144 consistently with the upward shift of the clear-sky  $[Q_{\text{rad}}]$ . However, the  
145 peak convergence level warms slightly and correspondingly the anvil cloud  
146 temperature increases slightly as the static stability at this level increases.  
147 These findings confirm that the climate feedback of tropical anvil clouds is  
148 positive but of a smaller magnitude than that suggested by the original FAT  
149 hypothesis.

150 Using the same argument, Bony et al. (2016) proposed that tropical anvil  
151 cloud cover is expected to shrink under warming. As the climate warms, the  
152 anvil clouds rise to remain at approximately the same temperature follow-  
153 ing the FAT hypothesis. As the clouds rise they are embedded in a more  
154 stable atmosphere. The increased stability decreases the radiatively driven  
155 mass flux (see Eq. 4) and the convective outflow, leading to a reduction of  
156 the anvil cloud fraction. This stability effect has been confirmed based on  
157 interannual variations of anvil cloud fraction (Saint-Lu et al., 2020) in data  
158 from the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations  
159 (CALIPSO).

160 The original FAT hypothesis was developed for the tropics only, but the  
161 same general behavior of atmospheric radiative cooling, which is dominated  
162 by water vapor, also holds in the extra-tropics (Thompson et al., 2017). The  
163 pressure level in the upper troposphere at which the clear-sky atmospheric  
164 radiative cooling profile decreases rapidly with height thus defines the top  
165 of the troposphere and cloud-top temperature throughout the globe. This  
166 is a strong constraint that can be used to infer cloud top height and how it  
167 changes under warming.

168 Much of the discussions above have focused on the aspect of the  
169 circulation–cloud coupling which concerns how the atmospheric water cy-  
170 cle governs large-scale cloudiness. Let us now address the second aspect of  
171 this coupling which concerns how the CRE-AH—through its impact on at-  
172 mospheric radiative cooling—feeds back on diabatic circulations. Referring  
173 again to Eq. (5), we see that the CRE-AH can affect the condensation rate  
174 and therefore precipitation either by directly modifying the radiative cool-  
175 ing profile or by indirectly modifying the temperature profile through the

176 radiative cooling perturbation. The temperature profile governs both the  
177 vertical gradient of the saturation specific humidity and the static stability  
178 in the atmosphere, which are the numerator and denominator of the factor  
179  $[f]$  defined in Eq. (6).

180 A number of studies using numerical simulations have shown that the  
181 CRE-AH plays an important role in determining the mean tropical circula-  
182 tion (Slingo and Slingo, 1988, 1991, Bergman and Hendon, 2000, Tian and  
183 Ramanathan, 2003) as well as the general circulation of the atmosphere and  
184 global precipitation (Randall et al., 1989, Li et al., 2015). Averaged over  
185 the tropics and/or globally, the CRE-AH produces radiative heating in the  
186 free troposphere, correspondingly a reduction in the all-sky radiative cool-  
187 ing rate (see e.g. Fig. 4 in Li et al., 2015). If this were the only effect of  
188 the CRE-AH, we would expect that precipitation decreases—particularly in  
189 the tropics where the reduction in the radiative cooling rate by the CRE-  
190 AH is largest. However, in all of the aforementioned studies but Li et al.  
191 (2015), it was found on the contrary that the CRE-AH enhances precipi-  
192 tation. Randall et al. (1989) found that the CRE-AH results in a warmer  
193 and deeper troposphere. When integrated over a warmer and deeper tropo-  
194 sphere, the  $[\partial_p q_{\text{sat}}]$  term in Eq. (5) increases significantly. An enhancement  
195 in precipitation thus occurs despite reduced radiative cooling.

196 Given that the role of the CRE-AH on diabatic circulations remains  
197 inconclusive, it would be worthwhile to re-examine this topic in future stud-  
198 ies. For future analysis, the impact of the CRE-AH on precipitation can be  
199 evaluated more accurately by accounting for all of the three terms  $[Q_{\text{rad}}]$ ,  
200  $[\partial_p q_{\text{sat}}]$ , and  $[\sigma]$  in Eq. (5). Above we have touched upon the impacts of  
201 the CRE-AH on  $[Q_{\text{rad}}]$  and  $[\partial_p q_{\text{sat}}]$ , but the CRE-AH also affects  $[\sigma]$ —both  
202 locally by modifying the vertical profile of temperature in cloudy air and  
203 remotely by modifying the meridional temperature gradient. As shown in  
204 Li et al. (2015), the difference in the CRE-AH between the tropics and the  
205 extra-tropics leads to a meridional temperature gradient that affects the  
206 meridional transport of energy by the eddies. The transport of energy by  
207 the eddies in turn affects the static stability in the extra-tropics.

208 The discussions so far have been limited to clouds in the free tropo-  
209 sphere above the boundary layer. Strictly speaking, the scaling argument  
210 used previously for the free troposphere (see Eqs. 1–6) does not apply to the  
211 boundary layer because (i) the source of moisture that results from surface  
212 evaporation must be added to the moisture budget balance in Eq. (1) for the  
213 boundary layer and (ii) the updrafts in the boundary layer below the LCL  
214 are not saturated. Nevertheless, in the upper boundary layer, the impact of  
215 clouds on large-scale diabatic circulations can be qualitatively understood

216 from the radiative cooling constraint. In the upper boundary layer (around  
217 750–850 hPa), the CRE-AH is dominated by the LW emission by cloud  
218 hydrometeors, leading to enhanced radiative cooling there (Haynes et al.,  
219 2013). This effect is apparent in the prevalent marine stratocumulus in the  
220 subtropics and higher latitudes (Wood, 2012). The CRE-AH of boundary  
221 layer clouds thus strengthens the overturning diabatic circulations, resulting  
222 in an increase in the globally averaged precipitation (Fermepin and Bony,  
223 2014). For other issues regarding the coupling between radiatively induced  
224 circulations and low clouds, the readers are referred to Section 2 below.

225 In summary, notable progress in our understanding of the coupling be-  
226 tween circulations and clouds has been made in the last few decades. In  
227 particular, constraints on how clouds change under climate change have  
228 been obtained based on basic understanding of tropospheric diabatic cir-  
229 culations. These constraints on cloud properties (vertical and horizontal  
230 distributions, water content, and coverage) will enable improved, accurate  
231 evaluation of the impacts of the CRE on the Earth’s energy budget and the  
232 climate feedback of clouds on global warming. However, existing studies  
233 have not settled on the roles of the CRE-AH on circulations and precipi-  
234 tation. This leaves significant opportunities for future studies. Progress is  
235 anticipated to occur rapidly within the next decade given the advancement  
236 in model development and increasing availability of global and long-term  
237 observational data of clouds (such as CALIPSO).

## 238 **2 Low clouds and shallow circulations**

239 Shallow circulations are characterized by a convergence/divergence in the  
240 boundary layer and a compensating flow in the lower free troposphere. The  
241 ascending branch of these circulations is generally located in the warm,  
242 convective regions and the descending branch in the cooler, less convective  
243 regions because of the pressure gradients created by the temperature anom-  
244 lies. Boundary layer convergence occurs in the warm, convective regions and  
245 divergence in the cool, non-convective regions (see the horizontal black arrow  
246 near the bottom of Fig. 1), with opposite patterns just above the boundary  
247 layer (see the horizontal grey arrows in Fig. 1). Shallow circulations appear  
248 in numerical model simulations at both mesoscale and large scales and have  
249 been observed in the tropics at large scales. In this section, we will first  
250 explain the mechanism that gives rise to such circulations. Second, we will  
251 review how these circulations influence the spatial organization of convec-  
252 tion. Lastly, we will review the instances of observed shallow circulations

253 and their influence on the large-scale tropical climatology.

## 254 **2.1 Mechanism of shallow circulations**

255 In non-convective regions, the boundary layer experiences radiative cooling  
256 at its top, mostly through LW radiation. This cooling results from both low  
257 clouds and clear-sky processes. Indeed, the boundary layer is significantly  
258 moister, and therefore absorbs and re-emits more LW radiation than the  
259 free troposphere above. A large part of the LW radiation emitted upward  
260 at the top of the boundary layer is not absorbed by the free troposphere  
261 and hence escapes to space, allowing the boundary layer top to cool. Cloud  
262 hydrometeors also absorb and emit infrared radiation very efficiently, so low  
263 clouds experience strong radiative cooling at their tops as well. This cooling  
264 is particularly intense in the case of stratocumulus clouds (Wood, 2012,  
265 Bellon and Geoffroy, 2016, Bellon and Bony, 2020). Mixing by turbulence  
266 redistributes the cooling from the top of the boundary layer downward.  
267 Vertical turbulent mixing is very efficient in a well-mixed boundary layer  
268 but a little less so in a shallow convective boundary layer.

269 The radiative cooling in the boundary layer can give rise to shallow  
270 circulations. In the hydrostatic approximation,

$$\frac{\partial\Phi}{\partial p} = -\frac{1}{\rho} \approx -\frac{R_a T}{p} \quad (7)$$

271 with  $\Phi$  the geopotential,  $\rho$  the density,  $T$  the temperature,  $p$  the pressure,  
272 and  $R_a$  the specific gas constant of air. This means that the vertical increase  
273 of the geopotential through the boundary layer is smaller in radiatively  
274 cooled regions than in others. The baroclinic component of this pattern  
275 corresponds to the geopotential near the surface being larger in radiatively  
276 cooled regions than in others, and the geopotential at the top of the bound-  
277 ary layer being smaller in these cooled regions than in others. The associated  
278 geopotential gradient forces a circulation that includes outflow of air from  
279 the cooled regions in the boundary layer and inflow of air toward the cooled  
280 regions just above the boundary layer. This mechanism has been illustrated  
281 and validated by Large Eddy Simulation experiments and conceptual models  
282 (Naumann et al., 2017, 2019).

## 283 **2.2 Shallow circulations and aggregation of convection**

284 Shallow circulations differ from troposphere-deep circulations particularly in  
285 terms of the transport of moist static energy (MSE)  $h = c_p T + \Phi + L_v q$ , with

286  $c_p$  the specific heat capacity of air at constant pressure,  $L_v$  the latent heat  
287 of vaporization, and  $q$  the specific humidity. Shallow circulations transport  
288 MSE up-gradient and therefore increase the contrast in MSE between the  
289 convective and dry regions, while deep circulations transport MSE down-  
290 gradient and reduce such contrast.

291 The difference in the direction of transport of MSE between troposphere-  
292 deep circulations and shallow circulations results from the stratification of  
293 MSE in the atmosphere:  $h$  is large in the boundary layer where the humidity  
294 is high, minimum in the lower free troposphere where the humidity is low,  
295 and monotonically increases with altitude in the free troposphere because of  
296 the contribution from the geopotential; at the tropopause it reaches values  
297 similar to the surface values (see Fig. 4 in Glenn and Krueger, 2017). The  
298 vertical integral of  $h$  over the middle and upper troposphere is larger than  
299 the vertical integral of  $h$  over the boundary layer. Therefore, the upper  
300 branches of troposphere-deep circulations transport more MSE (from the  
301 ascending regions into the subsiding regions) than their lower branches in the  
302 boundary layer (from the subsiding regions into the ascending regions). The  
303 net effect is that troposphere-deep circulations export MSE from ascending,  
304 convective regions of large column-integrated MSE to dry, subsiding regions  
305 with small column-integrated MSE. In contrast, shallow circulations import  
306 MSE from their subsiding branches (where column-integrated MSE is small)  
307 into their ascending branches (where column-integrated MSE is large).

308 Because shallow circulations increase the horizontal gradient of MSE,  
309 they create a positive feedback on the spatial variability: anomalies in MSE  
310 are reinforced by the transport associated with these circulations. As a re-  
311 sult, shallow circulations can be powerful actors in the spatial organization  
312 of convection: warm, convective regions become warmer and moister while  
313 dry, cool regions become cooler and drier. This mechanism of spatial or-  
314 ganization of convection, named “self-aggregation” is documented both in  
315 convection-permitting simulations and in general circulation model (GCM)  
316 simulations even without any external circulation nor the effect of rota-  
317 tion. In particular, low-level radiative cooling can cause the development  
318 of cooler and drier regions, sometimes called “radiative cold pools” that are  
319 instrumental to the development of self-aggregation. Figures 2 and 3 show  
320 examples of such radiative cold pools in a convection-permitting model and  
321 a GCM.

322 Figure 2 shows results of an idealized simulation (see Bellon and Coppin,  
323 2021) using the non-hydrostatic mesoscale model MesoNH (Lafore et al.,  
324 1998, Lac et al., 2018) in a convection-permitting configuration. The do-  
325 main is  $90\,000\text{ km}^2$  with a 3-km horizontal resolution and 48 vertical lev-

326 els. The configuration prescribes a fixed sea surface temperature of 301 K  
327 over the entire domain and a horizontally uniform large-scale subsidence  
328 ( $0.5 \text{ kg m}^{-2} \text{ s}^{-1}$  at 400 hPa). Figure 2 shows the average variables over one  
329 day of the stationary state reached in this simulation.

330 Figure 2(a) shows the horizontal distribution of precipitable water in the  
331 MesoNH simulation described above, with a clear dry patch surrounded by  
332 a fairly uniform moist region. Using the bimodality of the distribution of  
333 column-integrated MSE, a dry region and a moist region can objectively  
334 be identified and the dashed line in Fig. 2(a) shows the boundary between  
335 these regions. Figures 2(b) and (c) show the vertical profiles of the mixing  
336 ratios of water vapor and cloud condensates averaged over each of these  
337 regions. The figures show that the dry column is much drier than the moist  
338 column, both in the boundary layer and in the free troposphere, and with  
339 hardly any clouds. The moist region is convective, with large amount of  
340 cloud condensates throughout the troposphere.

341 Figure 2(d) shows the radiative heating rates (with negative values indi-  
342 cating radiative cooling) in the dry and moist regions. In the lower tropo-  
343 sphere, the LW radiative cooling is larger in the dry region because of the  
344 smaller greenhouse effect of water vapor and clouds in the free troposphere  
345 above. Conversely, in the upper troposphere, the LW radiative cooling is  
346 larger in the moist region because of the re-emission of terrestrial radiation  
347 by the large amount of water vapor and clouds there. Except in the bound-  
348 ary layer, the SW radiative heating is larger in the moist region where there  
349 is more absorption of solar radiation by water vapor and clouds. The differ-  
350 ence is opposite in the boundary layer because the downward solar radiative  
351 flux reaching the top of the boundary layer is larger in the dry region. In this  
352 simulation, the differences in the LW and SW effects compensate each other  
353 in the upper troposphere, but not in the lower troposphere where the net  
354 radiative cooling is larger (by about  $0.5 \text{ K d}^{-1}$ ) in the dry region than in the  
355 moist region. The radiative cooling of the dry region relative to the moist  
356 region creates a shallow circulation with winds diverging from the dry region  
357 near the surface and a return flow in the lower free troposphere. Consistently  
358 with the discussions above, the shallow circulation increases the contrast in  
359 MSE between the dry and moist columns (not shown). Note that in this  
360 particular simulation, the radiative effect is mostly a clear-sky effect. But in  
361 similar simulations, a strong CRE-AH due to low clouds has been identified,  
362 with a similar resulting shallow circulation (Muller and Held, 2012, Muller  
363 and Bony, 2015).

364 Figure 3 shows regional snapshots of 925-hPa wind vectors and tem-  
365 perature (left panel) and precipitable water (right panel) at day 151 of a

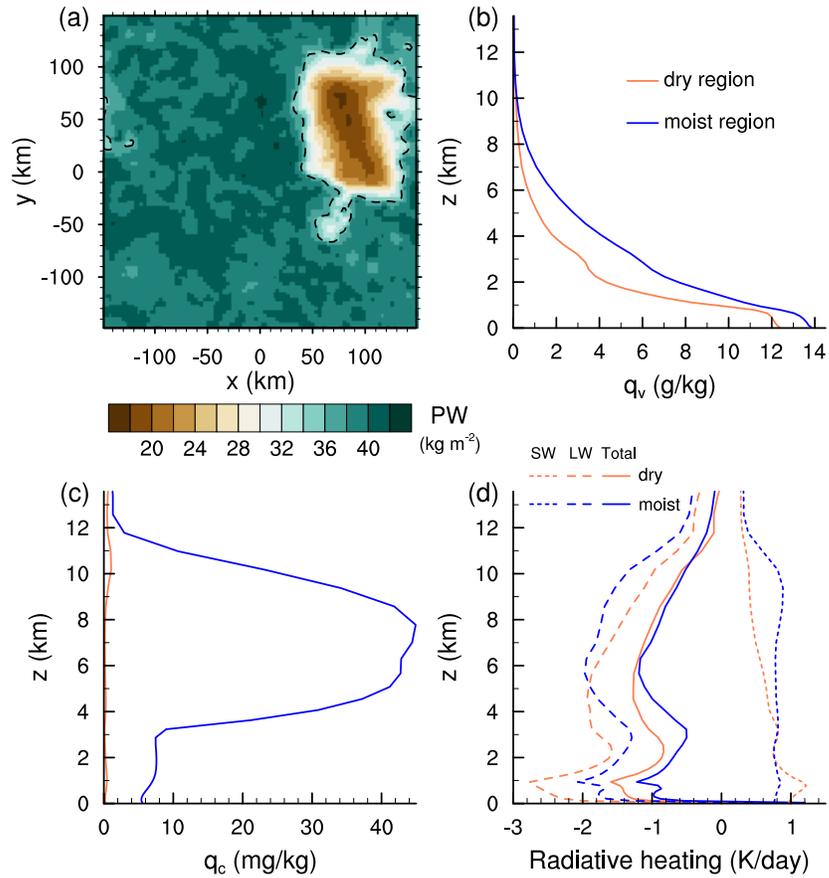


Figure 2: One-day average of a convection-permitting simulation: (a) map of precipitable water with a dashed contour showing the boundary between the moist and dry regions, (b) profile of water vapor mixing ratio, (c) profile of water condensate mixing ratio, and (d) profiles of solar (SW, dotted lines), terrestrial (LW, dashes lines) and net (total, solid lines) radiative heating rates. Blue lines refer to the moist region and red lines to the dry region.

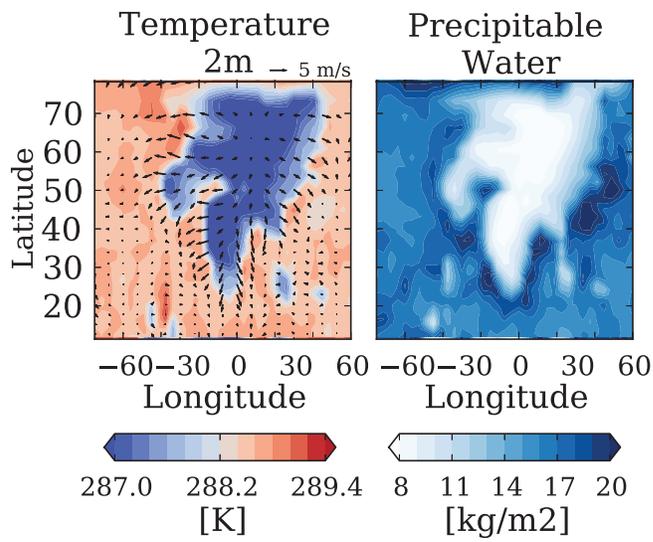


Figure 3: Radiative cold pool in a GCM simulation; left panel: temperature (shadings) and 925-hPa winds (vectors) at day 151 of the simulation; right panel: precipitable water. Adapted from Fig. 4 in Coppin and Bony (2015).

366 simulation using the GCM LMDz5A (Hourdin et al., 2006). The simulation  
367 was in a global radiative-convective-equilibrium configuration (i.e., with-  
368 out rotation and with a prescribed, uniform sea surface temperature) and  
369 initialized with horizontally uniform atmospheric conditions. In this case,  
370 the sea surface temperature is fairly low (292 K), and the spatial organiza-  
371 tion of convection results from mechanisms similar to those shown above  
372 in convection-permitting simulations. Details on the configuration and the  
373 mechanisms of self-aggregation at play in this simulation can be found in  
374 Coppin and Bony (2015). Figure 3 shows the development of a dry, cool  
375 region with near-surface winds diverging from that region. A return flow  
376 with converging winds occurs in the lower free troposphere (not shown).  
377 The expansion of this radiative cold pool eventually leads to circumscribing  
378 convection to a few limited regions of the globe.

379 As a final point, we note that while shallow circulations appear as a  
380 key mechanism of self-aggregation in a large number of model simulations,  
381 other mechanisms can also cause or contribute to self-aggregation (see Wing  
382 et al., 2017 for a review). Furthermore, while there are similarities between  
383 modeled self-aggregated convection and observed organized convection (see  
384 Holloway et al., 2017), it is still unclear whether the mechanisms producing  
385 self-aggregation in model simulations are active in the real world.

### 386 2.3 Observed shallow circulations

387 Observing systems have limited capacity to observe the three-dimensional  
388 atmospheric velocity fields and indirect estimates using diabatic heating  
389 are not robust for troposphere-deep signal, let alone shallow circulations  
390 (Bellon et al., 2017). As a result, mesoscale shallow circulations are yet to  
391 be observed.

392 At large scales, shallow meridional circulations (SMCs) have been iden-  
393 tified in the tropics around tropical convergence zones. The first of such  
394 observation was in the Intertropical Convergence Zone (ITCZ) of the east-  
395 ern Pacific (Zhang et al., 2004). Figure 4 shows this SMC in the boreal  
396 autumn there, with low-level flow convergence around the ITCZ, which is  
397 located at  $10^{\circ}$ – $15^{\circ}$ N in this season. The northerly cross-equatorial flow in  
398 the boundary layer converges in the ITCZ and is compensated by diverg-  
399 ing flows both in the lower free troposphere (at 2–6 km in Fig. 4) and in  
400 the troposphere above 6 km, forming both shallow and deep overturning cir-  
401 culations. Similar SMCs have been observed in the central Atlantic ocean  
402 (Zhang et al., 2008) and in the Caribbean (Schulz and Stevens, 2018).

403 These SMCs in the ITCZ were first thought to result from the cross-

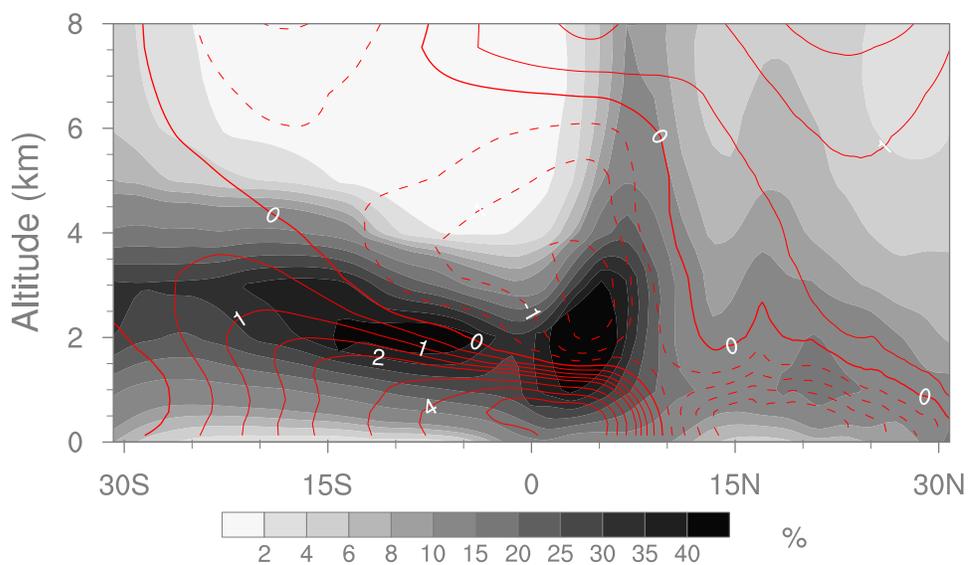


Figure 4: Cloud fraction (shadings, dataset GOCCP, Chepfer et al., 2010) and meridional wind (red contours, dataset ERA5, Hersbach et al., 2020) averaged over the eastern Pacific ( $90^{\circ}\text{W}$ – $120^{\circ}\text{W}$ ) in the boreal autumn (September–November).

404 equatorial sea surface temperature gradients that are communicated to the  
405 boundary layer air by turbulent fluxes and create pressure gradients that  
406 force the circulations (Nolan et al., 2007, 2010), but more recent work showed  
407 the role of the boundary-layer radiative cooling in the descending branch of  
408 the SMC. Figure 4 shows that the northerly flow in the non-convective region  
409 is co-located with the boundary layer clouds, which lends some credibility  
410 to a role of boundary-layer-top cooling, and particularly the CRE-AH. The  
411 SMC is also more intense if deep convection is momentarily suppressed and  
412 shallow convection is more active (Zhang et al., 2004, Yokoyama et al., 2014),  
413 potentially because the boundary-layer temperature follows more closely the  
414 sea surface temperature if deep convection is suppressed, but also because it  
415 changes the boundary-layer vertical structure and hence its radiative cooling.  
416 Additionally to the diabatic forcing, the momentum constraint allows the  
417 SMC to develop only if the ITCZ is away from the equator (Dixit and  
418 Srinivasan, 2017).

419 SMCs are also observed in monsoon regions such as West Africa, India,  
420 and Australia (Zhang et al., 2008, Zhai and Boos, 2017) with a rising branch  
421 over the monsoon heat low. These result from the pressure gradients between  
422 the equatorial ocean and the heat low over the continent (Zhang et al., 2008).

423 SMCs contribute to moistening the convergence zones, although to a  
424 lesser extent than troposphere-deep circulations. Recall from Section 2.2  
425 that SMCs and deep circulations transport MSE in opposite directions be-  
426 cause the vertical profile of MSE has a minimum in the lower free tropo-  
427 sphere. On the other hand, both types of circulations import moisture into  
428 the convergence zones as water vapor decreases monotonically with height  
429 in the atmosphere (see e.g. Fig. 2b). However, by exporting air in the lower  
430 free troposphere out of the ITCZ, the ITCZ SMCs import less moisture into  
431 the ITCZ than deep circulations (Zhang et al., 2008). Monsoon SMCs even  
432 include a drying contribution from horizontal advection of moisture, which  
433 further decreases the SMCs' moistening effect: as they extend to the heat  
434 low poleward of the convergence zones, they export moist air to that region  
435 in the boundary layer while importing very dry air into the ITCZ in the  
436 lower free troposphere (Zhai and Boos, 2017).

### 437 **3 Responses of tropical high clouds to the CRE-** 438 **AH**

439 This section describes the motions induced by the CRE-AH in tropical high  
440 clouds and the impacts of these motions on the evolution, lifetime, and

441 the CRE at the TOA of these clouds. The tropical high clouds that are  
 442 strongly influenced by the motions induced by their own CRE-AH include  
 443 (i) cirrus in the tropical tropopause layer (TTL); these clouds form either  
 444 by in-situ ice nucleation or from the remnants of anvil clouds, and (ii) anvil  
 445 clouds at various stages of evolution and optical properties, ranging from  
 446 very reflective fresh anvils with large ice water contents to optically thin  
 447 anvils that spread far away from deep convective cores.

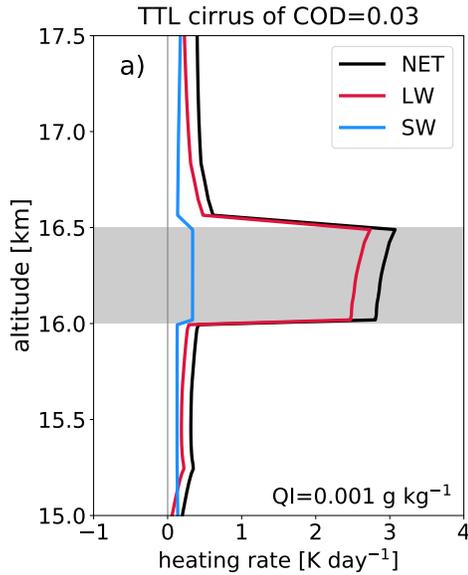


Figure 5: Radiative heating rates for a TTL cirrus assuming typical tropical temperature and moisture profiles. QI refers to ice mixing ratio. The ice crystal effective radius is set to values between  $10 \mu\text{m}$  at the cloud top and  $16 \mu\text{m}$  at the cloud base.

448 The radiative heating rates that result from the interaction of ice crystals  
 449 with radiation are shown in Figs. 5 and 6 for typical high cirrus clouds. The  
 450 TTL cirrus in Fig. 5 has a cloud optical depth (COD) of 0.03 and the anvil  
 451 cirrus in Fig. 6 have CODs of 50, 5, and 1. The radiative heating rates shown  
 452 in these figures were calculated using the Rapid Radiative Transfer Model  
 453 (RRTM, Mlawer et al., 1997, Iacono et al., 2008). The absorption of LW  
 454 radiation results in heating which maximizes either near the cloud top for  
 455 the TTL cirrus (Fig. 5) or near the cloud bases for the anvil clouds (Fig. 6).  
 456 For the thick anvil clouds that are opaque to LW radiation (Figs. 6a and b),

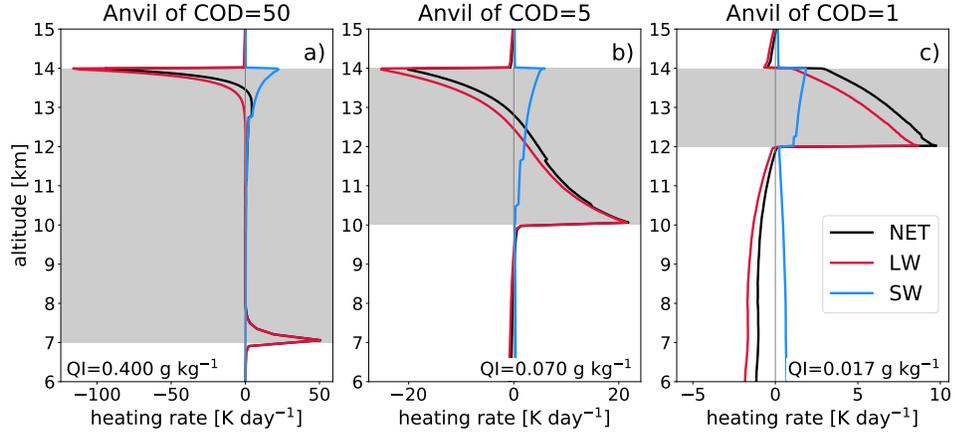


Figure 6: Radiative heating rates for (a) thick, (b) intermediately thick, and (c) thin anvil clouds assuming typical tropical temperature and moisture profiles. QI refers to ice mixing ratio. The ice crystal effective radius is set to values between  $40\ \mu\text{m}$  at the cloud top and  $70\ \mu\text{m}$  at the cloud base in case (a),  $30\ \mu\text{m}$  at the cloud top and  $60\ \mu\text{m}$  at the cloud base in case (b), and  $20\ \mu\text{m}$  at the cloud top and  $30\ \mu\text{m}$  at the cloud base in case (c), roughly in line with satellite observations of anvil clouds by Sokol and Hartmann (2020).

457 the large emissivities result in LW cooling near the cloud tops. For all the  
 458 clouds shown, the absorption of SW radiation results in heating (Figs. 5  
 459 and 6), but the magnitude of the SW heating is significantly smaller than  
 460 the LW heating and cooling.

461 The CRE-AH in both TTL cirrus and anvils can drive mesoscale circula-  
 462 tions (see Figs. 1 and 7a). The circulations consist of rising vertical motions  
 463 within the clouds (or portions of the clouds that are heated diabatically),  
 464 compensating sinking motions outside the clouds, horizontal outflows near  
 465 the cloud tops, and horizontal inflows near the cloud bases or below the lev-  
 466 els of maximum heating (Ackerman et al., 1988, Lilly, 1988, Durran et al.,  
 467 2009, Dinh et al., 2010, Gasparini et al., 2019). In addition, long exposure  
 468 to a strong CRE-AH can bend the isentropic surfaces, forming unstable,  
 469 convective layers within the high clouds (see Figs. 1 and 7b, and also Dobbie  
 470 and Jonas, 2001, Dinh et al., 2010, Schmidt and Garrett, 2013).

471 The magnitude and vertical profile of the CRE-AH and the correspond-  
 472 ing dynamical responses are highly sensitive to the COD. In the following,

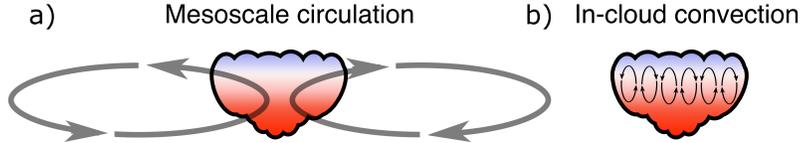


Figure 7: Air motions induced by the CRE-AH in tropical high clouds.

473 we therefore consider separately thin cirrus in the TTL (Section 3.1) and  
 474 anvil clouds which are much thicker (Section 3.2).

### 475 3.1 TTL cirrus

476 Thin cirrus are widespread in the TTL, with reported cloud fractions of  
 477 20–50 % (Massie et al., 2002, Tseng and Fu, 2017). Such clouds are nearly  
 478 transparent to the human eye, with CODs on the order of 0.01–0.05 (Dessler  
 479 and Yang, 2003, Haladay and Stephens, 2009, Lee et al., 2009). They heat  
 480 radiatively due to the absorption of LW radiation and to a minor extent SW  
 481 absorption, with typical heating rates of about  $5 \text{ K d}^{-1}$  or less (Fig. 5).

482 TTL cirrus modulate the amount of water vapor that enters the strato-  
 483 sphere and therefore the radiative effect of stratospheric water vapor on  
 484 climate (Dinh and Fueglistaler, 2014a). Furthermore, given that the clear-  
 485 sky radiative cooling diminishes near zero in the TTL, the CRE-AH of these  
 486 clouds plays a critical role in driving cross-isentropic transport of air from  
 487 the TTL into the stratosphere (Corti et al., 2006, Dinh and Fueglistaler,  
 488 2014b).

The mesoscale dynamical response to the radiative heating in TTL cirrus  
 can be qualitatively understood based on the simplified framework of a quasi-  
 hydrostatic, two-dimensional Boussinesq fluid, for which

$$\frac{\partial b}{\partial t} + N^2 w = Q_{\text{rad}}, \quad (8)$$

$$\frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0 \quad (9)$$

489 (Eqs. 3 and 4 in Durran et al., 2009). Here  $u$  and  $w$  are respectively the  
 490 horizontal and vertical velocities,  $b$  is the buoyancy,  $N$  is the Brunt–Väisälä

491 frequency, and  $Q_{\text{rad}}$  is the CRE-AH. As time goes on ( $t \rightarrow \infty$ ),

$$w \rightarrow w_{\text{ss}} = \frac{Q_{\text{rad}}}{N^2}. \quad (10)$$

492 The steady-state vertical velocity ( $w_{\text{ss}}$ ) is thus proportional to and has the  
493 same shape as the heating. Using Eq. (9) and  $w_{\text{ss}}$  in Eq. (10), the steady-  
494 state horizontal velocity can also be found. The steady-state horizontal  
495 velocity depends on the vertical gradient of the heating and extends laterally  
496 beyond the cloud/heating boundaries (Durrán et al., 2009).

497 Following Eqs. (8) and (10), rising motions are induced in the clouds  
498 where the air is heated radiatively. Outside the lateral edges of the clouds,  
499 the buoyancy anomalies result in compensating sinking motions (see Fig. 7a  
500 and Fig. 3 in Dinh et al., 2010). Mass conservation (Eq. 9) leads to horizontal  
501 inflows in the lower halves of the cloud layers and horizontal outflows in the  
502 upper halves of the cloud layers. The developed circulations narrow the  
503 cloud bases, expand the cloud tops, and lead to the spreading and lofting of  
504 the clouds (see Figs. 6 and 7 in Dinh et al., 2010).

505 The mesoscale circulations described above advect environmental air into  
506 the TTL cirrus (Dinh et al., 2010, 2012, 2014). Environmental air is brought  
507 into the clouds by the inflows in the lower halves of the clouds and then  
508 advected upward by the radiatively induced rising motions in the clouds.  
509 This leads to water vapor flux convergence (divergence) inside the clouds if  
510 the ambient air is moist (dry). Therefore, depending on whether the ambient  
511 air is supersaturated or subsaturated (with respect to ice), advection of air  
512 by the mesoscale circulations supports or suppresses depositional growth of  
513 cloud ice crystals, thereby lengthening or shortening the cloud lifetime (Dinh  
514 et al., 2010, 2012, 2014).

515 The vertical gradient of the radiative heating is negative near the tops  
516 of the TTL cirrus (at altitude of 16.5 km in Fig. 5). This can lead to the  
517 formation of shallow unstable layers at the cloud tops that support small-  
518 scale convective motions (see Figs. 4–6 in Dinh et al., 2010). As a result,  
519 the cloud tops become heterogeneous with pockets of updrafts with higher  
520 ice water contents and areas of downdrafts mixed with environmental air  
521 leading to ice sublimation.

522 The relevance of the mesoscale circulations induced by the CRE-AH for  
523 TTL cirrus evolution remains disputed. In-situ measurements show that  
524 ice crystal radii are typically larger than 5–10  $\mu\text{m}$  (Lawson et al., 2008,  
525 Krämer et al., 2020). Gravitational settling of large ice crystals may not  
526 allow sufficient time for the circulations to develop in response to the CRE-  
527 AH (Jensen et al., 2011). However, given that TTL cirrus can last for several

528 days (Winker and Trepte, 1998), it is more likely than not that these in-  
529 situ observations did not sample the cloud formation period (the first 12 h  
530 or so), during which the freshly nucleated ice crystals remain small in size.  
531 The presence of wind shear and gravity wave temperature fluctuations (Dinh  
532 et al., 2016) were also shown to lead to a faster TTL cirrus decay, therefore  
533 diminishing the potential impacts of the circulations (Jensen et al., 2011,  
534 Podglajen et al., 2016). These simulations testing the roles of wind shear  
535 and temperature fluctuations were carried out for individual cloud cases  
536 only. Simulations of large cloud ensembles are needed to further investigate  
537 the sensitivity of the strength of the circulations induced by the CRE-AH  
538 to initial and environmental conditions.

### 539 **3.2 Anvil clouds**

540 The deep convective plumes of cloudy air, initially of nearly uniform po-  
541 tential temperature, flatten and stretch after being injected into a stably  
542 stratified environment (Lilly, 1988). The convective plumes are self-lofted  
543 by the strong latent heating within the convective updrafts until reaching  
544 the level of neutral buoyancy, which is constrained by the clear-sky radiative  
545 cooling profile (see Hartmann and Larson, 2002 and Section 1 above). The  
546 tops of the convective outflows are colder than the surrounding environment  
547 and therefore sink, while the bottoms are warmer and rise, leading to verti-  
548 cal compression and horizontal expansion of the convective outflows (Lilly,  
549 1988) forming thick anvil clouds. From then on, cloud-radiative interactions  
550 start to play important roles in modulating the morphology and life cycle  
551 of anvil clouds.

552 As a difference from TTL cirrus, freshly detrained anvil clouds of CODs  
553 larger than about 4 develop a radiative dipole (Wall et al., 2020) character-  
554 ized by LW radiative heating near cloud bases and LW cooling near cloud  
555 tops (Figs. 6a and b). The cloud tops are in addition heated by the absorp-  
556 tion of SW radiation by the cloud condensates. The SW heating reaches  
557 comparable magnitudes to the LW cooling at the cloud tops in the middle  
558 of the day when insolation values exceeds  $1000 \text{ W m}^{-2}$  (Wall et al., 2020,  
559 Sokol and Hartmann, 2020). However, averaged over both day and night,  
560 the SW heating is of secondary importance and the net CRE-AH follows  
561 closely the LW component.

562 The resulting CRE-AH drives mesoscale circulations. In the simulations  
563 by Gasparini et al. (2019) shown in Fig. 8, the primary circulation includes  
564 an ascent in the middle of the cloud between 7 km and 11 km and a strong  
565 outflow at about 10–12 km (Fig. 8b). The primary circulation cell is closed

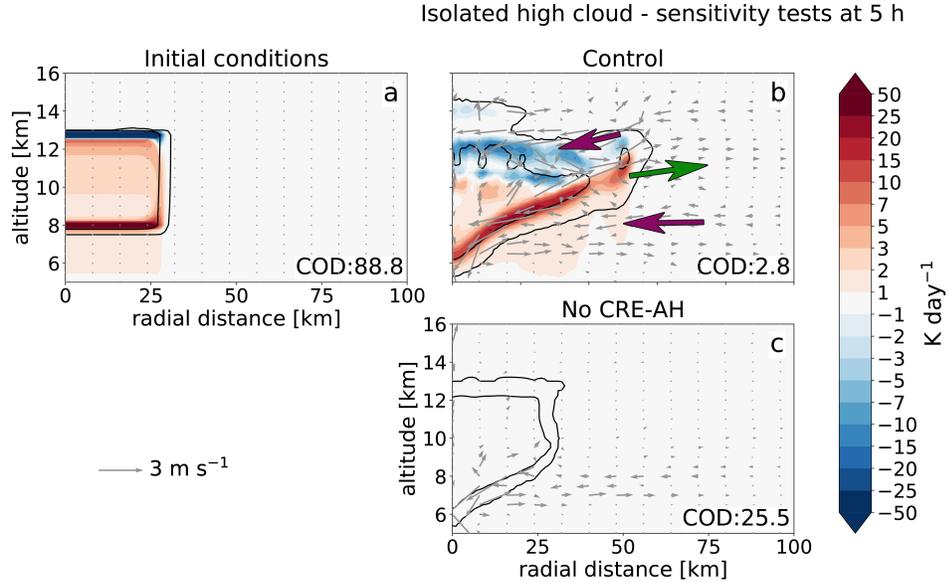


Figure 8: CRE-AH and wind vectors at (a) the initialization and (b) and (c) hour 5 after initialization of an optically thick anvil cloud simulated in a cloud-resolving model (adapted from Gasparini et al., 2019). Black contours represent ice water mixing ratios of 0.1 and  $0.0001 \text{ g kg}^{-1}$ . The vertical velocities are multiplied by a factor of 8 for a better visualization. The purple arrows highlight the inflows toward the cloud and the green arrow highlights the outflow.

566 by subsidence at the domain edge and an inflow at about 8–9 km altitude.  
 567 The circulation spreads the upper half of the cloud and narrows the lower  
 568 half of the cloud, thereby significantly changing the shape of the cloud  
 569 relative to the initialization time (Fig. 8a).

570 Also shown in Fig. 8(b), the cloud-top radiative cooling induces down-  
 571 drafts that sink the cloud top and thin the cloud. The radiative cooling  
 572 further induces an inflow of drier environmental air that erodes the cloud  
 573 top. This secondary circulation leads to the formation of an upper thin cir-  
 574 rus cloud (at about 14 km in Fig. 8b), which is later detached from the main  
 575 anvil cloud. Similar clouds were observed in in-situ aircraft measurements  
 576 (Garrett et al., 2004) and satellite remote sensing (Sokol and Hartmann,  
 577 2020).

578 Last but not least, the negative vertical gradient of the radiative heating

579 rate (cooling above 11 km, heating below 11 km) destabilizes the air at the  
 580 cloud top, resulting in convective motions and cell-like heterogeneous cloud  
 581 elements there (see the  $0.1 \text{ g kg}^{-1}$  contour in Fig. 8b).

582 The CRE-AH strongly affects the CRE at the TOA of anvil clouds. The  
 583 CRE at the TOA is the difference between the all-sky and clear-sky net (LW  
 584 plus SW) incoming (downward minus upward) radiative fluxes at the TOA.  
 585 In the simulations shown in Fig. 8, when the CRE-AH is turned off (Fig. 8c),  
 586 the cloud at hour 5 after initialization has a COD higher than 25 and a CRE  
 587 at the TOA of about  $-100 \text{ W m}^{-2}$ . In contrast, in the presence of the CRE-  
 588 AH (Fig. 8b), the cloud at hour 5 is optically much thinner with a COD of  
 589 about 3 and a CRE at the TOA of only about  $-6 \text{ W m}^{-2}$ . Integrated over  
 590 the whole cloud life cycle, the net CRE at the TOA is strongly negative in  
 591 the simulation without the CRE-AH, while the simulation with the CRE-  
 592 AH is close to being net CRE neutral at the TOA. The latter is consistent  
 593 with satellite observations that the CRE at the TOA is close to zero for  
 594 tropical convective clouds over the Indo-Pacific Warm Pool (Ramanathan  
 595 et al., 1989, Hartmann et al., 2001, Hartmann and Berry, 2017).

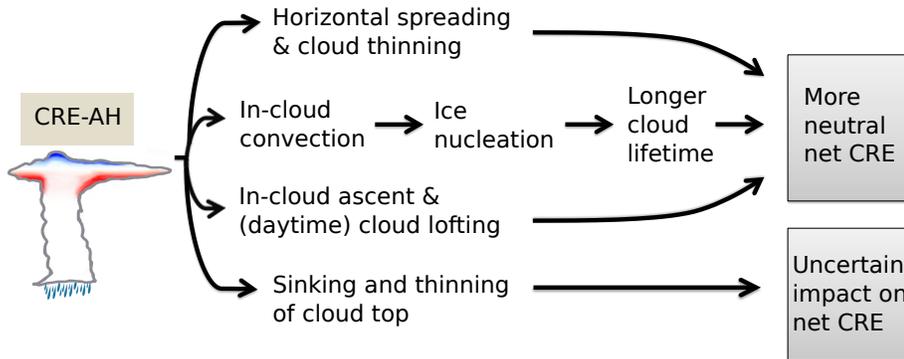


Figure 9: Mechanisms of the CRE-AH influencing the morphology and life cycle of tropical anvil clouds and their CRE at the TOA.

596 Figure 9 summarizes the mechanisms by which the CRE-AH of anvil  
 597 clouds influences their CRE at the TOA. The dominant effect comes from the  
 598 horizontal spreading of the clouds by the radiatively induced mesoscale cir-  
 599 culations. The aging, optically thin, and horizontally extensive anvil clouds  
 600 have a positive CRE at the TOA (Kubar et al., 2007, Gasparini et al.,  
 601 2019), counteracting the strongly negative CRE contribution from freshly  
 602 detrained, thick but much smaller anvil clouds.

603 The motions induced by the CRE-AH also affect the persistence and life-  
604 time of the clouds. Within the updrafts of the small-scale convective cells at  
605 the cloud tops, nucleation of new ice crystals can take place. Freshly nucle-  
606 ated ice crystals are much smaller in size and therefore sediment much more  
607 slowly than the pre-existing detrained ice crystals. The matured, optically  
608 thin anvil clouds can last a long time as they are replenished with the new  
609 ice crystals at their tops. As a result, the net CRE at the TOA integrated  
610 over the entire life cycle of anvil clouds becomes more positive (Hartmann  
611 et al., 2018).

612 In addition, the cloud radiative heating drives in-cloud ascents, which  
613 counteract ice crystal sedimentation, prolonging the cloud lifetime. On av-  
614 erage, the cloud radiative heating comes mainly from the LW absorption,  
615 but during the day the SW absorption can significantly increase the net  
616 heating rate (Ruppert and Hohenegger, 2018, Wall et al., 2020). Therefore,  
617 during the day, the radiatively induced updrafts can be strong enough to  
618 overcome ice crystal sedimentation, lifting the clouds to higher levels and  
619 colder temperatures, therefore exerting a stronger LW CRE at the TOA  
620 (Ruppert and Klocke, 2019, Wall et al., 2020). Finally, the LW cooling at  
621 the cloud tops leads to the sinking and erosion of the cloud tops, decreasing  
622 the lifetime of the anvil clouds. However, as the sinking and thinning of the  
623 clouds decrease both the LW and SW CRE at the TOA, the net effect on  
624 the TOA radiative fluxes is uncertain.

625 In summary, past observational and modeling work have highlighted the  
626 importance of the motions induced by the CRE-AH for tropical anvil clouds’  
627 evolution and radiative climatic impacts. However, we note that existing  
628 modeling studies are limited to individual cloud cases only and may not  
629 capture the full range of variation of cloud properties. Both the local CRE-  
630 AH and the CRE at the TOA of tropical high clouds are highly sensitive  
631 to the microphysical properties of ice crystals, such as their effective ra-  
632 dius and asymmetry parameter (Järvinen et al., 2018, Bantges et al., 2020).  
633 Simulations of the tropical atmosphere in which the life cycles of a diverse  
634 cloud population are captured will be needed to thoroughly evaluate how  
635 the CRE-AH influences tropical cloud distribution and radiative effects.

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