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# Evaluation of ocean surface waves along the coastal area of the Sea of Okhotsk during winter

S. Iwasaki<sup>1</sup> and J. Otsuka<sup>1</sup>

<sup>1</sup>Civil Engineering Research Institute for Cold Region, 1-3-1-34 Toyohira, Sapporo 062-8602, Japan.

Corresponding author: Shinsuke Iwasaki ([iwasaki-s@ceri.go.jp](mailto:iwasaki-s@ceri.go.jp))

## Key Points:

- Six wave-ice parameterization models are evaluated using the buoy observation in the Sea of Okhotsk.
- The empirical model in which the attenuation rate depends on the frequency is found to be the most stable.
- Simulation with sea ice significantly improved the bias of wave fields in the coastal area compared to the simulation without sea ice.

**25 Abstract**

26 Ocean surface waves tend to be attenuated on interaction with sea ice. In this study, six sea ice  
27 models were implemented in the third-generation wave model WAVEWATCH III<sup>®</sup> (WW3) to  
28 estimate wave attenuation by sea ice. The models were evaluated using buoy observations in the  
29 coastal area of the Sea of Okhotsk (SO). Additionally, the impact of sea ice on wave fields was  
30 demonstrated by model experiments with and without the utilization of sea ice. As a result, one of  
31 the empirical models strongly agrees with the buoy observation. The simulation with sea ice  
32 drastically improved the bias of wave fields in coastal areas compared to simulation without sea  
33 ice. Moreover, the impact of sea ice reached more than 1 m (3 s) for the monthly significant wave  
34 height (period). These results suggest that the effect of sea ice on wave calculation is essential in  
35 the SO.

**36 Plain Language Summary**

37 It is postulated that sea ice is decreasing in the Sea of Okhotsk (SO) due to the effects of global  
38 warming. It is a matter of great concern that the ocean surface wave of the SO will increase, owing  
39 to the decrease in sea ice. This study is a first-cut analysis of the evaluation of wave calculation  
40 and the effect of sea ice on waves in the SO.

**41 1 Introduction**

42 The Sea of Okhotsk (SO) is a marginal ice zone (defined as the region of an ice cover that  
43 is affected by waves and swell penetrating into the ice from the open ocean) and is the  
44 southernmost sea with a sizeable seasonal ice cover in the Northern Hemisphere. Accurate  
45 calculation of ocean surface waves in the SO is important for ensuring safe shipping routes and  
46 identifying hazardous areas. In addition to its social importance, ocean waves in sea ice are a part  
47 of the interaction between sea ice, the ocean, and the atmosphere, and is essential to understand  
48 climate change. In winter, sea ice rapidly extends southeastward from November to March, and  
49 thereafter it reduces (Figure 1a–g). Sea ice suppresses the wave-wind interaction by reducing fetch.  
50 It also modifies the wave dispersion relation, and the wave energy is attenuated through a  
51 conservative scattering and non-conservative dissipation phenomenon (Squire, 2020). Although  
52 the sea ice extent in the SO has large interannual variability, its maximum value has been reported  
53 to decrease at a rate of 3.9 %/decade on the Japan Meteorological Agency (JMA) website

54 ([https://www.data.jma.go.jp/gmd/kaiyou/english/seaice\\_okhotsk/series\\_okhotsk\\_e.html](https://www.data.jma.go.jp/gmd/kaiyou/english/seaice_okhotsk/series_okhotsk_e.html)).

55 Therefore, it is of concern that a decrease in sea ice in the SO will result in an increase in ocean  
56 surface waves in the future.

57 WAVEWATCH III<sup>®</sup> (WW3; WAVEWATCH<sup>®</sup> Development Group, 2019), one of the  
58 most widely used third-generation spectral wave models based on the radiative transfer equation  
59 for global and regional wave forecasts, has implemented several parameterizations for wave-ice  
60 interaction. In deep water, when currents are absent, the evaluation of wind-generated ocean waves  
61 is governed by:

$$62 \quad \frac{\partial N}{\partial t} + \nabla \cdot C_g N = \frac{S}{\sigma}, \quad (1)$$

63 where  $N=E/\sigma$  is the wave action density spectrum, which is a function of wave number or radian  
64 frequency( $k$  or  $\sigma$ ), direction( $\theta$ ), space( $x, y$ ), and time( $t$ ),  $E$  is the wave energy spectral density,  
65 and  $C_g$  is the group velocity. For ice-covered region, the sum of the source term on the right-hand  
66 side of Eq. (1) is defined as follows:

$$67 \quad S = (1 - C_i)(S_{in} + S_{ds}) + S_{nl} + C_i S_{ice}, \quad (2)$$

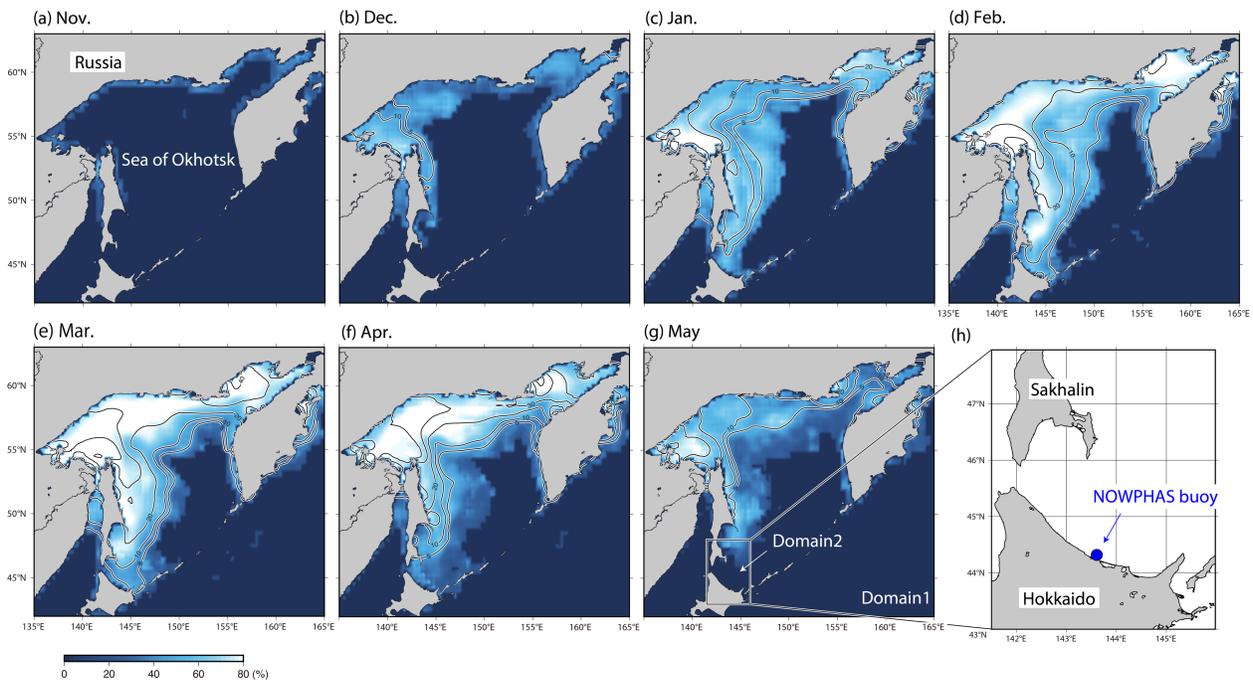
68 where  $S_{in}$  is the input term by wind,  $S_{ds}$  is the dissipation term induced by wave breaking,  $S_{nl}$  is  
69 the nonlinear interaction term among spectral components,  $S_{ice}$  is the wave-ice interaction term,  
70 and  $C_i$  is the ice concentration. Both wind input and dissipation terms ( $S_{in}$  and  $S_{ds}$ ) are scaled by  
71 the open water fraction( $1 - C_i$ ), whereas  $S_{ice}$  is scaled by the ice concentration. The effects of ice  
72 on ocean waves can be presented as a complex wavenumber  $k = k_r + ik_i$ , with the real part  $k_r$   
73 representing the physical wave number related to the wave length and propagation speeds,  
74 producing effects analogous to shoaling and refraction by bathymetry, and the imaginary part  $k_i$   
75 representing the exponential attenuation coefficient  $k_i = k_i(x, y, t, \sigma)$  which depends on the  
76 location, time, and radian frequency.  $k_i$  is introduced in the WW3 model as:

$$77 \quad \frac{S_{ice}}{E} = -C_g \alpha = -2C_g k_i, \quad (3)$$

78 Here,  $\alpha$  is the exponential attenuation rate for wave energy, which is twice that of the amplitude  
79 ( $\alpha = 2k_i$ ). The above equation ( Eq. 3) is used to calculate the dissipation by ice in WW3, denoted  
80 as IC1–5 (except for IC0).

81 Recently, studies have compared and evaluated some wave–ice parameterization models  
82 of the WW3 using field observations in the Arctic Sea, in regions such as the Barents Sea (Liu et

83 al., 2020), Chukchi Sea (Nose et al., 2020), and Beaufort Sea (Cheng et al., 2020). Although, sea  
 84 ice can be expected to have a significant impact on the wave fields, no studies have evaluated the  
 85 effect of sea ice on the wave field in the SO. This study evaluates the wave fields derived from six  
 86 wave–ice parameterization models (IC0–5 in WW3) using the Nationwide Ocean Wave  
 87 Information Network for Ports and Harbours (NOWPHAS) buoy observations (see Text S2 and  
 88 Figure 1h). Moreover, the impact of sea ice on wave fields using model simulations with and  
 89 without sea ice were also clarified.



90

91 **Figure 1.** Monthly ice concentration (color) and ice thickness (contour) from November to May  
 92 during 2008–2010 incorporating two model domains. (a–g) represents the ice concentration and  
 93 ice thickness derived from NOAA OI SST V2 and CFSR, respectively. CFSR ice thickness (cm)  
 94 were smoothed with a two-dimensional boxcar filter with a width of 50 km. (h) The blue dot shows  
 95 the NOWPHAS buoy location.

## 96 2 Model design

97 Two model domains were created using a nesting process, for a horizontal resolution of  
 98  $0.25^\circ$  (domain 1) and  $0.08^\circ$  (domain 2) (Figure 1g). The outer domain (domain 1) covers the entire  
 99 SO ( $42^\circ$ – $63^\circ$ N,  $135^\circ$ – $165^\circ$ E). The inner domain (domain 2) was used for the validation of wave  
 100 fields in the coastal area ( $43^\circ$ – $48^\circ$ N,  $141.5^\circ$ – $146^\circ$ E). The directional resolution was  $10^\circ$ , and the

101 frequency space was 0.035–1.1 Hz, which was logarithmically discretized into 30 increments.  
102 GEBCO2020 was used to provide the bottom topography and coastlines.

103 The simulation of domain 1 was driven incorporating 6-hourly surface wind data from the  
104 Japanese 55-year Reanalysis (JRA55) (Kobayashi et al., 2015) from the JMA. This product is  
105 approximately 55 km in latitude and longitude. In addition, the wind data for domain 2 were  
106 obtained from JRA55’s dynamic regional downscaling product (DSJRA55) (Kayaba et al., 2016)  
107 developed by JMA, in which the product has a spatial resolution of 5 km and a temporal resolution  
108 of 1 h. Daily ice concentration was obtained from NOAA Optimum Interpolation (OI) sea surface  
109 temperature (SST) version 2 high-resolution dataset with a  $0.25^\circ \times 0.25^\circ$  spatial grid (Reynolds et  
110 al. 2007). Ice thickness was incorporated from the Climate Forecast System Reanalysis (CFSR)  
111 produced by NCEP (Saha et al., 2010). The thickness product has a spatial resolution of  $0.25^\circ$  at  
112 the equator, extending to a global  $0.5^\circ$  beyond the tropics, with a temporal resolution of 6 h. The  
113 wind, ice concentration, and thickness data were linearly interpolated to the same spatial grid in  
114 the wave simulation of both the domains.

115 In this study, six models for  $S_{ice}$ , IC0, IC1, IC2, IC3, IC4, and IC5 were used. Only IC4 is  
116 different from the other models and provides seven empirical formulas denoted as IC4M1–M7  
117 (see Text S1). In addition, in order to investigate the impact of sea ice on the wave field, a  
118 simulation without incorporating ice concentration was conducted. Hereinafter, the model results  
119 without ice concentration are denoted as “Non-ICE”. Although IC4M5 and IC4M6 both provide a  
120 step function in the frequency space, IC4M6 has more steps than IC4M5. Therefore, IC4M5 was  
121 excluded from validation in this study. A simple diffusive scattering model (denoted as IS1 in  
122 WW3) was used for these simulations. Another scattering model (denoted as IS2) was  
123 implemented in WW3. However, the difference between the scattering models (i.e., IS1 and IS2)  
124 was small compared to the difference between the dissipation models (IC0–IC5) (not shown). For  
125 terms  $S_{in}$  and  $S_{ds}$ , we used both ST4 (Ardhuin et al., 2010; Rascle & Ardhuin, 2013) and ST6  
126 (Rogers et al., 2012; Zieger et al., 2015; Liu et al., 2019). All simulations were performed over a  
127 three-year period from 2008 to 2010. The significant wave height ( $H_s$ ) and mean wave period  
128 ( $T_{m01}$ ) were both saved every hour during the computation period. To obtain the modeled value at  
129 the buoy position, we linearly interpolated the fields to the buoy position using the surrounding

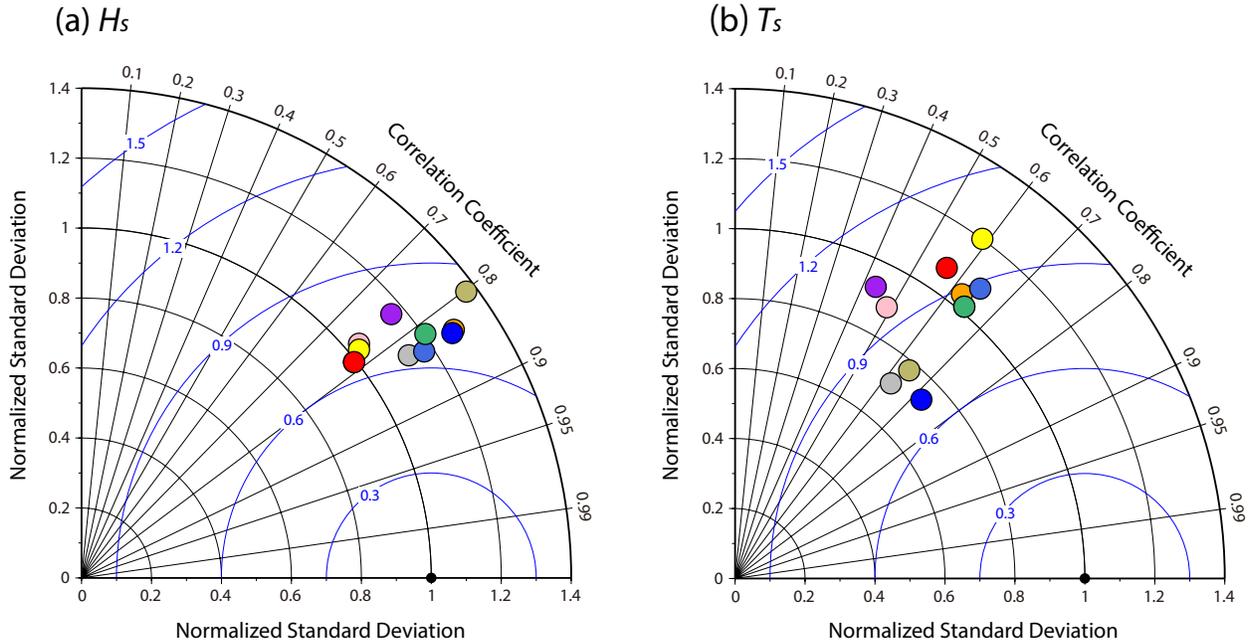
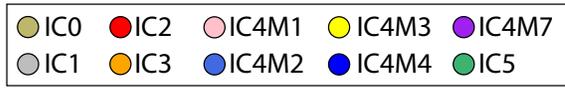
130 four grid values from domain 2. The significant wave period ( $T_s$ ) of the model simulation was  
131 derived using the following equation:  $T_s = 1.2T_{m01}$  (Goda, 2010).

### 132 **3 Results**

#### 133 3.1 Validation with buoy

134 To visualize the standard deviation (STD), root mean square error (RMSE), and correlation  
135 coefficient between the model simulations and NOWPHAS buoy, Figure 2 displays Taylor  
136 diagrams between the two fields (Taylor, 2001). In addition, Table 1 lists the statistical values  
137 between the model simulation and buoy observations for  $H_s$  and  $T_s$ . Here, IC4M2 is the simulation  
138 result of IC4M6H2 as this result demonstrated relatively better accuracy (see Table S3). In addition,  
139 the results of IC4M6 are not presented here as IC4M6 can be almost reproduced by the binomial  
140 fitting of IC4M2 (see Tables S3 and S4). In the present study, we utilized values only when the  
141 ice concentration in the coastal area ( $44^\circ$ – $46^\circ$ N,  $142.5^\circ$ – $145.5^\circ$ E) around the buoy was 10% or  
142 more (except in Figures 3–5). The number of validation data points were 3277. For  $H_s$ , all model  
143 simulations indicate a correlation coefficient greater than 0.75, a normalized STD between 0.99  
144 and 1.4, and a normalized RMSE and RMSE of less than 0.8 and 0.5 m, respectively (Figure 2a  
145 and Table 1). The bias for all  $H_s$  simulation was within  $\pm 0.3$  m except for IC0 (Table 1). The  
146 RMSE and the correlation coefficients of IC1 and IC4M2 were 0.4 m and 0.83, respectively, which  
147 were better than those of other simulations (Table 1), although a normalized STD of both  
148 simulations slightly overestimates as presented in Figure 2a. In contrast, the bias, normalized  
149 RMSE, and RMSE of IC0 were 0.47, 0.82, and 0.51 m, respectively, which were poorly estimated  
150 as compared with other simulations Figure. 2a and Table 1). Overall, for  $T_s$ , all simulations  
151 provided corresponding correlation coefficients of less than 0.73, which was relatively worse than  
152 those of  $H_s$  (Figure. 2 and Table 1). In addition, the differences in the statistical values between  
153 simulations were large compared to those of  $H_s$  (Figure 2 and Table 1). A normalized STD for IC0,  
154 IC1, and IC4M4 was less than 0.8, which tends to be underestimated (Figure 2b). Moreover,  
155 IC4M1 and IC4M7 were poorly simulated, as the correlation coefficients in both simulations were  
156 less than 0.5 (Table 1). In contrast, IC3, IC4M2, and IC5 were simulated with least number of  
157 errors and indicated a normalized STD from 1 to 1.1, and a normalized RMSE (RMSE) of less

158 than approximately 0.9 (2 s) (Figure 2b and Table 1). In particular, the bias for IC4M2 was 0.02 s,  
 159 smaller than those of IC3 and IC5 (Table 1).



160

161 **Figure 2.** Taylor diagram summarizing the statistical comparison between the NOWPHAS buoy  
 162 observation and the model simulations with ST6: (a)  $H_s$  and (b)  $T_s$ . The source terms of  $S_{ice}$  are  
 163 represented by the different colored-markers in legend in the upper region of the panel. The black  
 164 circle at the bottom indicates the buoy observation. The blue colored contour with an interval of  
 165 0.3 denotes the RMSE between the simulations and observations. The RMSE and standard  
 166 deviations have been normalized by the observed standard deviation. The correlation coefficients  
 167 between both the fields are shown by the azimuthal position of the simulation field.

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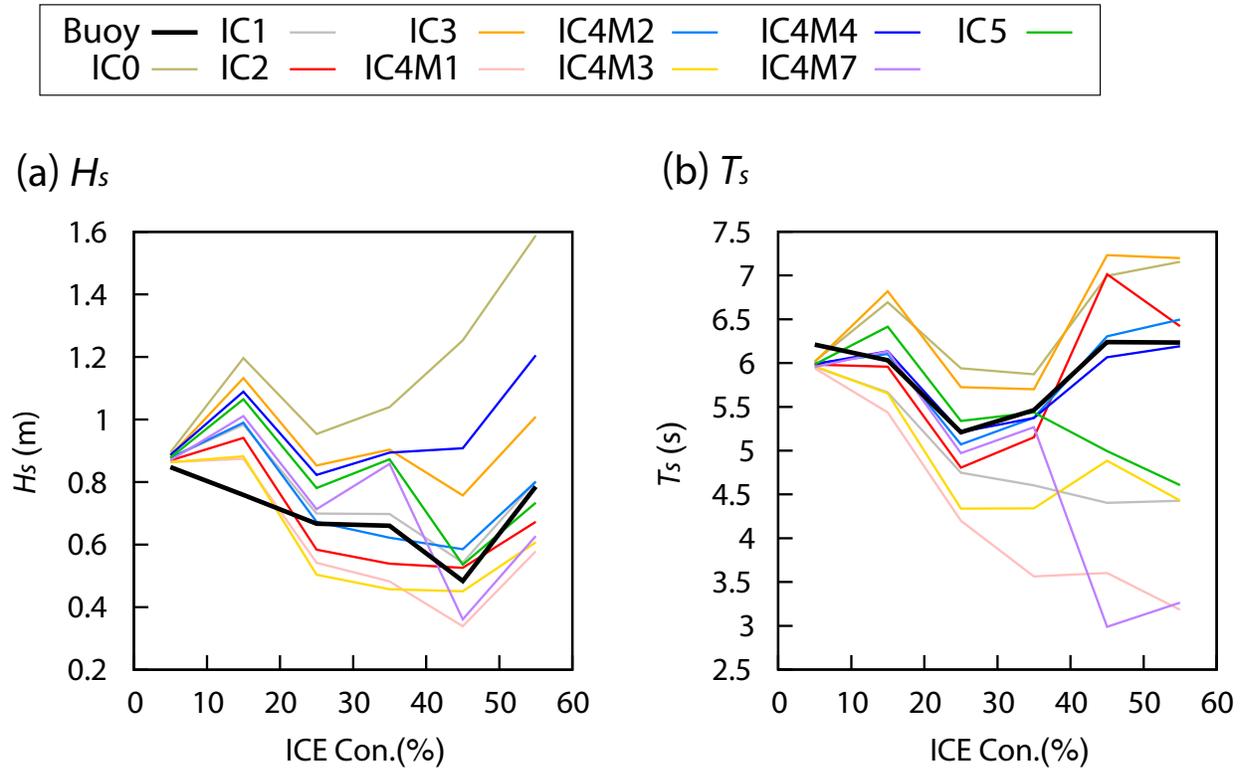
173

174 **Table 1.** *Statistical values of  $H_s$  and  $T_s$  between model simulations and buoy observation.*

	IC0	IC1	IC2	IC3	IC4M1	IC4M2	IC4M3	IC4M4	IC4M7	IC5
<i><math>H_s</math></i>										
Bias (m)	0.47	0.10	0.01	0.27	-0.07	0.08	-0.06	0.29	0.10	0.17
RMSE (m)	0.51	0.40	0.41	0.44	0.44	0.40	0.43	0.44	0.47	0.43
Corr.	0.80	0.83	0.78	0.83	0.76	0.83	0.77	0.83	0.76	0.82
<i><math>T_s</math></i>										
Bias (s)	0.67	-0.82	-0.07	0.66	-1.48	0.02	-0.92	0.00	-0.79	-0.20
RMSE (s)	1.74	1.75	2.17	1.97	2.14	1.96	2.26	1.54	2.29	1.89
Corr.	0.64	0.62	0.56	0.62	0.49	0.65	0.59	0.72	0.43	0.64

175

176 Moreover, we validated the model simulations as a function of ice concentration (Figure  
177 3). All  $H_s$  simulations were overestimated at low ice concentrations ( $C_i < 20\%$ ) (Figure 3a). At  
178 high ice concentrations ( $C_i > 20\%$ ), the tendency differed depending on the simulation (Figure 3a).  
179 IC0, IC3, and IC4M4 were overestimated, while IC4M1 and IC4M3 tended to underestimate  
180 (Figure 3a). IC1 and IC4M2 were relatively close to the buoy observations and were simulated  
181 with high accuracy, consistent with the comparison shown in Figure 2a and Table 1. For  $T_s$ , the  
182 difference  $G$  between the simulations became remarkable as the ice concentration increased  
183 (Figure 3b). IC4M2 and IC4M4 were in good agreement with the observations (Figure 3b). IC1,  
184 IC4M1, IC4M3, and IC4M7 were underestimated, especially for IC4M1 and IC4M7 at  $C_i > 40\%$   
185 (Figure 3b). On the other hand, the  $T_s$  of IC0 and IC3 were overestimated, regardless of ice  
186 concentration (Figure 3b).

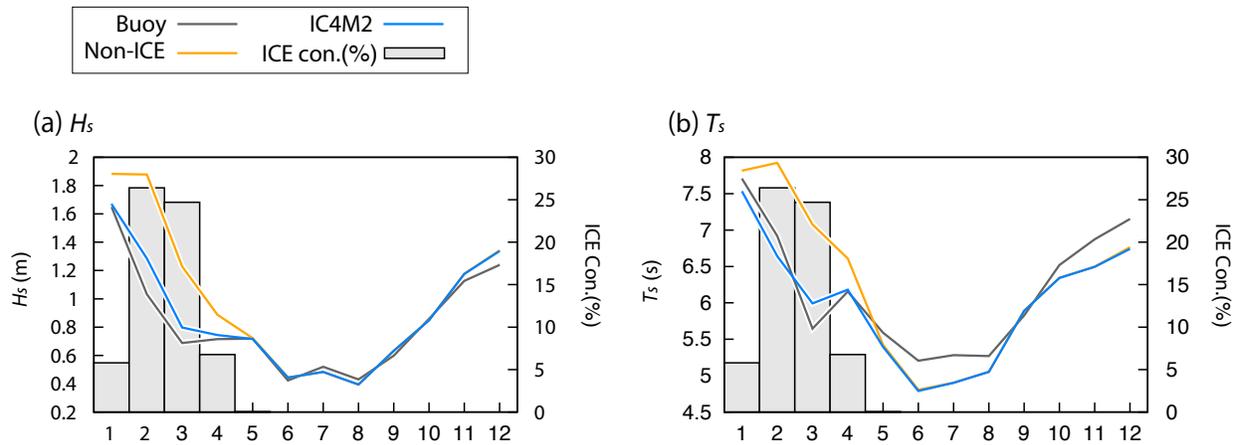


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188 **Figure 3.** (a)  $H_s$  and (b)  $T_s$  averaged from the ST6 model simulations and NOWPHAS buoy as a  
 189 function of ice concentration in 10% bins. The source terms of  $S_{ice}$  represented by the different  
 190 colored lines are interpreted in the legend of the figure. The horizontal axis denotes the ice  
 191 concentration in the coastal area around the buoy ( $44^{\circ}$ – $46^{\circ}$ N,  $142.5^{\circ}$ – $145.5^{\circ}$ E).

### 192 3.2 Sea ice impact for wave field

193 To evaluate the impact of sea ice on ocean waves in the SO, we compared the non-ICE  
 194 simulations and IC4M2, which are relatively accurate. Figure 4 shows the monthly  $H_s$  and  $T_s$  for  
 195 the simulation and observation at the buoy position. In general, large  $H_s$  and  $T_s$  were observed  
 196 in the coastal areas of Hokkaido during winter (Figure 4). Interestingly, IC4M2 simulations  
 197 remarkably improved the overestimation of  $H_s$  and  $T_s$  of Non-ICE simulations from January to  
 198 April, when sea ice existed (i.e., ice concentration is not 0%) Figure 4).

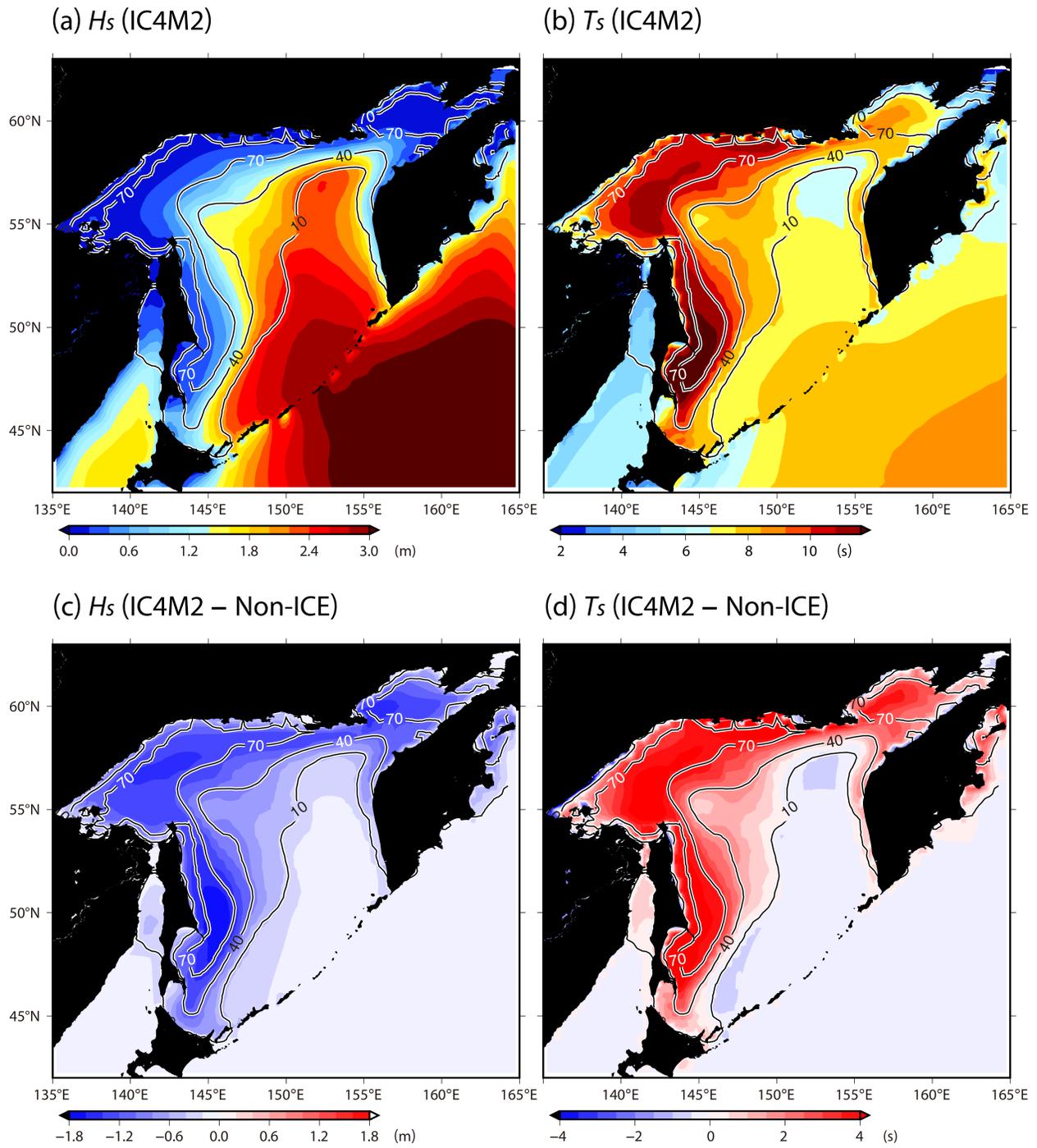


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200 **Figure 4.** Temporal variations of monthly (a)  $H_s$  and (b)  $T_s$  derived from the simulation and the  
 201 buoy observation. The line colors and bars are defined in the legend in the upper left corner. As  
 202 shown in the legend in the upper left corner, different colored lines are used for the buoy  
 203 observation (gray), IC4M2 simulation (light blue), and Non-ICE simulation (yellow). Both  
 204 simulations are modeled results with ST6. Values are averaged each month from 2008 to 2010.  
 205 The light gray bars represent the ice concentration in the coastal area around buoy ( $44^\circ\text{--}46^\circ\text{N}$ ,  
 206  $142.5^\circ\text{--}145.5^\circ\text{E}$ ).

207

208 Figure 5 shows the spatial distribution of  $H_s$  and  $T_s$  from IC4M2 in February, and the  
 209 differences between IC4M2 and non-ICE. As expected, the wave fields were strongly dependent  
 210 on the sea ice field, and  $H_s$  ( $T_s$ ) became smaller (larger) as the ice concentration increased (Figures.  
 211 5a, b). The  $H_s$  ( $T_s$ ) difference between IC4M2 and non-ICE is greater (less) than 1 m (3 s) at high  
 212 ice concentrations ( $C_i > 70\%$ ) (Figure 5).



213

214 **Figure 5.** Averaged field (color) of (a)  $H_s$  and (b)  $T_s$  computed by IC4M2 in February during  
 215 2008–2010; its difference (color) between IC4M2 and Non-ICE simulations; (c)  $H_s$ ; (d)  $T_s$ . Spatial

216 smoothing using a box filter of horizontal scale 50 km was performed for the ice concentration  
217 (contour) (%). In this figure, we used the model results from domain 1.

#### 218 **4 Summary and Discussion**

219 In this study, we evaluated six wave–ice parameterization models (IC0–IC5) using buoy  
220 observations. We also clarified the impact of sea ice on wave fields over the SO. As a result,  
221 IC4M2 appears to agree mostly with buoy observation. We also clarified the impact of sea ice on  
222 wave fields over the SO. In the coastal area, the simulation with sea ice drastically improved the  
223 bias of wave fields ( $H_s$  and  $T_s$ ) compared to that without the use of sea ice. In addition, the  
224 difference between the simulation with and without sea ice is more than 1 m (3 s) for the monthly  
225 mean  $H_s$  ( $T_s$ ). These results suggest that the effect of sea ice on wave calculation is essential not  
226 only in the Arctic and Antarctic Oceans but also in the SO.

227 Various coefficients have been proposed for the binomial fitting of IC4M2 based on  
228 different observational data (Text S1 and Table S1). In the eight simulation results of IC4M2, the  
229 bias of IC4M6H1, WA3 UK, and WA3 NIWA were greater than 0.15 m (0.45 s) in  $H_s$  ( $T_s$ ), which  
230 was larger than the other simulations (Table S2). In fact, the attenuation rates of IC4M6H1, WA3  
231 UK, and WA3 NIWA were lower than those of the other (Figure S1).

232 Our validation demonstrated that the accuracy of IC4M1, IC4M3, and IC4M7 was poor  
233 (especially in  $T_s$ ), and the attenuation rate was significantly different from that of IC4M2 (Figure  
234 S2). This is probably because the sea ice conditions based on these parameterizations are different  
235 from those of the SO. The sea ice thickness is less than 10 cm in the coastal area of Hokkaido  
236 (Figure 1). In addition, the floe size of sea ice is from 1.19 m to 5 m in the coastal area of Hokkaido  
237 (Kioka et al., 2020). In contrast, IC4M1 uses field data with sea ice floe sizes ranging from 20 m  
238 to 30 m. In addition, IC4M3 is based on the ice thickness between 0.5 m and 3m, which is much  
239 thicker than the ice conditions in this study. Moreover, IC4M7 is based on observations of only  
240 the pancake ice region, although both pancake and frazil ice may exist in the SO.

241 The accuracy of theoretical models IC2, IC3, and IC5 is not very poor, despite the use of  
242 the default theoretical ice parameters, which remains questionable in the SO. Recently, Liu et al.  
243 (2020) quantified the kinematic viscosity ( $\nu$ ) used in IC2, the  $\nu$  and the effective shear modulus

244 ( $G$ ) in IC3, based on field observations in the Barents Sea. If the optimum theoretical ice  
245 parameters for the SO can be quantified, improvements in these theoretical models can be expected.

246 ST4 is a source term of  $S_{in}$  and ( $S_{ds}$ ), which is often used in addition to ST6. As described  
247 in Section 2, we also evaluated six dissipation models (IC0–IC5) with ST4 (Figure S3, S4, and  
248 S5). Overall, there were no significant differences in the wave fields between ST4 and ST6 in the  
249 buoy location (Figure S3, Tables 1, and S5). However, the normalized STD for  $H_s$  with ST4 was  
250 remarkably reduced (approximately 0.16) compared with that of ST6 (Figure S3, Tables 1, and  
251 S5). When examined as a function of ice concentration,  $H_s$  and  $T_s$  with ST4 were slightly smaller  
252 than those with ST6, but the tendency in both simulations remained the same (Figure S4).

253 Recently, Nose et al. (2020) revealed that the uncertainty between ice concentration  
254 products is greater than the uncertainty between theoretical models (IC2, IC3, and IC5). Thus, it  
255 should be noted that our results depend not only on the parameterization for source terms such as  
256  $S_{in}$ ,  $S_{ds}$ , and  $S_{ice}$ , but also on the ice concentration used as forcing. In addition, the theoretical  
257 models IC2, IC3, and IC5 also depend on the ice thickness. Moreover, differences in wind data  
258 may also be one of the causes of uncertainty in wave fields.

## 259 **Acknowledgments**

260 We are grateful to data providers including the Ports and Harbours Bureau, Ministry of  
261 Land, Infrastructure, Transport, and Tourism (MLIT) for NOWPHAS buoy  
262 ([https://www.mlit.go.jp/kowan/nowphas/index\\_eng.html](https://www.mlit.go.jp/kowan/nowphas/index_eng.html)), NOAA for OISST version 2  
263 (<https://psl.noaa.gov/data/gridded/data.noaa.oisst.v2.highres.html>), NCEP for CFSR  
264 (<https://rda.ucar.edu/datasets/ds093.1>), and JMA for JRA55  
265 (<https://rda.ucar.edu/datasets/ds628.0>) and DSJRA55 ([https://jra.kishou.go.jp/DSJRA-  
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