

Bathymetric influences on Antarctic ice-shelf melt rates

D. N. Goldberg¹, T. A. Smith², S. H. K. Narayanan³, P. Heimbach^{2,4,5}, M.

Morlighem⁶

¹School of Geosciences, University of Edinburgh, Edinburgh, United Kingdom

²Oden Institute for Computational Engineering and Sciences, The University of Texas at Austin, Austin,
Texas

³Mathematics and Computer Science Division, Argonne National Laboratory

⁴Jackson School of Geosciences, The University of Texas at Austin, Austin, Texas

⁵Institute for Geophysics, The University of Texas at Austin, Austin, Texas

⁶University of California Irvine, Department of Earth System Science, Irvine, California

Key Points:

- Sensitivity of ocean-driven ice-shelf melt is investigated using the adjoint of an ocean model
- Sensitivity of ice-shelf melt to ocean bathymetry is concentrated on isolated bathymetric features, with wide areas exerting little control
- Results could be used to prioritize locations of high-fidelity investigations of sub-ice shelf cavity geometry

Abstract

Ocean bathymetry exerts a strong control on ice sheet-ocean interactions within Antarctic ice-shelf cavities, where it can limit the access of warm, dense water at depth to the underside of floating ice shelves. However, ocean bathymetry is challenging to measure within or close to ice-shelf cavities. It remains unclear how uncertainty in existing bathymetry datasets affect simulated sub-ice shelf melt rates. Here we infer linear sensitivities of ice shelf melt rates to bathymetric shape with grid-scale detail by means of the adjoint of an ocean general circulation model. Both idealised and realistic-geometry experiments of sub-ice shelf cavities in West Antarctica reveal that bathymetry has a strong impact on melt in localised regions such as topographic obstacles to flow. Moreover, response of melt to bathymetric perturbation is found to be non-monotonic, with deepening leading to either increased or decreased melt depending on location. Our computational approach provides a comprehensive way of identifying regions where refined knowledge of bathymetry is most impactful, and also where bathymetric errors have relatively little effect on modelled ice sheet-ocean interactions.

1 Introduction

The bathymetry of the ocean exerts a leading order influence on ocean circulation, both at global and regional scales (e.g., Roberts & Wood, 1997; D. Marshall, 1995; Hughes & Killworth, 1995; Gille et al., 2004). It plays a key role in regulating exchanges between the Antarctic continental shelf and the deep ocean (e.g., Walker et al., 2013; Thoma et al., 2008; Graham et al., 2016; Thompson et al., 2018) and in setting circulation patterns on the continental shelf (e.g., Padman et al., 2010; Jacobs et al., 2011; Arneborg et al., 2012; Cochran & Bell, 2012; De Rydt et al., 2014; Rosier et al., 2018; Wählin et al., 2020). Its role in ice sheet-ocean interactions is accentuated by the fact that a large part of the Antarctic ice sheet rests well below sea level (Bentley et al., 1960), with a sizable portion of its margins terminating in large floating ice shelves. These ice shelves slow the speed of fast-flowing ice streams through buttressing (Thomas & Bentley, 1978; Thomas, 1979). Therefore the collapse or retreat, melting and associated thinning of ice shelves, while having a limited direct effect on sea level (Jenkins & Holland, 2007), can result in increased grounded ice loss from the continent (Shepherd et al., 2004) – a loss which may be amplified due to a positive feedback involving the geometry of sub-ice sheet topography known as the Marine Ice Sheet Instability (Schoof, 2007; Joughin et al., 2014).

50 The circulation of water under ice shelves is of great importance in the Amund-
51 sen and Bellingshausen Seas, West Antarctica, where intrusions of warm, salty Circum-
52 polar Deep Water (CDW) from the Antarctic Circumpolar Current occur (Jacobs et al.,
53 1996; Jenkins et al., 1997; Thoma et al., 2008; Arneborg et al., 2012; Jenkins et al., 2016;
54 Zhang et al., 2016), promoted in part by continental shelf geometry in these regions (Pritchard
55 et al., 2012). Regional atmospheric forcing and sea-ice states lead to stable stratifica-
56 tion of the water column that limits mixing of this dense water with cool surface layers
57 (Petty et al., 2013), allowing higher rates of ice-shelf mass loss than elsewhere in Antarc-
58 tica (Jenkins, 2016). CDW-driven ice-shelf melt is not strictly limited to the Amund-
59 sen and Bellingshausen Seas (Gwyther et al., 2014; Greene et al., 2017), and climate mod-
60 elling suggests it could become more widespread around Antarctica under climate change
61 scenarios (Hellmer et al., 2012). The ability of this warm, dense water to drive ice-shelf
62 melt depends to a large extent on how it is steered or blocked by bathymetry on the con-
63 tinental shelf and within the cavity.

64 Despite considerable efforts devoted to improving Antarctic-wide estimates of bed
65 topography (see most recently Morlighem et al. (2020)), our knowledge of bathymetry
66 in large parts of the marine margins of the ice sheet is highly uncertain. Direct obser-
67 vations of the ocean seafloor near Antarctica are beset by difficulties such as remoteness
68 and sea ice cover (Nitsche et al., 2007). Collecting bathymetric data under floating ice
69 shelves is even less practical. Autonomous submersibles capable of measurements un-
70 der floating ice shelves are only beginning to be deployed. With a ~ 300 m swath, ex-
71 tensive coverage of under-ice shelf bathymetry is not feasible (e.g., Jenkins et al., 2010).
72 Airborne gravity sensing offers an alternative means of bathymetric measurement (e.g.,
73 Tinto & Bell, 2011; Millan et al., 2017); however, gravimetric inversions are subject to
74 errors related to resolution and geologic uncertainty. Seismic observations of the bed do
75 not rely on lithology assumptions, but as they are generally ground-based, data-gathering
76 is expensive and often limited to point estimates (e.g., Rosier et al., 2018).

77 Previous studies have addressed this uncertainty in the context of a physical ocean
78 model by considering idealised bathymetries (De Rydt et al., 2014; Zhao et al., 2018) or
79 testing different bathymetry products (Schodlok et al., 2012; Goldberg et al., 2019). To
80 date, no modelling study has investigated the melt response to the full range of uncer-
81 tainty in sub-ice shelf bathymetry. Here, we aim to provide a better understanding of

82 this uncertainty by estimating the sensitivity of ocean-driven ice-shelf melt rates to bathymetry
83 in a West Antarctic sector.

84 Previously, Losch & Heimbach (2007) developed a method to calculate the sensi-
85 tivity of circulation metrics (e.g., the strength of meridional overturning or zonal mass
86 transport) to ocean bathymetry using the adjoint of the Massachusetts Institute of Tech-
87 nology general circulation model (MITgcm). In general, adjoint models generate linearized
88 sensitivities of model outputs to an arbitrarily large set of input parameters (Wunsch,
89 1996), providing a computationally efficient means for investigating the impacts of grid-
90 scale uncertainties. To avoid tedious “by-hand” differentiation of a complex ocean gen-
91 eral circulation model, Losch & Heimbach (2007) made use of *algorithmic differentia-*
92 *tion* (AD) software, which has been used extensively with the MITgcm (Heimbach et al.,
93 2005; Wunsch et al., 2009). However, this adjoint model involving bathymetry sensitiv-
94 ities has not been extensively used since, and has not previously been applied to sub-
95 ice shelf circulation.

96 In this paper, we “revive” the adjoint model infrastructure for treating bathymetry
97 as an uncertain input variable, and employ this framework to investigate the impacts of
98 bathymetric uncertainty on ice-shelf melt rates. Two important technical improvements
99 are (i) the use of an open-source AD tool to generate the adjoint model, and (ii) improved
100 treatment of the implicit free-surface solver in generating the adjoint model. These are
101 summarized in Section 2, where we briefly discuss our methodology, including our ad-
102 joint approach and our updates to the MITgcm code base (with further details in the
103 Section 1 of the supplementary material). We apply our framework to an idealised do-
104 main and analyse the resulting sensitivities (Section 3). We then carry out a study of
105 the Crosson and Dotson ice shelves in the Amundsen Sea Embayment (Section 4), and
106 conclude with discussion in Section 5.

107 **2 Methodology**

108 **2.1 Modelling of ice-ocean interactions**

109 We simulate sub-ice shelf circulation with the MITgcm, an open-source general purpose
110 finite-volume code which solves the hydrostatic primitive equations on the rotat-
111 ing sphere governing ocean flow (J. Marshall et al., 1997). (The code has nonhydrostatic
112 capability but it is not used in this study.) Since its inception, code “packages” repre-

113 sending modularized parameterizations, numerical algorithms, and separate climate com-
 114 ponents have been introduced. One such package, **SHELFICE** (Losch, 2008), allows for
 115 circulation in cavities beneath ice shelves that may be many hundreds of meters deep.
 116 **SHELFICE** also calculates melt rates and the associated heat and salt fluxes at the ice-
 117 ocean interface based on under-ice ocean properties using a viscous sublayer parameter-
 118 ization (Holland & Jenkins, 1999). In this study we use the velocity-dependent form of
 119 the melt parameterization (Dansereau et al., 2014), unless otherwise stated. The ice-ocean
 120 model has successfully run the Ice Shelf Ocean Model Intercomparison Experiment (ISOMIP;
 121 Holland et al. (2003)), the experimental setup of which forms the basis for our first ex-
 122 periment.

123 **2.2 Discretization of bathymetry in the MITgcm**

124 The vertical discretization of bathymetry in MITgcm is distinct from other aspects
 125 of discretization in the model, and given the nature of this study it deserves mention.
 126 To allow for varying bathymetry but avoid dramatic steps due to the prescribed verti-
 127 cal level thicknesses, a *partial cell* discretization is implemented (Adcroft et al., 1997),
 128 where bottom cells can be partially fluid-filled with fraction h_f , down to a minimum spec-
 129 ified thickness $h_{f,min}$. This means that vertical cell faces (i.e. faces normal to horizon-
 130 tal directions) are partially fluid-filled as well, which is important as cell faces determine
 131 volume and tracer transport. Due to memory requirements, bathymetry is represented
 132 as piecewise-constant (as opposed to piecewise-linear), meaning fluid fractions at cell faces
 133 are a function of depth at adjacent cell centers (see Fig. 1(a)). This choice has impli-
 134 cations for algorithmic differentiation of bottom sensitivity, as discussed below.

135 **2.3 Adjoint model**

136 An ocean model may be conceptualised as a mathematical function that maps an
 137 input vector \mathbf{x}_{in} onto an output vector \mathbf{x}_{out} . The input vector \mathbf{x}_{in} consists of the dis-
 138 cretized initial conditions for the oceanic state, as well as all inputs required to integrate
 139 the partial differential equations that govern the circulation of the ocean, including dis-
 140 cretized input fields for surface (forcing) and bottom (bathymetry) boundary conditions.
 141 \mathbf{x}_{out} consists of all prognostic model output (generally of a much higher dimension than
 142 that of \mathbf{x}_{in}), or diagnostic functions thereof, including scalar-valued metrics. It is often
 143 of interest to know how perturbations in \mathbf{x}_{in} affect \mathbf{x}_{out} , or how they affect quantities

144 that depend on \mathbf{x}_{out} (sometimes referred to as “objective functions” or “quantities of in-
145 terest”). An example application of an adjoint model might be investigating how Atlantic
146 meridional overturning is sensitive to global patterns of precipitation (Pillar et al., 2016;
147 Smith & Heimbach, 2019).

148 The *sensitivity vector*, i.e. the gradient of the quantity of interest with respect to
149 \mathbf{x}_{in} , could be determined by perturbing separately each element of \mathbf{x}_{in} and observing
150 the model response (formally, inferring a directional derivative); however, such an ap-
151 proach for computationally intensive models and input vectors of high dimension is im-
152 practical. However, forming the *adjoint* of the model (or, more precisely, the adjoint of
153 its Jacobian) provides an alternative means (Errico, 1997), enabling calculation of the
154 sensitivity vector at a computational cost that does not depend on the dimension of \mathbf{x}_{in} .

155 Differentiation of the ocean model can be carried out at the equation level (Sirkes
156 & Tziperman, 1997), though this approach requires a separate code that must be up-
157 dated when the ocean model is modified. Another method – and the one used in this work
158 – is Algorithmic Differentiation (AD), which uses a software tool to automate differen-
159 tiation of the model at the discrete (code) level. In this study, two different AD tools are
160 used: *Transformations of Algorithms in Fortran* (TAF; Giering et al. (2005)) and Ope-
161 nAD (Utke et al., 2008). Both are source-to-source tools, meaning code is generated in
162 the native language (as opposed to operator-overloading). Both tools have been used to
163 generate the MITgcm adjoint; TAF, a commercial product, has been used more exten-
164 sively with the MITgcm, while OpenAD is a more recent open-source tool.

165 While AD presents great benefits in differentiating complex numerical codes and
166 keeping the adjoint code in synchronization with the parent numerical code, some de-
167 gree of manual intervention is generally required. In the present study changes to the
168 adjoint generation were necessary to facilitate efficient computation, the foremost deal-
169 ing with the way in which MITgcm evolves the ocean free surface. These and other de-
170 tails are discussed in detail in Section 1 of the supplementary material (Giles et al., 2002).

171 **3 Idealised Experiment**

172 To gain insight into how bathymetry modulates the interaction between ocean cir-
173 culation and ice shelf melt, we first examine sensitivity of melt to bathymetry in an ide-
174 alized domain, which is a slightly modified version of the computational domain used in

175 the Ice Shelf Ocean Model Intercomparison Project (ISOMIP; Holland et al. (2003)). In
 176 the MITgcm implementation of the standard ISOMIP setup, the ocean circulates within
 177 a closed rectangular domain with a flat bathymetry of 900 m depth, with an initially uni-
 178 form temperature of -1.9°C . A zonally-uniform ice-shelf draft slopes meridionally from
 179 700 m depth to 200 m depth over about 450 km, and is constant north of this point. We
 180 use a resolution of 30 m in the vertical, 0.3° zonally, and 0.1° meridionally (amounting
 181 to ~ 8.5 km zonally and ~ 11 km meridionally. A full description can be found in Losch
 182 (2008); to enable a direct comparison with that study, we specify velocity-independent
 183 turbulent exchange coefficients in the melt rate parameterisation. We modify the ISOMIP
 184 domain by introducing a zonally-constant ridge in the bathymetry just south of the point
 185 of deepening of the ice shelf. The meridional expression is a half-cosine “bump” with a
 186 width of 2° latitude and a height of 200 m above the uniform seafloor (Fig. 2(a)), and
 187 we refer to our experiment as “ISOMIP-bump”. This bathymetry is inspired by bathy-
 188 metric ridges identified under a number of Antarctic ice shelves (e.g., Jenkins et al., 2010;
 189 Wei et al., 2019), which are found to strongly control the transport of relatively warm
 190 water within ice shelf cavities (De Rydt et al., 2014; Dutrieux et al., 2014).

191 Our adjoint experiment is as follows: the ISOMIP-bump model is run forward in
 192 time for 2 model years, and the spatial integral of the melt rate in the final time step
 193 is evaluated as our quantity of interest J :

$$194 \quad J = \sum_i d_i m_i, \quad (1)$$

195 where d_i and m_i are the area of, and melt rate within, horizontal cell i . The adjoint model
 196 accumulates sensitivity of J with respect to bathymetry back in time along the 2-year
 197 simulation trajectory and thus depends on the state of the entire 2-year run, not just the
 198 final state. Thus, to mitigate impacts of equilibration, we begin the model run from a
 199 “spun-up” state rather than a quiescent one. The model is thus first spun-up for 3 years,
 200 and the resulting state forms the initial conditions for our 2-year forward and adjoint
 201 run.

202 **3.1 Results**

203 The melt (and accretion) rate at the final time in the adjoint experiment (Fig. 2(b))
 204 has a similar pattern to that of Mathiot et al. (2017) (their Fig. 2), although melt and
 205 accretion rates are generally smaller (with the peak accretion being about 1/3 of that

206 of Mathiot et al. (2017)), and there is a “tongue” of melt rates bisecting the accretion
 207 region over the ridge. The barotropic circulation also differs slightly with respect to the
 208 standard ISOMIP experiment: rather than a broad cyclonic gyre, there is a narrow an-
 209 ticyclonic anomaly on the north side of the ridge (Fig. 2(b)). Barotropic flow is primar-
 210 ily along the ridge, crossing it primarily near the eastern and western boundaries, sim-
 211 ilar to what has been shown in a simplified two layer model (Zhao et al., 2018). Zonally-
 212 averaged temperatures (Fig. 2(a)) suggest slightly cooler waters at depth just south of
 213 the ridge as opposed to the northern flank. The smaller melt and accretion rates as com-
 214 pared to Mathiot et al. (2017) could reflect the fact that our simulation has not yet reached
 215 steady-state – indicating that the presence of the ridge increases the time to reach a new
 216 steady-state. Alternatively, the ridge may act as a potential vorticity barrier, prevent-
 217 ing warmer bottom waters from coming in contact with the shelf (De Rydt et al., 2014;
 218 Zhao et al., 2018).

219 The adjoint-derived sensitivities are shown in Fig. 3(a). In this figure, shading indi-
 220 cates $\frac{\partial J}{\partial \delta R_i}$, where R_i is bottom depth at location i . Positive values indicate locations
 221 where raising the seafloor will increase integrated melt, and negative values indicate where
 222 lowering the seafloor will increase melt. There are distinct broad-scale patterns in the
 223 sensitivities, particularly over the ridge itself. Across much of the zonal extent of the ridge
 224 there is negative sensitivity (region 1 in Fig. 3(a)), indicating a lowering of the ridge would
 225 increase melt. Near the eastern boundary, however, there is a region with strongly pos-
 226 itive sensitivities (region 2). Northward of the ridge where both bathymetry and ice draft
 227 are constant, there is a broad dipole pattern, with positive sensitivities toward the cen-
 228 ter (region 3) and negative toward the east (region 4). In our investigation below we fo-
 229 cus on these four regions, foregoing close analysis of areas with negligible influence on
 230 melt (such as southward of the ridge), and areas where there is strong spatial variabil-
 231 ity in the sensitivity, such as the western edge of the ridge.

232 In order to ensure that adjoint sensitivity patterns did not arise from issues involv-
 233 ing Algorithmic Differentiation, both AD tools (OpenAD and TAF) were used to gen-
 234 erate sensitivities. (A similar approach was taken in Heimbach et al. (2011).) The dif-
 235 ferences in the sensitivities, likely arising from numerical truncation, were negligible, and
 236 are not shown.

237

3.2 Finite-amplitude perturbations of bathymetry

238

239

240

241

242

243

244

245

246

247

As with any adjoint-based study, it is important to verify the adjoint-derived sensitivities by perturbing the input, or *control*, field in the forward model, i.e. by estimating finite-difference approximations to the gradients that the adjoint model calculates. In the MITgcm this type of “gradient check” is more challenging when dealing with model bathymetry than with other control variables, as demonstrated in Fig. 1(b): finite perturbations of bathymetry can change grid structure, for example by adding new cells to, or removing cells from, the domain. Neither operation is differentiable, and hence linearized sensitivities may not reflect model responses to perturbed bathymetry. Additionally, bathymetric perturbations may not be as anticipated, as thicknesses of cells will be adjusted by the model initialization to ensure no partial cell is thinner than $h_{f,min}$.

248

249

250

251

252

253

254

These challenges aside, we implement finite perturbations to bathymetry in order to test the results from the adjoint model, but our experiment design is intended to minimize the above complications. Rather than perturb values in individual cells, we apply perturbation *patterns*. We carry out experiments with four separate perturbation patterns, naturally selected in regions of high sensitivity, where bathymetric perturbations exhibit the greatest control on melt-rates, as shown in Fig. 3(a). The patterns have a Gaussian profile:

255

$$\delta R(\phi, \lambda) = \delta R_0 \exp \left(-\frac{(\phi - \phi_0)^2}{L_\phi^2} - \frac{(\lambda - \lambda_0)^2}{L_\lambda^2} \right) \quad (2)$$

256

257

258

where ϕ and λ are latitude and longitude. ϕ_0 , λ_0 , L_ϕ and L_λ vary with experiment but the location and radii of the perturbations can be seen from Fig. 4 for each region. Different values of δR_0 are considered as described below.

259

260

For a given depth perturbation δR , the linear response to J predicted by the adjoint is

261

$$\delta J = \sum_i \delta J_i = \sum_i (\delta R_i) (\delta^* R_i), \quad (3)$$

262

263

264

265

266

267

268

where δR_i is the finite perturbation to bathymetry in ocean column i and $\delta^* R_i = \frac{\partial J}{\partial R_i}$ is the bathymetric sensitivity in i as calculated by the adjoint. If the adjoint model is accurate, Eqn. (3) should be fairly accurate for small values of δR_i . This is the case for $\delta R_0 = 0.1$ m (Fig. 3(b)). Positive and negative perturbations are considered in regions 1 and 2; in regions 3 and 4 only positive perturbations are examined as negative perturbations would lower bathymetry beyond the extent of the computational grid. For larger perturbations ($\delta R_0 = 10$ m), linear sensitivities give fairly accurate predictions in re-

269 regions 2, 3 and 4; in region 1 (the center of the ridge), the linear approximation under-
 270 estimates the response. Closer inspection reveals that, when bathymetry is perturbed
 271 in the center of the ridge, a number of fluid-containing cells become empty. Similarly,
 272 when regions 1 and 2 are negatively perturbed with $\delta R_0 = 10$ m, an even larger num-
 273 ber of previously empty cells become fluid-filled. These non-differentiable changes could
 274 explain the underestimates.

275 Examining the perturbed melt rates and circulation provides further insight into
 276 the sensitivity patterns produced by the adjoint model. Bathymetric rises in regions 3
 277 and 4 affect melt rates predominantly to the north (i.e. oceanward) of the bathymetric
 278 ridge (Fig. 4(c,d)). Examination of the perturbed barotropic circulation (Fig. S2(c,d)
 279 of the supplementary material) shows that in both cases, an anticyclonic region devel-
 280 ops to the west of the rise, and a cyclonic region to the east. The pattern is reminiscent
 281 of the interaction between a jet and a topographic rise (Huppert & Bryan, 1976; Hol-
 282 land et al., 2003), with the broad cyclonic cell in this region (Fig. 2(b)) generating the
 283 background flow. As this cell transports water away from the cold outflow from the cav-
 284 ity before it circulates back toward the ridge, it is likely that perturbations which strength-
 285 en/oppose this circulation will increase/decrease melt – although as Figs. 4(c,d) indi-
 286 cate, this effect does not penetrate beyond the ridge.

287 For perturbations to the ridge itself (regions 1 and 2), there is a more complex melt
 288 response, the effects of which are felt more strongly to the south of the ridge (Fig. 4(a,b)).
 289 In terms of the circulation, there is a similar response to the barotropic stream function
 290 as with regions 3 and 4, although complicated by the varying background topography.
 291 In the case of a raised bump on the eastern ridge (region 2), the leading effect on the cir-
 292 culation is a southward shift of the warm jet travelling eastward along the ridge (Sup-
 293 plemental Fig. S2(b)). There is decreased melt in the southeast of the ice shelf, but this
 294 is offset by stronger melt above the ridge and decreased accretion in the western outflow
 295 (Fig. 4(b)). A rise in the center of the ridge has the opposite effect, decreasing melt over
 296 the ridge 4(a)).

297 While these results are highly idealized, they are nonetheless instructive regard-
 298 ing bathymetric influence on melt in ice-shelf cavities with topographic obstacles: (1)
 299 bathymetry in areas “protected” by the obstacle play a relatively small role in control-
 300 ling melt; (2) the height of the obstacle has a strong influence on melt, but the direc-

tion, or sign, of the influence may depend on the location along the ridge and related to the background flow that is set up by the geometry; and (3) bathymetry oceanward of the obstacle can influence melt as well, by controlling the circulation that brings warm water toward the ice-shelf cavity. These insights inform the interpretation of sensitivities in simulations with realistic bathymetry.

The perturbation experiments offer a further lesson: an adjoint indicates linear sensitivities of a scalar objective function, such as integrated melt rates – but it does not indicate how the *pattern* of melt will change in response to inputs. If melt in a certain location, or changes of a specific pattern, are of interest, a different objective function should be considered.

4 Realistic experiment: Dotson and Crosson ice shelves

The Dotson and Crosson Ice Shelves are relatively small but strongly thermally-forced ice shelves in the Amundsen Sea Embayment of West Antarctica (Fig. 5(a)). Recently, these ice shelves, as well as the ice streams that flow into them, have been the subject of focused glaciological and oceanographic study (e.g., Randall-Goodwin et al., 2015; Goldberg et al., 2015; Miles et al., 2016; Gourmelen et al., 2017; Jenkins et al., 2018; Lilien et al., 2018). Moreover, ice-ocean interactions under these ice shelves have significance for biological productivity in the Southern Ocean: levels of carbon sequestration in the highly productive Amundsen Polynya are thought to be connected strongly to ice-shelf melt volume (Gerringa et al., 2012; Yager et al., 2012). A recent modelling study by Goldberg et al. (2019) showed that the choice of bathymetric product has a significant influence on the melt rates modelled for these ice shelves. Therefore, it is an ideal region in which to examine the sensitivity of melt to bathymetry.

4.1 Model configuration

Our ocean model configuration is based on that of Goldberg et al. (2019). We use the MITgcm with the SHELFICE package and with ice-shelf draft and bathymetry based on Millan et al. (2017). At ocean-facing boundaries we impose conditions on temperature, salinity and velocity from a regional simulation by Kimura et al. (2017). However, there are important differences with the configuration of Goldberg et al. (2019), which are largely influenced by practical considerations concerning the performance of the OpenAD-

331 generated adjoint. Adjoint models generally require more computing time than the for-
332 ward models from which they derive, requiring in some cases recomputation to avoid in-
333 tractable memory requirements (Griewank & Walther, 2008). The 4-year simulations con-
334 ducted by Goldberg et al. (2019) ran for approximately 32 hours on 48 cores on the Re-
335 search Councils UK (RCUK) ARCHER supercomputer (discounting queueing times in
336 between batches), meaning an adjoint experiment might require up to several weeks' wall-
337 clock execution time leading to large delays in our investigations and potentially irre-
338 sponsible energy usage. (This scaling is based on the timings of experiments in this study
339 and not a rigorous analysis of OpenAD performance.) Thus, modifications were made
340 to reduce computational expense and facilitate adjoint computation.

341 A 2-km grid was used as opposed to a 1-km grid, and the time step increased from
342 150 to 300 seconds. Additionally, a larger horizontal eddy viscosity, $\nu_H = 120 \text{ m}^2\text{s}^{-1}$,
343 was imposed, for the following reason. The ocean adjoint model is a distinct numerical
344 code – related to the forward ocean model but with its own stability constraints, aris-
345 ing in part from the chosen quantity of interest, which informs the boundary and ini-
346 tial conditions of the adjoint model. It is often the case that the adjoint of a nonlinear
347 forward model produces sensitivity patterns with sharp spatial gradients, which grow in
348 amplitude over time because the model lacks the nonlinear feedbacks to damp them, re-
349 sulting in numerical instabilities. Hoteit et al. (2005) showed that a stabilization of the
350 adjoint may be achieved with a larger value of ν_h for the adjoint model, while retain-
351 ing a smaller eddy viscosity in the forward model, but such a capability for the OpenAD-
352 MITgcm adjoint is not yet available. We point out that our chosen value for ν_h is smaller
353 than that used in the ice-ocean interaction study of Dansereau et al. (2014), which also
354 used the SHELFICE package of MITgcm.

355 Additionally the open boundary conditions of our computational domain, which
356 represent interactions with the Antarctic Circumpolar Current (i.e. the ocean-facing bound-
357 ary conditions), were made time-constant rather than time-varying as in Goldberg et al.
358 (2019). As discussed in Section 4.3, this better enables the assessment of the timescale
359 of adjustment to boundary conditions. Velocity, temperature and salt conditions from
360 Kimura et al. (2017) were averaged over 2011 (the highest-melt year in the the Goldberg
361 et al. (2019) study), allowing for a shorter experiment.

362 Finally, the Millan et al. (2017) bathymetry was adjusted over a region of approx-
363 imately 90 km² close to the junction between Crosson and Dotson Ice Shelves, where the
364 Kohler range extends into the ice-shelf cavity (Fig. 5(a)). In this area, the Millan bathymetry
365 suggests a significant ridge with a peak less than 300 m below sea level. Without mod-
366 ification, this ridge would lead to very thin ocean columns in our model, effectively lim-
367 iting ocean transport to the narrow region between the ridge and Bear Peninsula. How-
368 ever, observed melt rate patterns (Gourmelen et al., 2017; Goldberg et al., 2019) show
369 high melt rates in this location, suggesting a more extensive connection between the ice
370 shelves than the bathymetry product would allow. Furthermore, recent glider and float
371 observations in this region (which are not incorporated into the version of BedMachine
372 used in this study) show that this ridge may be lower than suggested by the gravime-
373 try (Dutrieux et al., 2020). We adjust bathymetry in this region to a maximum of 500 m
374 depth. Our modification of this bathymetry in this region allows a wider area for ocean
375 flow while still maintaining a ridge at the Dotson-Crosson junction. While our modifi-
376 cation is not observationally grounded, our adjoint computation (described below) gives
377 an indication of the impact of this modification. If circulation in this region were neg-
378 ligible, such assessment might not be possible.

379 Our adjoint experiment largely mirrors that of the ISOMIP-bump experiment. Prior
380 to the adjoint run, the Dotson-Crosson model is spun up for 3 years, over the last year
381 of which total melt varies by less than 1%. Beginning with this spun-up state, the ad-
382 joint model is run for 1 year, and the sensitivity of the objective function J – the spa-
383 tial integral of melt – with respect to bathymetry is computed. The realistic experiment
384 was carried out only with the OpenAD-generated adjoint model. Even with the afore-
385 mentioned adjustments to shorten the required wallclock time of the run, an additional
386 modification to OpenAD was required to circumvent limits on wallclock time on HPC
387 systems. This technical modification is referred to as resilient adjoints and is described
388 in Section 2 of the supplementary material (Aupy et al., 2014; Griewank & Walther, 2000).

389 4.2 Results

390 Relevant aspects of the forward model are depicted in Fig. 5. Despite the lower res-
391 olution and higher viscosity compared to the configuration used by Goldberg et al. (2019),
392 the melt rate patterns are similar. Broadly consistent with observation-based inferences
393 (Randall-Goodwin et al., 2015), there is a strong outflow at the western margin of Dot-

394 son Ice Shelf – though in our model outflow is less confined to the margin, potentially
395 due to high viscosities or horizontal resolution. The total melt rate is approximately 81.5
396 Gt/yr (Fig. 6(b)), similar to that found by Randall-Goodwin et al. (2015) for Dotson
397 ice shelf alone in January 2011. Melt rates in the simulation domain are insensitive to
398 bathymetry under much of the Dotson Ice Shelf (Fig. 6(a)), with the exception of the
399 junction with Crosson Ice Shelf and over the small ridge at the entrance of the ice shelf
400 (the “outer ridge” labelled in Fig. 6(a)).

401 The sensitivity pattern over the outer ridge bears similarities to the idealized ISOMIP-
402 bump experiment – with negative sensitivities in the centre of the ridge, indicating a low-
403 ering would increase melt, and positive sensitivities at the margins. In the junction be-
404 tween Crosson and Dotson ice shelves, there is a somewhat similar pattern, with neg-
405 ative sensitivities along the crest of the ridge (the “inner ridge” indicated in Fig. 6) and
406 positive sensitivities closer to Bear Peninsula where the bed is slightly deeper. However,
407 this pattern should be regarded with caution due to the modifications made to the bathymetry
408 (Section 4.1, Fig. 5(a)).

409 The most coherent pattern of sensitivity oceanward of Dotson is in the eastern side
410 of the trough entering the cavity (Fig. 6). The negative sensitivities downslope and pos-
411 itive sensitivities upslope imply that a steepening of the trough margin would amplify
412 the geostrophically driven flow of warm water to the ice shelf, and thus increase melt-
413 ing. This result is corroborated by recent observational and experimental work which
414 highlights the critical role of topography in steering heat to Antarctic ice shelves (Wählin
415 et al., 2020).

416 Under Crosson Ice Shelf, there are fairly weak but extensive positive sensitivities,
417 indicating raising of the bed would increase melt, which at first seems counter-intuitive.
418 This could arise because the cavity column depth is relatively small (on average, the col-
419 umn depth under Crosson is ~ 150 m less than under Dotson), meaning a shallower col-
420 umn would bring inflowing CDW closer to the ice shelf. Oceanward of Crosson, there
421 are coherent areas of negative sensitivity, correlating with localized bathymetric highs,
422 indicating that lowering in these regions would increase melt. However, this is not a con-
423 sistent pattern, as there is a region along the front with positive sensitivities, indicat-
424 ing that in this shallow-bedded region, raising the bed would actually increase melt rates.

4.3 Equilibration of adjoint sensitivities

Although the adjoint model represents a differentiation of all physical processes, this does not guarantee that the adjoint run should capture the dominant linear adjustments associated with bathymetric influence of melt. This is because these adjustments operate over an intrinsic time scale (e.g. Heimbach & Losch, 2012), and it is difficult to know *a priori* if the adjoint run encompasses this scale.

The nature of our adjoint run allows us to evaluate whether this adjustment is captured *a posteriori*. The bathymetry field in the ocean model ultimately affects the model through the partial cell factors h_f (cf. Section 2.2), and related factors h_f^w and h_f^s , the fluid-filled portion of cell faces at the southern and western sides of bottom cells. This dependency among the cell factors is set in the initialization of the model. Thus, if the *adjoint sensitivity* fields corresponding to these variables are relatively steady as the adjoint model steps backward in time, then bathymetric sensitivities are *converged*: they would not change significantly with a longer run. In physical terms, this would imply that the length of the simulation is on the order of the time scale of adjustment to perturbations or greater.

Fig. 6(b) shows the Euclidean norm of the δ^*h_f field, the adjoint sensitivity of h_f , as the adjoint model evolves, which it does backward in time (from month 12 to 0). Similar time series are shown for adjoint fields corresponding to the h_f^w and h_f^s fields. $\delta^*h_f^w$ and $\delta^*h_f^s$ norms have roughly steadied by the end of the adjoint run (month 0), while δ^*h_f is steadily growing. However, δ^*h_f only makes a small contribution to bathymetric sensitivity over this time period. Since the vertical faces h_f^w and h_f^s determine horizontal transport in the bottom cells, these results suggest the immediate effect of changing bathymetry is on transport, with a timescale of about a year for the present model. However, partial cell volume, which affects, among other things, the heat content at depth, might have strong impacts on melt rate over much longer time scales, not considered here.

We point out that our ability to evaluate adjoint equilibration in this manner is due to our use of time-invariant controls. In adjoint experiments involving time-varying controls, such as wind forcing or time-evolving boundary conditions (e.g., Heimbach & Losch, 2012), the adjoint sensitivity would not be expected to asymptotically approach a “steady state” in reverse-time.

4.4 Impact of bathymetry product uncertainty

As demonstrated in Goldberg et al. (2019), one application of adjoint sensitivities is in estimating the impact of an alternative data product on the quantity of interest. Recently, a new bathymetric product for Antarctica became available, BedMachine (Morlighem et al., 2020), which differs from that of Millan et al. (2017). In particular, there are large differences within the ice shelf cavities, especially for Dotson (Fig. 7(a)), as the bathymetry of Millan was later updated by using the methodology described in An et al. (2019), which makes use of independent measurements of bathymetry to estimate airborne gravity inversion errors arising from density variations.

In a similar fashion to the idealized finite perturbation experiments in section 3.2, we estimate the impact of using the BedMachine product rather than the Millan product by inputting their difference into Eqn. (3). This formula results in an estimated 10 Gt/yr increase in Dotson and Crosson melt-rates resulting purely from the differences in these two products. It is informative to examine which areas of the ice-shelf cavities actually contribute to this increase. This can be seen from Fig. 7(b), which shows

$$\delta J_i = (\delta R_i)(\delta^* R_i) \quad (4)$$

i.e. the summand of Eqn. (3), for this combination of bathymetric perturbation and adjoint sensitivity. Despite the extensive differences in bathymetry under Dotson between the products, there are only a few regions where this difference matters, which are elucidated by the sensitivity pattern in Fig. 6. Most prominently, the representation of the ridge near the front of Dotson, which is far less pronounced in the BedMachine product, accounts for 4.3 Gt/yr difference in melt-rates (Fig. 7(b)).

Of course, this estimate is only a first order approximation as it assumes that this linear term dominates any higher order (i.e. nonlinear) effects. As in Section 3.2, we compare the perturbation in melt to that predicted by the adjoint-based analysis with the response of the full nonlinear model. To this end we run a forward experiment using BedMachine data interpolated to our grid. As the BedMachine data set is in certain locations deeper than our baseline bathymetry by hundreds of meters, there are additional fluid-filled cells whose properties must be initialised. We assign these cells the initial temperature and salinity of the bottom fluid-filled cell in our baseline simulation.

486 The resulting melt rate forced by BedMachine bathymetry is 71 Gt/yr, which is
 487 10 Gt/yr less than the baseline simulation – the *opposite* of that predicted by the adjoint-
 488 based analysis. It should be kept in mind that this response is a composite of responses
 489 to a number of large-scale *features*, such as the lowering of the outer ridge under Dot-
 490 son ice shelf (Fig. 7(a)). We conduct one additional forward perturbation experiment,
 491 in which we replace Millan data with BedMachine data, only within the region indicated
 492 in Fig. 7(b), i.e. the outer Dotson ridge. The response is an increase in 3.3 Gt/yr, which
 493 compares more favorably with the 4.3 Gt/yr predicted by the adjoint analysis.

494 Our results suggest that our adjoint approach is not likely to reflect the melt re-
 495 sponse to bathymetric uncertainty at the regional scale. This is not a complete surprise
 496 as the adjoint model provides sensitivities linearized about a reference state – in our case,
 497 the ocean state given the Millan bathymetry – and changes across the entire model do-
 498 main of O(100m) are not likely to be captured within a linear regime. On the other hand,
 499 we find it encouraging that our model reasonably predicts the response to somewhat more
 500 localized perturbations, such as the lowering of the outer ridge under Dotson as shown
 501 here. Moreover, we posit that the adjoint model can be a useful tool for identifying these
 502 important features, so that the underlying causal drivers can be readily explored in a tar-
 503 geted effort.

504 **4.5 Sensitivity of grounded ice loss to ocean bathymetry**

505 Understanding the impact of ocean bathymetry on sub-ice shelf melt rates is im-
 506 portant due to the impact of melting on the loss of buttressing and grounded ice volume
 507 (i.e. the volume of ice that can contribute to sea level, Bamber et al. (2018)). The ex-
 508 periments above focus on melt rate as a target quantity of interest, rather than grounded
 509 ice volume. To comprehensively estimate sensitivity of grounded ice volume to ocean and
 510 sub-ice sheet bathymetric uncertainty would require the adjoint to a fully coupled ice
 511 sheet-ocean model, which does not presently exist.

512 Nevertheless, with our current framework we can begin to explore pathways of sen-
 513 sitivity from ocean model inputs to ice-sheet state-related quantities of interest. In math-
 514 ematical terms, we seek the total sensitivity of ice sheet volume (as our quantity of in-
 515 terest) to bathymetry, that is, $\frac{\partial V}{\partial R_i}$ where V is grounded ice volume and R is bathymetry
 516 in location i . We emphasize that this quantity is distinct from sensitivity of grounded

517 volume to under-ice bathymetry, which directly controls ice flow and dynamic thinning;
 518 rather, the pathway of influence considered here is through control on melt rates, which
 519 in turn impact ice-shelf buttressing (see illustration in Fig. 8(a)). Thus, for ocean bathy-
 520 metric grid points, R_i , we may write:

$$521 \quad \frac{\partial V}{\partial R_i} = \sum_k \frac{\partial V}{\partial m_k} \frac{\partial m_k}{\partial R_i}. \quad (5)$$

522 where m_k is ocean melt rate in cell k and $\frac{\partial V}{\partial m_k}$ is the ice-sheet model derivative of grounded
 523 volume with respect to melt in cell k . While calculating sensitivity of grounded ice vol-
 524 ume to melt is beyond the scope of an ocean model, an ice-sheet model framework to
 525 do this does exist (e.g., Goldberg & Heimbach, 2013). If these sensitivities can be found,
 526 then a new quantity of interest for the ocean model can be defined:

$$527 \quad J_{gv} = (\nabla_{\mathbf{m}} V)^T \mathbf{m} \equiv \sum_k \left(\frac{\partial V}{\partial m_k} \right) m_k, \quad (6)$$

528 Note that if the first term in the inner product is external to the ocean model, then the
 529 gradient of J_{gv} with respect to R_i , ocean bathymetry in location i , is equivalent to the
 530 expression on the right hand side of Eqn. (5). A different way of seeing this is that the
 531 product “projects” patterns of ice sheet volume sensitivities to melt rates onto melt rate
 532 sensitivities to ocean bottom topography.

533 In Goldberg et al. (2019), an *ice-sheet* adjoint model was used to find the sensitiv-
 534 ity of grounded volume of Smith Glacier, the glacier that feeds Dotson and Crosson Ice
 535 Shelves, to ice-shelf melt rates (Fig. 8(b)). These ice-melt sensitivities are used to con-
 536 struct the quantity of interest J_{gv} and sensitivities with respect to ocean bathymetry are
 537 found. This result is shown in Fig. 8(c). The most striking feature of this result is the
 538 similarity of the pattern to that of Fig. 6, the sensitivity of melt to bathymetry (R^2 of
 539 0.93; see also Fig. 8(d)). Comparing Eqns. (1) and (6), the quantities of interest effec-
 540 tively differ only in a weighting of melt rate by grounded ice volume sensitivities. Thus
 541 the similarity in Figs. 8(c) and 6 suggests that only *total*, or spatially integrated, melt
 542 can be strongly affected by bathymetry; whereas melt rate *patterns* are controlled by other
 543 factors such as ice-shelf geometry (Goldberg et al., 2019).

544 We point out this sequence of adjoint sensitivity calculations, in which ice-sheet
 545 sensitivity is passed to an ocean model adjoint, which is in turn used to find ocean sen-
 546 sitivity, is a simplified representation of a coupled adjoint ice-ocean model. In a prop-
 547 erly coupled model, the ocean provides melt rates to the ice sheet, while the ice sheet

548 provides ice-shelf drafts to the ocean model, with these fields being continually updated.
549 Ideally, in a coupled adjoint model melt sensitivities would be passed to the ocean ad-
550 joint model and ice-draft sensitivities to the ice adjoint model with the same frequency.
551 (In our study, ice-draft sensitivities were not calculated, but our framework could be eas-
552 ily modified to do so.) Moreover, if the ocean and ice models are not on the same grid
553 (as is the case with our ocean model and the ice-sheet model used by Goldberg et al. (2019)),
554 a coupled model would interpolate the melt rates to the ice-sheet grid. Strictly, the term
555 $(\nabla_{\mathbf{m}}V)^T$ in the definition of J_{gv} should be right-multiplied by the adjoint of this inter-
556 polation operator. This was not done in our calculation, rather the ice-sheet adjoint sen-
557 sitivity was interpolated to the ocean grid directly. Still, our results present a useful pre-
558 liminary assessment of the controls of ocean bathymetry on ice-sheet volume, and can
559 potentially inform more comprehensive assessments using coupled ice sheet-ocean mod-
560 els.

561 **5 Discussion and Conclusions**

562 In this study we have applied an algorithmic differentiation (AD) framework to an
563 ocean general circulation model in order to determine the sensitivity of ice-shelf melt rates
564 to ocean bathymetry. A similar framework of inferring bottom topography sensitivities
565 has been applied before (Losch & Heimbach, 2007), in a coarse-resolution global-scale
566 model. Here, we extend this computational framework to a regional domain that includes
567 circulation in sub-ice shelf cavities in order to assess the impact of uncertainty in bathymetry,
568 a quantity which cannot be measured under ice-shelves by ship-based methods, on melt
569 rates. Additionally, we have made technical improvements by avoiding the differentia-
570 tion by the AD tool of the Poisson solver for the implicit free surface and facilitating the
571 use of the tool in high performance computing environments (see supplementary mate-
572 rials, sections 1 and 2). We have done so using an open-source AD tool.

573 Results from both the idealized and realistic simulations show how bathymetry near
574 and underneath ice-shelves modulate melt-rates. Ocean-ward of an ice shelf, troughs lead-
575 ing to the ice front act as a guide for incoming warm ocean waters. Specifically, we show
576 that steepening the trough in front of the Dotson ice shelf would increase melting as a
577 result of increasing the geostrophic inflow. These results provide a complementary per-
578 spective to the observations and experimental results shown in Wählin et al. (2020).

579 Underneath ice shelves, it is well known that ridges or sills hinder the inflow of warm,
580 dense waters into cavities (Dutrieux et al., 2014; De Rydt et al., 2014; Slater et al., 2019;
581 Zhao et al., 2018). However, the spatial details of how these obstacles impact ice shelf
582 melting are in some instances counter-intuitive. For example, the sensitivities in our ide-
583 alised ISOMIP-bump experiment identified locations where *raising* the level of a sub-
584 ice-shelf ridge led to increased melt. These results were proven to be robust in forward
585 experiments, and they were mirrored in our Dotson-Crosson regional simulation. Thus,
586 while bathymetric obstacles do play a strong role, they do not simply serve as a “dam”
587 to hold back dense warm waters; rather, an obstacle’s impact on melt must be assessed
588 in the context of the broader ocean circulation and topographic steering of that circu-
589 lation.

590 When calculating sensitivities to bathymetry, the MITgcm adjoint is subject to non-
591 linearities and non-differentiable operators, and may over- or under-estimate response
592 to some perturbations (*cf.* Fig. 3(b)), particularly in response to large perturbations (Sec-
593 tion 4.4). More work is needed to determine under what conditions and scales the pre-
594 dicted melt response to bathymetric perturbations is valid. Nevertheless, our idealized
595 experiments suggest the adjoint is able to identify locations and regions where topog-
596 raphy “matters”. Losch & Heimbach (2007) reach a similar conclusion with their study.
597 They attribute this to low model resolution, though based on our idealised experiments
598 this limitation might apply to high-resolution studies as well.

599 Regardless, such experiments provide utility to observations of sub-shelf bathymetry
600 which seek to aid modelling of ice-ocean interactions. High-resolution studies of ice-shelf
601 bathymetry (for instance, through gravity analysis and seismic inversion) are possible,
602 but are very limited in scope. As our understanding of sub-shelf bathymetry evolves, our
603 adjoint-based method could be adapted to identify candidate locations where high res-
604 olution observational campaigns can be most impactful – for instance, by assessing the
605 potential information gain in important quantities of interest, as in Loose et al. (2020).
606 Additionally, patterns of spatial variability in sensitivity (such as that seen on the flank
607 of Dotson trough) could inform requirements for airborne gravity surveys (in terms of
608 aircraft speed and altitude) to ensure such variability is captured.

609 A major use of the MITgcm adjoint model is for improved assimilation of oceano-
610 graphic data (e.g., Wunsch & Heimbach, 2007; Wunsch et al., 2009). However, it is un-

611 likely that an adjoint ocean model can be used to estimate sub-ice shelf bathymetry by
612 assimilating spatial observations of melt rates, for two reasons. Firstly, as demonstrated
613 in our idealised and realistic experiments, there are extensive regions under ice shelves
614 where melt rates are not sensitive to bathymetry. Thus two very different bathymetry
615 products (such as the Millan and BedMachine datasets) could give very similar melt rates.
616 Secondly, sub-shelf circulation seems to “filter” the effects on melt rate, such that while
617 bathymetry has a strong impact on total melt, its effect on melt rate patterns may be
618 weaker – effectively limiting the information contained in spatially resolved melt patterns
619 (Gourmelen et al., 2017). It may be possible, nevertheless, to “fine tune” our knowledge
620 of bathymetry in regions that are known to strongly impact melt rates.

621 Our study was spatially limited in that only Crosson and Dotson ice shelves were
622 modelled – but it was also *temporally* limited, with time-invariant conditions represent-
623 ing far-field heat content and thermocline depths. In reality, the depth of CDW on the
624 Amundsen shelf and elsewhere in Antarctica varies both seasonally and interannually
625 (e.g., Thoma et al., 2008; Jenkins et al., 2016; Webber et al., 2017), and it is possible that
626 this variability could impact sensitivity of melt to bathymetry. Furthermore, our choice
627 of resolution and horizontal viscosity may have precluded resolution of turbulent eddies
628 which interact with bathymetry, affecting transport of heat to the ice-ocean interface.
629 Therefore, the results in Section 4 should be viewed as a preliminary exploration of bathy-
630 metric sensitivity of ice-shelf melt for Antarctic ice shelves. Our methodology must be
631 applied to simulations of ice-ocean interactions that are longer-term, more spatially ex-
632 tensive, and validated against observations of ice-shelf melt (Rignot et al., 2013; Gourme-
633 len et al., 2017; Jenkins et al., 2018) in order that the impacts of ocean bathymetry upon
634 ice-shelf melt can be fully evaluated.

635 The full potential of this work may be realised in fully coupled forward and adjoint
636 ocean-ice sheet calculations on decadal to century scales, in which ice sheet volume sen-
637 sitivities to ocean bathymetric uncertainties may be more comprehensively studied. To
638 do so will require tackling computational challenges along two main fronts. The first is
639 in terms of efficient, property-conserving strategies allowing century-scale coupled ice-
640 ocean simulations at resolutions that resolve important oceanographic phenomena, us-
641 ing codes that are adjointable. Some progress has already been made in this area through
642 decadal-scale synchronous coupling of the MITgcm ocean and land ice models (Jordan

643 et al., 2017; Goldberg et al., 2018), both of which have been differentiated by both TAF
644 and OpenAD.

645 The second front is in terms of the efficiency of the adjoint model relative to the
646 forward model. Adjoint models are extremely efficient in terms of sensitivity analyses,
647 providing ability to estimate sensitivity to tens or hundreds of thousands of input pa-
648 rameters simultaneously. However, model nonlinearities require that intermediate vari-
649 ables be stored or recomputed because of the time-reversed adjoint integration. As a re-
650 sult the adjoint run time is generally a multiple of the forward model. Certain AD tools
651 such as TAF have achieved multiples on the order of 3 to 6 – but this performance is a
652 result of extensive performance optimization of these tools in relation to the application
653 code, and this multiple can vary by an order of magnitude among any AD tool which
654 has not been similarly optimized, such as OpenAD. Therefore achieving performance in
655 the open-source domain that would make large-scale adjoint studies of coupled ice-ocean
656 dynamics feasible requires further close collaboration between domain scientists and de-
657 velopers of AD software.

658 **Acknowledgments and Code/Data Availability.**

659 D.G. was supported by NERC Standard Grants NE/M003590/1 and NE/T001607/1.
660 D.G. and M.M. were supported jointly by NERC-NSF ITGC Grant PROPHET. T.S.
661 and P.H. were supported in part by NSF grant #1750035 and JPL/Caltech subcontract
662 "ECCO: Understanding Sea Level, Ice, and Earths Climate". S.N. was supported by the
663 U.S. Department of Energy, Office of Science, under contract DE-AC02-06CH11357. MIT-
664 gcm code can be accessed publicly at mitgcm.org and OpenAD from <https://www.mcs.anl.gov/OpenAD>.
665 BedMachine data is available from <https://nsidc.org/data/nsidc-0756> . Output availabil-
666 ity information for Kimura et al. (2017) is given in their publication. All model output
667 used to produce figures for this manuscript is provided as supporting information.

668 **References**

- 669 Adcroft, A., Hill, C., & Marshall, J. (1997). Representation of topography by shaved
670 cells in a height coordinate ocean model. *Monthly Weather Review*, *125*(9), 2293-
671 2315. doi: 10.1175/1520-0493(1997)125
672 An, L., Rignot, E., Millan, R., Tinto, K., & Willis, J. (2019). Bathymetry of North-

- 673 west Greenland Using “Ocean Melting Greenland” (OMG) High-Resolution
674 Airborne Gravity and Other Data. *Remote Sens.*, 11(2). Retrieved from
675 <https://www.mdpi.com/2072-4292/11/2/131> doi: 10.3390/rs11020131
- 676 Arneborg, L., Wählin, A. K., Björk, G., Liljebldh, B., & Orsi, A. H. (2012,
677 Nov 25). Persistent inflow of warm water onto the central amundsen shelf. *Nature*
678 *Geoscience*, 5, 876–880. doi: 10.1038/ngeo1644
- 679 Aupy, G., Herrmann, J., Hovland, P., & Robert, Y. (2014, 04). Optimal multi-
680 stage algorithm for adjoint computation. *SIAM Journal on Scientific Computing*,
681 38. doi: 10.1137/15M1019222
- 682 Bamber, J. L., Westaway, R. M., Marzeion, B., & Wouters, B. (2018, jun). The
683 land ice contribution to sea level during the satellite era. *Environmental Research*
684 *Letters*, 13(6), 063008. doi: 10.1088/1748-9326/aac2f0
- 685 Bentley, C. R., Crary, A. P., Ostenso, N. A., & Thiel, E. C. (1960, January). Struc-
686 ture of West Antarctica. *Science*, 131(3394), 131–136.
- 687 Cochran, J. R., & Bell, R. E. (2012). Inversion of icebridge gravity data for con-
688 tinental shelf bathymetry beneath the larsen ice shelf, antarctica. *Journal of*
689 *Glaciology*, 58(209), 540–552. doi: 10.3189/2012JoG11J033
- 690 Dansereau, V., Heimbach, P., & Losch, M. (2014). Simulation of subice shelf melt
691 rates in a general circulation model: Velocity-dependent transfer and the role of
692 friction. *Journal of Geophysical Research: Oceans*, 119(3), 1765–1790. Retrieved
693 from <http://dx.doi.org/10.1002/2013JC008846> doi: 10.1002/2013JC008846
- 694 De Rydt, J., Holland, P. R., Dutrieux, P., & Jenkins, A. (2014). Geometric
695 and oceanographic controls on melting beneath pine island glacier. *Journal of*
696 *Geophysical Research: Oceans*, 119(4), 2420–2438. Retrieved from [http://](http://dx.doi.org/10.1002/2013JC009513)
697 dx.doi.org/10.1002/2013JC009513 doi: 10.1002/2013JC009513
- 698 Dutrieux, P., De Rydt, J., Jenkins, A., Holland, P., Ha, H., Lee, S., ... Schröder, M.
699 (2014). Strong sensitivity of pine island ice-shelf melting to climatic variability.
700 *Science*, 343(6167), 174–178. Retrieved from [http://science.sciencemag.org/](http://science.sciencemag.org/content/343/6167/174)
701 [content/343/6167/174](http://science.sciencemag.org/content/343/6167/174) doi: 10.1126/science.1244341
- 702 Dutrieux, P., Lee, C., Rainville, L., Gobat, J., Girton, J., Christianson, K., ... Mil-
703 lan, R. (2020). Seaglider and Float Observations Beneath Dotson Ice Shelf, West
704 Antarctica. In *Ocean sciences meeting abstracts*.
- 705 Errico, R. M. (1997). What is an adjoint model? *BAMS*, 78, 2577–2591.

- 706 Gerringa, L. J., Alderkamp, A.-C., Laan, P., Thur'oczy, C.-E., Baar, H. J. D., Mills,
707 M. M., ... Arrigo, K. R. (2012). Iron from melting glaciers fuels the phytoplank-
708 ton blooms in amundsen sea (southern ocean): Iron biogeochemistry. Deep Sea
709 Research Part II: Topical Studies in Oceanography, 71-76, 16 - 31. Retrieved from
710 <http://www.sciencedirect.com/science/article/pii/S0967064512000446>
711 doi: <https://doi.org/10.1016/j.dsr2.2012.03.007>
- 712 Giering, R., Kaminski, T., & Slawig, T. (2005, October). Generating efficient deriva-
713 tive code with TAF adjoint and tangent linear euler flow around an airfoil. Future
714 Gener. Comput. Syst., 21(8), 1345–1355. Retrieved from [http://dx.doi.org/10](http://dx.doi.org/10.1016/j.future.2004.11.003)
715 [.1016/j.future.2004.11.003](http://dx.doi.org/10.1016/j.future.2004.11.003) doi: 10.1016/j.future.2004.11.003
- 716 Giles, M. B., Corliss, G., Faure, C., Griewank, A., Hascoët, L., & Naumann, U.
717 (2002). On the iterative solution of adjoint equations. In Automatic differentiation
718 of algorithms: From simulation to optimization (pp. 145–151). New York, NY:
719 Springer New York. doi: 10.1007/978-1-4613-0075-5-16
- 720 Gille, S. T., Metzger, E. J., & Tokmakian, R. (2004, March). Seafloor topography
721 and ocean circulation. Oceanography, 17. Retrieved from [https://doi.org/10](https://doi.org/10.5670/oceanog.2004.66)
722 [.5670/oceanog.2004.66](https://doi.org/10.5670/oceanog.2004.66)
- 723 Goldberg, D., Gourmelen, N., Kimura, S., Millan, R., & Snow, K. (2019). How accu-
724 rately should we model ice shelf melt rates? Geophysical Research Letters, 46(1),
725 189-199. Retrieved from [https://agupubs.onlinelibrary.wiley.com/doi/abs/](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2018GL080383)
726 [10.1029/2018GL080383](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2018GL080383) doi: 10.1029/2018GL080383
- 727 Goldberg, D., & Heimbach, P. (2013). Parameter and state estimation with a time-
728 dependent adjoint marine ice sheet model. The Cryosphere, 7(6), 1659–1678. Re-
729 trieved from <http://www.the-cryosphere.net/7/1659/2013/> doi: 10.5194/tc-7
730 -1659-2013
- 731 Goldberg, D., Heimbach, P., Joughin, I., & Smith, B. (2015). Committed re-
732 treat of smith, pope, and kohler glaciers over the next 30 years inferred by
733 transient model calibration. The Cryosphere, 9(6), 2429–2446. Retrieved from
734 <https://www.the-cryosphere.net/9/2429/2015/> doi: 10.5194/tc-9-2429-2015
- 735 Goldberg, D., Snow, K., Holland, P., Jordan, J., Campin, J.-M., Heimbach, P., ...
736 Jenkins, A. (2018). Representing grounding line migration in synchronous cou-
737 pling between a marine ice sheet model and a z-coordinate ocean model. Ocean
738 Modelling, 125, 45 - 60. Retrieved from <http://www.sciencedirect.com/>

- 739 science/article/pii/S1463500318301021 doi: <https://doi.org/10.1016/>
740 j.ocemod.2018.03.005
- 741 Gourmelen, N., N., G. D., Kate, S., F., H. S., G., B. R., Satoshi, K., ... Jan, B. W.
742 (2017). Channelized melting drives thinning under a rapidly melting antarctic
743 ice shelf. *Geophysical Research Letters*, *44*(19), 9796-9804. Retrieved from
744 <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/2017GL074929>
745 doi: 10.1002/2017GL074929
- 746 Graham, J. A., Dinniman, M. S., & Klinck, J. M. (2016). Impact of model
747 resolution for on-shelf heat transport along the west antarctic peninsula.
748 *Journal of Geophysical Research: Oceans*, *121*(10), 7880-7897. Retrieved from
749 <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/2016JC011875>
750 doi: 10.1002/2016JC011875
- 751 Greene, C. A., Blankenship, D. D., Gwyther, D. E., Silvano, A., & van Wijk, E.
752 (2017). Wind causes totten ice shelf melt and acceleration. *Science Advances*,
753 *3*(11). Retrieved from [https://advances.sciencemag.org/content/3/11/](https://advances.sciencemag.org/content/3/11/e1701681)
754 [e1701681](https://advances.sciencemag.org/content/3/11/e1701681) doi: 10.1126/sciadv.1701681
- 755 Griewank, A., & Walther, A. (2000, March). Algorithm 799: Revolve: An im-
756 plementation of checkpointing for the reverse or adjoint mode of computa-
757 tional differentiation. *ACM Trans. Math. Softw.*, *26*(1), 19-45. Retrieved from
758 <http://doi.acm.org/10.1145/347837.347846> doi: 10.1145/347837.347846
- 759 Griewank, A., & Walther, A. (2008). *Evaluating derivatives. principles*
760 *and techniques of algorithmic differentiation*, vol. 19 of *frontiers in applied*
761 *mathematics* (2nd ed.). Philadelphia: SIAM.
- 762 Gwyther, D. E., Galton-Fenzi, B. K., Hunter, J. R., & Roberts, J. L. (2014). Sim-
763 ulated melt rates for the totten and dalton ice shelves. *Ocean Science*, *10*(3), 267-
764 279. Retrieved from <http://www.ocean-sci.net/10/267/2014/> doi: 10.5194/os-
765 -10-267-2014
- 766 Heimbach, P., Hill, C., & Giering, R. (2005). An efficient exact adjoint of the paral-
767 lel MIT general circulation model, generated via automatic differentiation. *Future*
768 *Generation Computer Systems*, *21*, 1356-1371.
- 769 Heimbach, P., & Losch, M. (2012). Adjoint sensitivities of sub-ice shelf melt rates to
770 ocean circulation under Pine Island Ice Shelf, West Antarctica. *Annals of Glaciol.*,
771 *54*, 59-69. doi: 10.3189/2012/AoG60A025

- 772 Heimbach, P., Wunsch, C., Ponte, R. M., Forget, G., Hill, C., & Utke, J. (2011).
 773 Timescales and regions of the sensitivity of atlantic meridional volume and
 774 heat transport: Toward observing system design. Deep Sea Research Part
 775 II: Topical Studies in Oceanography, 58(17), 1858 - 1879. Retrieved from
 776 <http://www.sciencedirect.com/science/article/pii/S0967064511000488>
 777 (Climate and the Atlantic Meridional Overturning Circulation) doi: [https://](https://doi.org/10.1016/j.dsr2.2010.10.065)
 778 doi.org/10.1016/j.dsr2.2010.10.065
- 779 Hellmer, H. H., Kauker, F., Timmermann, R., Determann, J., & Rae, J. (2012).
 780 Twenty-first-century warming of a large antarctic ice-shelf cavity by a redirected
 781 coastal current. Nature, 485(7397), 225-228. Retrieved from [https://doi.org/](https://doi.org/10.1038/nature11064)
 782 [10.1038/nature11064](https://doi.org/10.1038/nature11064) doi: 10.1038/nature11064
- 783 Holland, D. M., Hunter, J., Grosfeld, K., Hellmer, H., Jenkins, A., Morales
 784 Maqueda, M. A., ... Dinniman, M. (2003, December). The Ice Shelf - Ocean
 785 Model Intercomparison Project (ISOMIP). AGU Fall Meeting Abstracts, C41A-
 786 05.
- 787 Holland, D. M., Jacobs, S. S., & Jenkins, A. (2003). Modelling the ocean circulation
 788 beneath the Ross Ice Shelf. Antarctic Science, 15, 13-23.
- 789 Holland, D. M., & Jenkins, A. (1999). Modelling thermodynamic ice-ocean interac-
 790 tions at the base of an ice shelf. J. Phys. Ocean., 29, 1787-1800. doi: [https://doi](https://doi.org/10.1175/1520-0485(1999)029)
 791 [.org/10.1175/1520-0485\(1999\)029](https://doi.org/10.1175/1520-0485(1999)029)
- 792 Hoteit, I., Cornuelle, B., Köhl, A., & Stammer, D. (2005). Treating strong adjoint
 793 sensitivities in tropical eddy-permitting variational data assimilation. Quarterly
 794 Journal of the Royal Meteorological Society, 131(613), 3659-3682. Retrieved
 795 2019-10-21, from [https://rmets.onlinelibrary.wiley.com/doi/abs/10.1256/](https://rmets.onlinelibrary.wiley.com/doi/abs/10.1256/qj.05.97)
 796 [qj.05.97](https://doi.org/10.1256/qj.05.97) doi: 10.1256/qj.05.97
- 797 Hughes, C. W., & Killworth, P. D. (1995). Effects of bottom topography in the
 798 large-scale circulation of the southern ocean. Journal of Physical Oceanography,
 799 25(11), 2485-2497. Retrieved from [https://doi.org/10.1175/1520-0485\(1995\)](https://doi.org/10.1175/1520-0485(1995)025<2485:E0BTIT>2.0.CO;2)
 800 [025<2485:E0BTIT>2.0.CO;2](https://doi.org/10.1175/1520-0485(1995)025<2485:E0BTIT>2.0.CO;2) doi: 10.1175/1520-0485(1995)025<2485:E0BTIT>2.0
 801 [.CO;2](https://doi.org/10.1175/1520-0485(1995)025<2485:E0BTIT>2.0.CO;2)
- 802 Huppert, H. E., & Bryan, K. (1976). Topographically generated eddies. Deep
 803 Sea Research and Oceanographic Abstracts, 23(8), 655 - 679. Retrieved from
 804 <http://www.sciencedirect.com/science/article/pii/S0011747176800137>

- 805 doi: [https://doi.org/10.1016/S0011-7471\(76\)80013-7](https://doi.org/10.1016/S0011-7471(76)80013-7)
- 806 Jacobs, S. S., Hellmer, H., & Jenkins, A. (1996). Antarctic ice sheet melting in the
807 Southeast Pacific. *Geophys. Res. Lett.*, *23*, 957–960. doi: [https://doi.org/10.1175/
808 1520-0485\(1999\)029](https://doi.org/10.1175/1520-0485(1999)029)
- 809 Jacobs, S. S., Jenkins, A., Giulivi, C., & Dutrieux, P. (2011). Stronger ocean circu-
810 lation and increased melting under Pine Island Glacier ice shelf. *Nat. Geosci.* doi:
811 10.1038/NGEO1188
- 812 Jenkins, A. (2016). A simple model of the ice shelf-ocean boundary layer and
813 current. *Journal of Physical Oceanography*, *46*(6), 1785–1803. Retrieved from
814 <http://dx.doi.org/10.1175/JPO-D-15-0194.1> doi: 10.1175/JPO-D-15-0194.1
- 815 Jenkins, A., Dutrieux, P., Jacobs, S., Steig, E. J., Gudmundsson, H., Smith, J.,
816 & Heywood, K. (2016, December). Decadal ocean forcing and antarctic ice
817 sheet response: Lessons from the amundsen sea. *Oceanography*, *29*. doi:
818 <https://doi.org/10.5670/oceanog.2016.103>
- 819 Jenkins, A., Dutrieux, P., Jacobs, S. S., McPhail, S. D., Perrett, J. R., Webb, A. T.,
820 & White, D. (2010). Observations beneath Pine Island Glacier in West Antarctica
821 and implications for its retreat. *Nat. Geosci.*, *3*, 468–472.
- 822 Jenkins, A., & Holland, D. M. (2007). Melting of floating ice and sea level rise.
823 *Geophys. Res. Lett.*, *34*, L16609.
- 824 Jenkins, A., Shoosmith, D., Dutrieux, P., Jacobs, S., Kim, T. W., Le, S. H., ...
825 Stammerjohn, S. (2018). West antarctic ice sheet retreat in the amundsen
826 sea driven by decadal oceanic variability. *Nat. Geoscience*, *11*, 733–738. doi:
827 <https://doi.org/10.1038/s41561-018-0207-4DO>
- 828 Jenkins, A., Vaughan, D. G., Jacobs, S. S., Hellmer, H. H., & Keys, J. R. (1997).
829 Glaciological and oceanographic evidence of high melt rates beneath Pine Island
830 Glacier, West Antarctica. *Journal of Glaciology*, *43*(143), 114–121.
- 831 Jordan, J. R., Holland, P. R., Goldberg, D., Snow, K., Arthern, R., Campin, J.-M.,
832 ... Jenkins, A. (2017). Ocean-forced ice-shelf thinning in a synchronously coupled
833 ice-ocean model. *Journal of Geophysical Research: Oceans*, n/a–n/a. Retrieved
834 from <http://dx.doi.org/10.1002/2017JC013251> doi: 10.1002/2017JC013251
- 835 Joughin, I., Smith, B. E., & Medley, B. (2014). Marine ice sheet collapse potentially
836 under way for the Thwaites Glacier Basin, West Antarctica. *Science*, *344*(6185),
837 735–738. Retrieved from <http://www.sciencemag.org/content/344/6185/735>

- 838 .abstract doi: 10.1126/science.1249055
- 839 Kimura, S., Adrian, J., Heather, R., R., H. P., M., A. K., B., W. D., ... Pierre,
840 D. (2017). Oceanographic controls on the variability of ice-shelf basal melting
841 and circulation of glacial meltwater in the amundsen sea embayment, antarctica.
842 Journal of Geophysical Research: Oceans, 122(12), 10131-10155. Retrieved from
843 <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/2017JC012926>
844 doi: 10.1002/2017JC012926
- 845 Lilien, D. A., Joughin, I., Smith, B., & Shean, D. E. (2018). Changes in flow of
846 crosson and dotson ice shelves, west antarctica, in response to elevated melt. The
847 Cryosphere, 12(4), 1415–1431. Retrieved from [https://www.the-cryosphere](https://www.the-cryosphere.net/12/1415/2018/)
848 [.net/12/1415/2018/](https://www.the-cryosphere.net/12/1415/2018/) doi: 10.5194/tc-12-1415-2018
- 849 Loose, N., Heimbach, P., Pillar, H. R., & Nisancioglu, K. H. (2020). Quantifying dy-
850 namical proxy potential through shared adjustment physics in the north atlantic.
851 Journal of Geophysical Research: Oceans, 125(9), e2020JC016112. Retrieved from
852 <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020JC016112>
853 (e2020JC016112 10.1029/2020JC016112) doi: 10.1029/2020JC016112
- 854 Losch, M. (2008). Modeling ice shelf cavities in a z coordinate ocean general
855 circulation model. Journal of Geophysical Research: Oceans, 113(C8), n/a–
856 n/a. Retrieved from <http://dx.doi.org/10.1029/2007JC004368> doi:
857 10.1029/2007JC004368
- 858 Losch, M., & Heimbach, P. (2007). Adjoint sensitivity of an ocean general cir-
859 culation model to bottom topography. Journal of Physical Oceanography,
860 37(2), 377-393. Retrieved from <https://doi.org/10.1175/JPO3017.1> doi:
861 10.1175/JPO3017.1
- 862 Marshall, D. (1995). Influence of topography on the large-scale ocean circulation.
863 Journal of Physical Oceanography, 25(7), 1622-1635. Retrieved from [https://doi](https://doi.org/10.1175/1520-0485(1995)025<1622:IOTOTL>2.0.CO;2)
864 [.org/10.1175/1520-0485\(1995\)025<1622:IOTOTL>2.0.CO;2](https://doi.org/10.1175/1520-0485(1995)025<1622:IOTOTL>2.0.CO;2) doi: 10.1175/1520
865 -0485(1995)025<1622:IOTOTL>2.0.CO;2
- 866 Marshall, J., Hill, C., Perelman, L., & Adcroft, A. (1997). Hydrostatic, quasi-
867 hydrostatic, and nonhydrostatic ocean modeling. Journal of Geophysical Research:
868 Oceans, 102(C3), 5733–5752. Retrieved from [http://dx.doi.org/10.1029/](http://dx.doi.org/10.1029/96JC02776)
869 [96JC02776](http://dx.doi.org/10.1029/96JC02776) doi: 10.1029/96JC02776
- 870 Mathiot, P., Jenkins, A., Harris, C., & Madec, G. (2017). Explicit represen-

- 871 tation and parametrised impacts of under ice shelf seas in the z^* coordinate
 872 ocean model nemo 3.6. Geoscientific Model Development, 10(7), 2849–2874.
 873 Retrieved from <https://www.geosci-model-dev.net/10/2849/2017/> doi:
 874 10.5194/gmd-10-2849-2017
- 875 Miles, T., Lee, S. H., Wåhlin, A., Ha, H. K., Kim, T. W., Assmann, K. M., &
 876 Schofield, O. (2016). Glider observations of the Dotson Ice Shelf outflow. Deep Sea
 877 Research Part II: Topical Studies in Oceanography, 123, 16 - 29. Retrieved from
 878 <http://www.sciencedirect.com/science/article/pii/S096706451500301X>
 879 doi: <https://doi.org/10.1016/j.dsr2.2015.08.008>
- 880 Millan, R., Rignot, E., Bernier, V., Morlighem, M., & Dutrieux, P. (2017).
 881 Bathymetry of the Amundsen Sea Embayment sector of West Antarctica from
 882 Operation IceBridge gravity and other data. Geophysical Research Letters, 44(3),
 883 1360-1368. doi: 10.1002/2016GL072071
- 884 Morlighem, M., Rignot, E., Binder, T., Blankenship, D., Drews, R., & others,
 885 . (2020). Deep glacial troughs and stabilizing ridges unveiled beneath the
 886 margins of the antarctic ice sheet. Nature Geoscience, 13(2), 132–137. doi:
 887 10.1038/s41561-019-0510-8
- 888 Nitsche, F. O., Jacobs, S. S., Larter, R. D., & Gohl, K. (2007). Bathymetry of
 889 the amundsen sea continental shelf: Implications for geology, oceanography,
 890 and glaciology. Geochemistry, Geophysics, Geosystems, 8(10). Retrieved from
 891 <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2007GC001694>
 892 doi: 10.1029/2007GC001694
- 893 Padman, L., Costa, D. P., Bolmer, S. T., Goebel, M. E., Huckstadt, L. A., Jenkins,
 894 A., ... Shoosmith, D. R. (2010). Seals map bathymetry of the antarctic continen-
 895 tal shelf. Geophysical Research Letters, 37(21). doi: 10.1029/2010GL044921
- 896 Petty, A. A., Feltham, D. L., & Holland, P. R. (2013). Impact of Atmospheric
 897 Forcing on Antarctic Continental Shelf Water Masses. Journal of Physical
 898 Oceanography, 43(5), 920-940. Retrieved from [https://doi.org/10.1175/](https://doi.org/10.1175/JPO-D-12-0172.1)
 899 <https://doi.org/10.1175/JPO-D-12-0172.1> doi: 10.1175/JPO-D-12-0172.1
- 900 Pillar, H. R., Heimbach, P., Johnson, H. L., & Marshall, D. P. (2016, Febru-
 901 ary). Dynamical Attribution of Recent Variability in Atlantic Overturn-
 902 ing. Journal of Climate, 29(9), 3339–3352. Retrieved 2019-09-04, from
 903 <https://journals.ametsoc.org/doi/full/10.1175/JCLI-D-15-0727.1> doi:

904 10.1175/JCLI-D-15-0727.1

905 Pritchard, H. D., Ligtenberg, S. R. M., Fricker, H. A., Vaughan, D. G., van den
906 Broeke, M. R., & Padman, L. (2012, April). Antarctic ice-sheet loss driven by
907 basal melting of ice shelves. *Nature*, *484*(7395), 502–505.

908 Randall-Goodwin, E., Meredith, M. P., Jenkins, A., Yager, P. L., Sherrell, R. M.,
909 Abrahamsen, E. P., ... Stammerjohn, S. E. (2015). Freshwater distributions and
910 water mass structure in the Amundsen Sea Polynya region, Antarctica. *Elementa*,
911 *5*, 65. doi: <http://doi.org/10.12952/journal.elementa.000065>

912 Rignot, E., Jacobs, S., Mouginot, J., & Scheuchl, B. (2013). Ice-Shelf Melting
913 Around Antarctica. *Science*, *341*(6143), 266–270. Retrieved from [http://science](http://science.sciencemag.org/content/341/6143/266)
914 [.sciencemag.org/content/341/6143/266](http://science.sciencemag.org/content/341/6143/266) doi: 10.1126/science.1235798

915 Roberts, M. J., & Wood, R. A. (1997). Topographic sensitivity studies with a
916 bryan-cox-type ocean model. *Journal of Physical Oceanography*, *27*(5), 823-
917 836. Retrieved from [https://doi.org/10.1175/1520-0485\(1997\)027<0823:](https://doi.org/10.1175/1520-0485(1997)027<0823:TSSWAB>2.0.CO;2)
918 [TSSWAB>2.0.CO;2](https://doi.org/10.1175/1520-0485(1997)027<0823:TSSWAB>2.0.CO;2) doi: 10.1175/1520-0485(1997)027<0823:TSSWAB>2.0.CO;2

919 Rosier, S. H. R., Hofstede, C., Brisbourne, A. M., Hattermann, T., Nicholls, K. W.,
920 Davis, P. E. D., ... Corr, H. F. J. (2018). A new bathymetry for the southeast-
921 ern filchner-ronne ice shelf: Implications for modern oceanographic processes and
922 glacial history. *Journal of Geophysical Research: Oceans*, *123*(7), 4610-4623. doi:
923 10.1029/2018JC013982

924 Schodlok, M. P., Menemenlis, D., Rignot, E., & Studinger, M. (2012). Sensitivity
925 of the ice-shelf/ocean system to the sub-ice-shelf cavity shape measured by NASA
926 IceBridge in Pine Island Glacier, West Antarctica. *Annals of Glaciology*, *53*(60),
927 156–162.

928 Schoof, C. (2007). Marine ice sheet dynamics. Part I. The case of rapid sliding. *J.*
929 *Fluid Mech.*, *573*, 27–55.

930 Shepherd, A., Wingham, D. J., & Rignot, E. (2004). Warm ocean is eroding West
931 Antarctic Ice Sheet. *Geophys. Res. Lett.*, *31*, L23402.

932 Sirkes, Z., & Tziperman, E. (1997). Finite difference of adjoint or adjoint of finite
933 difference? *Monthly Weather Review*, *125*(12), 3373-3378. doi: 10.1175/1520
934 -0493(1997)

935 Slater, D. A., Felikson, D., Straneo, F., Goelzer, H., Little, C. M., Morlighem, M.,
936 ... Nowicki, S. (2019). 21st century ocean forcing of the greenland ice sheet for

- 937 modeling of sea level contribution. The Cryosphere Discussions, 2019, 1–34. Re-
 938 trieved from <https://www.the-cryosphere-discuss.net/tc-2019-222/> doi:
 939 10.5194/tc-2019-222
- 940 Smith, T., & Heimbach, P. (2019). Atmospheric Origins of Variability in the South
 941 Atlantic Meridional Overturning Circulation. Journal of Climate, 32(5), 1483–
 942 1500. Retrieved 2019-02-07, from [http://journals.ametsoc.org/doi/10.1175/](http://journals.ametsoc.org/doi/10.1175/JCLI-D-18-0311.1)
 943 [JCLI-D-18-0311.1](http://journals.ametsoc.org/doi/10.1175/JCLI-D-18-0311.1) doi: 10.1175/JCLI-D-18-0311.1
- 944 Thoma, M., Jenkins, A., Holland, D. M., & Jacobs, S. S. (2008). Modelling Circum-
 945 polar Deep Water intrusions on the Amundsen Sea continental shelf, Antarctica.
 946 Geophys. Res. Lett., 35. doi: 10.1029/2008GL034939
- 947 Thomas, R. H. (1979). The dynamics of marine ice sheets. Journal of Glaciology, 24,
 948 167–177.
- 949 Thomas, R. H., & Bentley, C. R. (1978). A model for the Holocene retreat of the
 950 West Antarctic Ice Sheet. Quaternary Research, 10, 150–170.
- 951 Thompson, A. F., Stewart, A. L., Spence, P., & Heywood, K. J. (2018, December).
 952 The Antarctic Slope Current in a Changing Climate. Reviews of Geophysics,
 953 56(4), 741–770.
- 954 Tinto, K. J., & Bell, R. E. (2011). Progressive unpinning of thwaites glacier
 955 from newly identified offshore ridge: Constraints from aerogravity. Geophysical
 956 Research Letters, 38(20), L20503. Retrieved from [http://dx.doi.org/10.1029/](http://dx.doi.org/10.1029/2011GL049026)
 957 [2011GL049026](http://dx.doi.org/10.1029/2011GL049026) doi: 10.1029/2011GL049026
- 958 Utke, J., Naumann, U., Fagan, M., Tallent, N., Strout, M., Heimbach, P., ... Wun-
 959 sch, C. (2008). OpenAD/F: A modular open source tool for automatic differentia-
 960 tion of Fortran codes. ACM Transactions on Mathematical Software, 34.
- 961 Wählin, A. K., Steiger, N., Darelius, E., Assmann, K. M., Glessmer, M. S., Ha,
 962 H. K., ... Viboud, S. (2020, February). Ice front blocking of ocean heat trans-
 963 port to an Antarctic ice shelf. Nature, 578(7796), 568–571. Retrieved 2020-02-28,
 964 from <http://www.nature.com/articles/s41586-020-2014-5> (Number: 7796
 965 Publisher: Nature Publishing Group) doi: 10.1038/s41586-020-2014-5
- 966 Walker, D. P., Jenkins, A., Assmann, K., Shoosmith, D., & Brandon, M. (2013).
 967 Oceanographic observations at the shelf break of the Amundsen Sea, Antarctica.
 968 Journal of Geophysical Research: Oceans, 118(6), 2906-2918. Retrieved from
 969 <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/jgrc.20212>

970 doi: 10.1002/jgrc.20212

971 Webber, B., Heywood, K., Stevens, D. P., Dutrieux, P., Abrahamsen, E. P., Jenk-
 972 ins, A., ... Kim, T. W. (2017, February). Mechanisms driving variability in the
 973 ocean forcing of Pine Island Glacier. Nature Communications, 8, 14507. doi:
 974 10.1038/ncomms14507

975 Wei, W., Blankenship, D. D., Greenbaum, J. S., Gourmelen, N., Dow, C. F., Richter,
 976 T. G., ... Assmann, K. M. (2019). Getz ice shelf melt enhanced by freshwater
 977 discharge from beneath the west antarctic ice sheet. The Cryosphere Discussions,
 978 2019, 1–16. Retrieved from [https://www.the-cryosphere-discuss.net/
 979 tc-2019-170/](https://www.the-cryosphere-discuss.net/tc-2019-170/) doi: 10.5194/tc-2019-170

980 Wunsch, C. (1996). The ocean circulation inverse problem. New York: Cambridge
 981 University Press.

982 Wunsch, C., & Heimbach, P. (2007). Practical global ocean state estimation.
 983 Physica D, 230, 197–208.

984 Wunsch, C., Ponte, R., Heimbach, P., & Fukumori, I. (2009). The global general
 985 circulation of the ocean estimated by the ecco-consortium. Oceanography, 22, 88-
 986 103.

987 Yager, P. L., Sherrell, R. M., Stammerjohn, S. E., Alderkamp, A.-C., Schofield, O.,
 988 Abrahamsen, E. P., ... Wilson, S. (2012, September). Aspire: The amundsen
 989 sea polynya international research expedition. Oceanography, 25. Retrieved from
 990 <https://doi.org/10.5670/oceanog.2012.73>

991 Zhang, X., Thompson, A. F., Flexas, M. M., Roquet, F., & Bornemann, H.
 992 (2016). Circulation and meltwater distribution in the bellingshausen sea: From
 993 shelf break to coast. Geophysical Research Letters, 43(12), 6402-6409. doi:
 994 10.1002/2016GL068998

995 Zhao, K. X., Stewart, A. L., & McWilliams, J. C. (2018, November). Sill-Influenced
 996 Exchange Flows in Ice Shelf Cavities. Journal of Physical Oceanography, 49(1),
 997 163–191. Retrieved 2019-06-05, from [https://journals.ametsoc.org/doi/full/
 998 10.1175/JPO-D-18-0076.1](https://journals.ametsoc.org/doi/full/10.1175/JPO-D-18-0076.1) doi: 10.1175/JPO-D-18-0076.1

999
 1000

The submitted manuscript has been created by UChicago Argonne, LLC, Operator of Argonne National Laboratory ('Argonne'). Argonne, a U.S. Department of Energy Office of Science laboratory, is operated under Contract No. DE-AC02-06CH11357. The U.S. Government retains for itself, and others acting on its behalf, a paid-up nonexclusive, irrevocable worldwide license in said article to reproduce, prepare derivative works, distribute copies to the public, and perform publicly and display publicly, by or on behalf of the Government. The Department of Energy will provide public access to these results of federally sponsored research in accordance with the DOE Public Access Plan. <http://energy.gov/downloads/doe-public-access-plan>.

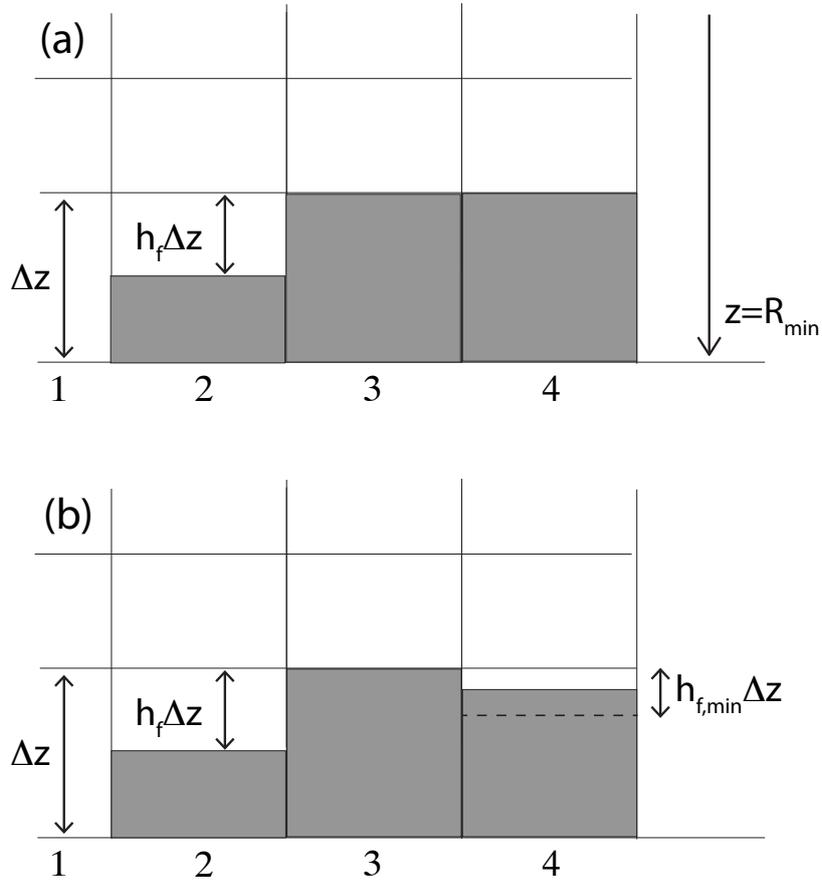


Figure 1. (a) A schematic (adapted from <http://mitgcm.org/>) of the representation of bottom topography in MITgcm. The white regions within cells contain fluid. In column 1, all cells are fluid-filled and the bathymetry is R_{\min} . The bottom cells of Columns 3 and 4 are non-fluid-containing, and in these columns the bottom elevation is $R_{\min} + \Delta z$. In Column 2, the bottom cell is a partial cell, and bathymetry is $R_{\min} + (1 - h_f)\Delta z$. The interface between the bottom cells of Column 1 and Column 2 has height $h_f \Delta z$, and there is no interface between the bottom cell of Column 2 with any cell in Column 3. (b) A perturbation to bathymetry is made, indicated by gray shading in to bottom cell of Column 4. Depending on the size of the perturbation, ocean model initialisation may lower bathymetry further so that the liquid-containing portion of the bottom cell is $h_{f,\min} \Delta z$; or it may restore bathymetry to that of (a).

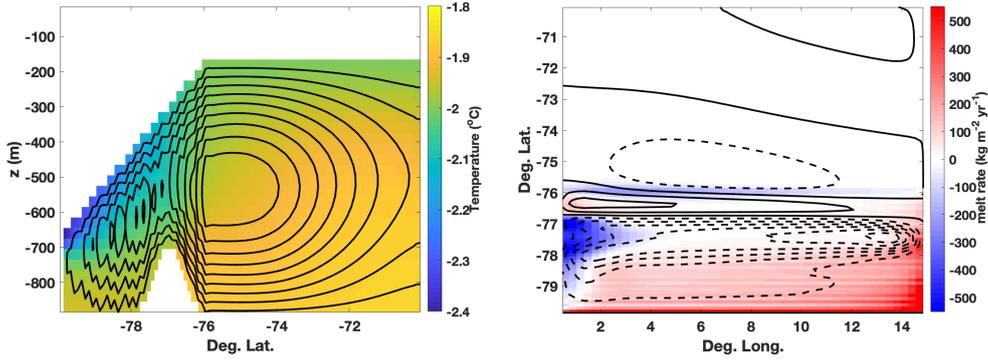


Figure 2. (left) Zonally averaged temperature (shading) and overturning stream function (contours, spacing 0.01 Sv) in the modified ISOMIP experiment. The profile of the “ridge” is apparent between -78° and -76° Latitude. (right) Melt rate at the termination of the experiment (shading; negative values indicate accretion) and depth-integrated stream function (contours, spacing 0.05 Sv; dashed lines where negative).

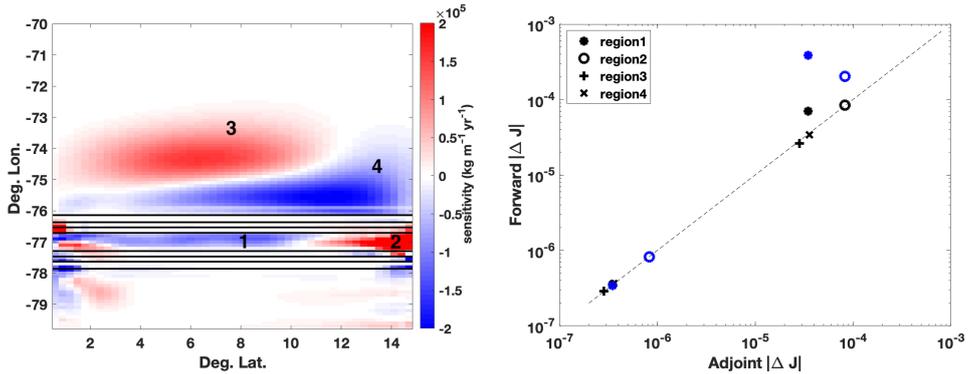


Figure 3. (left) Domain bathymetry (contours; 50m isolines) and sensitivity of spatially-integrated melt at model termination to bathymetry (shading); value of sensitivity in a cell indicates gradient of melt with respect to elevation in the cell, where positive (negative) values indicate regions where raising (lowering) the bottom will increase melt. (right) Comparison of perturbed objective function (“Forward” $|\Delta J|$, in Gt/a melt) with value predicted by linearized sensitivities (“Adjoint” $|\Delta J|$), as described in Section 3.2. Blue markers indicate negative perturbations while black markers indicate positive ones. Small values (less than 10^{-6} Gt/a) indicate perturbations scaled by 0.1m and large values (greater than 10^{-5} Gt/a) indicate perturbations scaled by 10m. Though the *sign* of the observed ΔJ is not given, it is in all cases the same as the prediction.

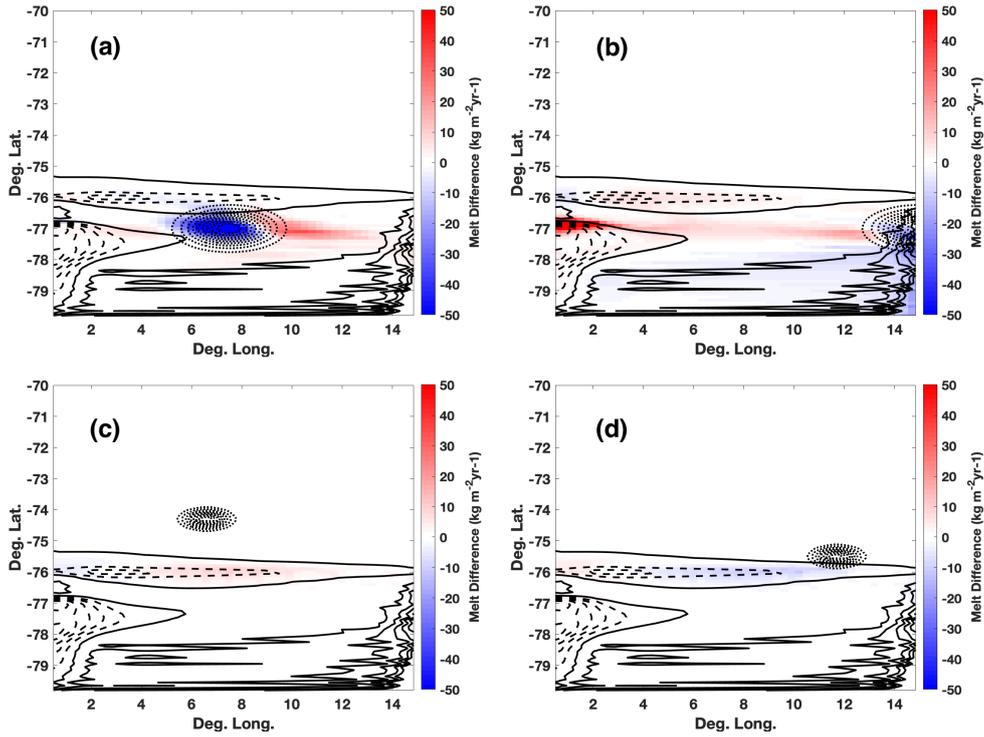


Figure 4. Perturbed beds (dotted contours) and corresponding perturbed melt rates (shading) in different regions of high sensitivity in Fig. 3. (a) through (d) correspond to finite perturbations in locations (1) through (4) in Fig. 3(a), respectively. Bathymetric perturbations plotted with $\delta R=10$ (Eqn. 3) and 1m isolines. Isolines of unperturbed melt rates are also shown (solid where positive, dashed where negative; $100 \text{ kg m}^{-2} \text{ yr}^{-1}$ spacing).

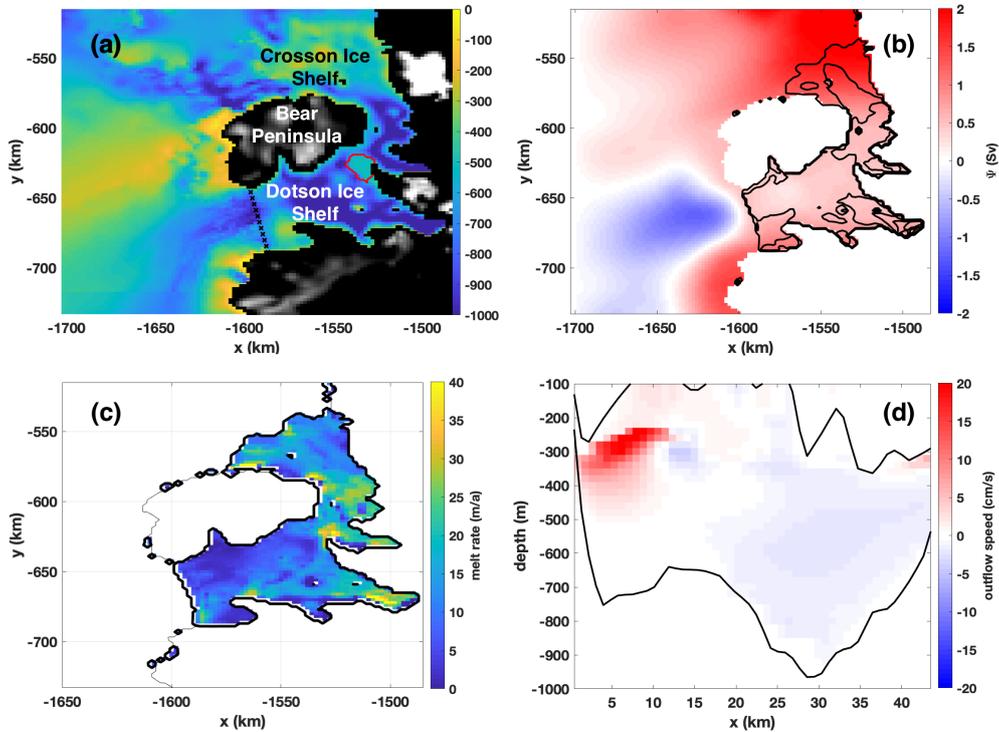


Figure 5. (a) The bathymetry of Millan et al. (2017), used in our adjoint experiment. Black and white shading indicates topography above sea level. X and Y coordinates refer to a Polar Stereographic projection. The cross marks across Dotson ice shelf front indicate the location of the velocity profile in (d), where the bottom edge of the transect corresponds to the left edge of (d). The red contour near the junction of Dotson and Crossson ice shelves indicates where bathymetry has been modified from Millan et al. (2017) as discussed in Section 4.1. (b) The barotropic stream function corresponding to the initial steady state of the ocean model (shading), and ice-shelf topography (contours, 150 m spacing). (c) Under-ice shelf melt rate corresponding to the steady state. (d) Outflow at the opening to the Dotson Ice Shelf cavity cf. Randall-Goodwin et al. (2015), their Figure 7(a)).

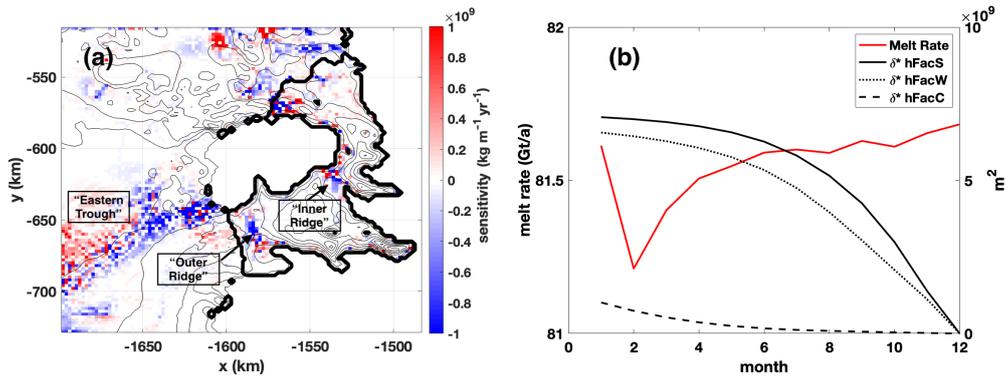


Figure 6. (a) Sensitivity of total (area-integrated) melt to bathymetry in Dotson-Crosson experiment (shading); interpretation is as in Fig. 3(a). Bathymetry is given by thin black contours (200 m spacing) and the boundary of the ice shelf by thick contours. Labels indicate regions discussed in Section 4.2. (b) Time series of melt volume and bathymetric factor sensitivities in our simulation of Dotson and Crosson ice shelves. The bathymetric factors h_f , h_f^s and h_f^w determine the proportion of the bottom cell that is fluid filled, in the center, southern face and western face, respectively. Note sensitivity fields computed from the adjoint model evolve backward in time.

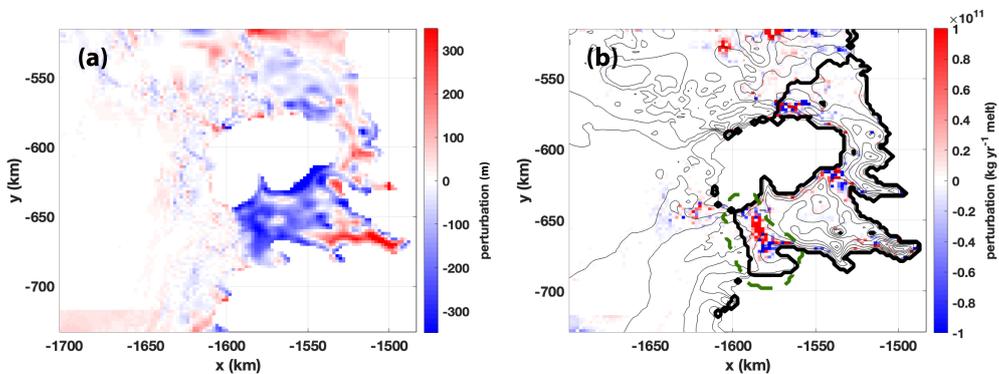


Figure 7. (a) Difference between BedMachine bathymetry and Millan bathymetry within the ocean model domain. The rectangular region in the bottom left of the figure is due to the Millan data set not extending to the edge of the domain. (b) The product of this difference and the sensitivity of melt with respect to bathymetry. The dashed contour indicates the region in which Millan bathymetry is replaced by BedMachine bathymetry in the perturbation experiment described in Section 4.4.

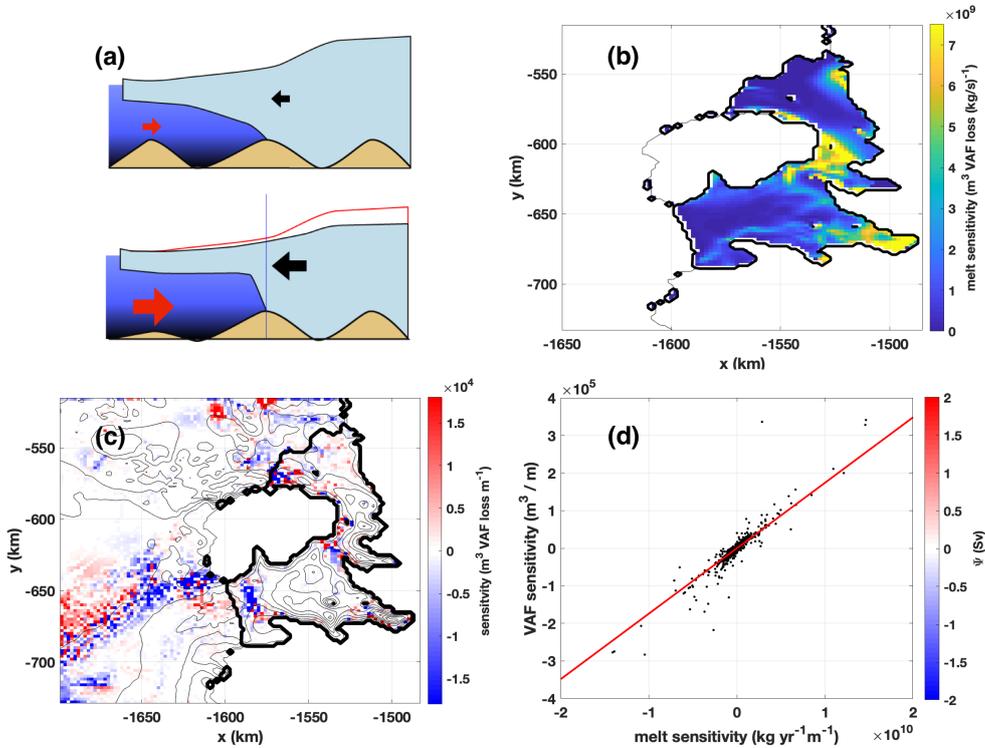


Figure 8. (a) A cartoon illustration of a potential pathway of influence from bed elevation to grounded ice volume. A lowering of bathymetry in the bottom panel relative to the top allows increased ocean heat flux (red arrows) toward the ice-shelf base, driving melting and thinning. The loss of ice-shelf buttressing causes increased ice volume flux across the grounding line (black arrows), and drawdown of grounded ice. “Grounded ice volume” refers only to the loss of ice upstream of the grounding line, i.e. to the right of the thin vertical blue line; the direct contribution to sea levels from loss of ice-shelf volume is negligible. (b) Sensitivity of grounded ice volume to ice-shelf melt (adapted from Goldberg et al. (2019), their Fig. 3(b)). (c) Sensitivity of the objective function given by Eqn. (6) to bathymetry. (d) Cell-by-cell correspondence of grounded ice volume sensitivity to melt-rate sensitivity.