

1           **Scaling of moored surface ocean turbulence measurements in the Southeast Pacific Ocean**

2           Una Kim Miller<sup>1</sup>, Christopher J. Zappa<sup>1</sup>, Seth Zippel<sup>2</sup>, J. Thomas Farrar<sup>2</sup>, and Robert A. Weller<sup>2</sup>

3                     <sup>1</sup>Lamont-Doherty Earth Observatory, Columbia University, Palisades, NY, USA

4                             <sup>2</sup>Woods Hold Oceanographic Institution, Falmouth, MA, USA

6           Corresponding author: Una Miller ([ukm2103@columbia.edu](mailto:ukm2103@columbia.edu))

8           **Key points**

- 9           • Moored instrumentation allows for prolonged timeseries of turbulence estimates with concurrent  
10           in-situ meteorological and wave measurements
- 11           • Dissipation rate is scaled well by Law of the Wall in shear-dominant regimes and by surface  
12           buoyancy flux in convective-dominant regimes
- 13           • It is unnecessary in the Southeast Pacific Stratus region to distinguish between a wind-driven and  
14           Langmuir-driven turbulence regime
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## Abstract

36 Estimates of turbulence kinetic energy (TKE) dissipation rate ( $\epsilon$ ) are key to  
37 understanding how heat, gas, and other climate-relevant properties are transferred across the air-  
38 sea interface and mixed within the ocean. A relatively new method involving moored pulse-  
39 coherent Acoustic Doppler Current Profilers (ADCPs) allows for estimates of  $\epsilon$  with concurrent  
40 surface flux and wave measurements across an extensive length of time and range of conditions.  
41 Here, we present 9 months of moored estimates of  $\epsilon$  at a fixed depth of 8.4m at the Stratus  
42 mooring site (20°S, 85°W). We find that shear- and buoyancy-dominant turbulence regimes are  
43 defined equally well using the Obukhov length scale ( $L_M$ ) and the newer Langmuir stability  
44 length scale ( $L_L$ ), suggesting that ocean-side friction velocity ( $u_*$ ) implicitly captures the  
45 influence of Langmuir circulation at this site. This is illustrated by a strong linear dependence  
46 between surface Stokes drift ( $u_s$ ) and  $u_*$  and is likely facilitated by the steady Southeast trade  
47 winds regime. The traditional Law of the Wall (LOW) and surface buoyancy flux scalings of  
48 Monin-Obukhov similarity theory scale our estimates of  $\epsilon$  well, collapsing data points near unity.  
49 We find that the newer Stokes drift scaling ( $\frac{u_*^2 u_s}{\text{mixed layer depth}}$ ) scales  $\epsilon$  well at times but is overall  
50 less consistent than LOW. Scaling relationships from prior studies in a variety of aquatic and  
51 atmospheric settings largely agree with our data in destabilizing, shear-dominant conditions but  
52 diverge in other regimes.

## 53 Plain Language Summary

54 Surface ocean turbulence is key in the transfer of heat, gas, and other climate-relevant  
55 properties between the ocean and atmosphere. Turbulence can be understood through estimates  
56 of turbulence kinetic energy (TKE) dissipation rate ( $\epsilon$ ), which is a measure of the rate of  
57 dissipation of turbulent energy into heat energy. Higher values of  $\epsilon$  indicate a more turbulent  
58 environment. Because  $\epsilon$  is important but difficult to estimate in the field, much effort has been  
59 put into parameterizing it from more easily obtainable variables such as wind speed, wave  
60 measurements, and surface buoyancy flux. Here, we test these parameterizations against an  
61 extensive timeseries of  $\epsilon$  estimates collected on a mooring line attached to a surface buoy in the  
62 Southeast Pacific Ocean. This region is known to support important South American fisheries as  
63 well play a significant role in the global radiation budget, yet is poorly represented in climate  
64 models. We find the wind- and buoyancy flux-based parameterizations to describe our estimates  
65 of  $\epsilon$  well, and we explore how conditions at the study site influence their performance.

## 66 1 Introduction

67 Turbulence kinetic energy (TKE) represents processes that drive the mixing of heat,  
68 momentum, and gas within and between the ocean and atmosphere, making it an important  
69 parameter in studies of weather and climate. It is generated in the Ocean Boundary Layer (OBL)  
70 primarily by wind- and wave-driven shear and buoyancy-driven convection, though wave  
71 breaking and other turbulent processes can play a significant role as well. Assuming a  
72 horizontally homogeneous flow, the TKE budget may be written as

$$\begin{aligned}
73 \quad \frac{D\bar{e}}{Dt} = & - \underbrace{\overline{\mathbf{u}'_h \mathbf{w}' \cdot \frac{\partial \mathbf{u}_h}{\partial z}}}_{\text{Shear production}} - \underbrace{\overline{\mathbf{u}'_h \mathbf{w}' \cdot \frac{\partial \mathbf{u}_s}{\partial z}}}_{\text{Stokes production}} + \underbrace{\overline{w' B'_0}}_{\text{Buoyant production/}} - \underbrace{\frac{\partial}{\partial z} \left( \overline{w' u'_i u'_i} + \frac{1}{\rho_0} \overline{w' p'} \right)}_{\text{Transport}} - \\
74 \quad & \underbrace{\overline{\varepsilon}}_{\text{Destruction by viscous}} \quad \quad \quad 1. \\
& \text{dissipation}
\end{aligned}$$

75

76 where  $e$  is TKE,  $\mathbf{u}_h$  and  $w$  are horizontal and vertical velocities,  $\mathbf{u}_s$  is the Stokes drift velocity  
77 vector,  $B_0$  is surface buoyancy flux,  $\rho_0$  is background density, and  $p$  is pressure. Prime notation  
78 indicates the turbulent component of a Reynolds decomposed quantity, overbars indicate a time  
79 mean, and the subscript  $i$  indicates tensor notation. The shear production term describes TKE  
80 from the shear of currents generated by winds at the surface while the Stokes production term  
81 describes that of the shear of Stokes drift associated with surface waves. The interaction of  
82 Stokes drift with the shear of the wind-driven current results in Langmuir circulation,  
83 characterized by vertically-oriented, counter-rotating vortices that are often visible at the surface  
84 as streaks of foam or kelp aligned in the direction of the wind (Craik and Leibovich, 1976).  
85 These vortices result in enhanced turbulent vertical velocities that aid in the transport of TKE  
86 generated near the surface to the base of the mixed layer (e.g. Sutherland et al., 2014), via the  
87 turbulent transport term. This plays an important role in the deepening of the mixed layer  
88 (Belcher et al., 2012; Li and Fox-Kemper, 2017). The buoyancy term describes the production of  
89 TKE by free convection associated with destabilizing surface buoyancy fluxes or its destruction  
90 by stratification caused by stabilizing fluxes.

91 The rate of TKE dissipation ( $\varepsilon$ ) into heat is of particular interest because it must, on  
92 average, equal the total TKE generated in a system. Traditional parameterizations of  $\varepsilon$  assume a  
93 simplified version of Equation 1 in which the production of TKE by current shear or convection  
94 is balanced by its dissipation. In the absence of surface waves (i.e., the OBL is a “wall”-bounded  
95 layer) and buoyancy flux, the wind term may be scaled using friction velocity ( $u_*$ ) to give rise to  
96 the Law of the Wall (LOW),

$$97 \quad \varepsilon \sim u_*^3 / \kappa |z| \quad \quad \quad 2.$$

98 where the von Kármán constant,  $\kappa$ , is 0.4. Likewise in the absence of waves and wind,  $\varepsilon$  scales  
99 with surface buoyancy flux ( $B_0$ ):

$$100 \quad \varepsilon \sim B_0 \quad \quad \quad 3.$$

101 Early studies of the application of LOW and Equation 3 in the OBL include Shay and Greg  
102 (1986), Anis and Moum (1992) and Brainerd and Gregg (1993). Dimensional analysis of LOW  
103 and Equation 3 gives rise to a key length scale known as the Obukhov length scale,

$$104 \quad L_M = \frac{-u_*^3}{\kappa B_0} \quad \quad \quad 4.$$

105 which may be conceptualized as the depth at which buoyancy and mechanical shear contribute  
106 equally to turbulence in the ocean (e.g. Stull, 1988). It follows that buoyancy forcing dominates  
107 the TKE regime where  $\left| \frac{z}{L_M} \right| > 1$  (production in convective conditions, suppression in stable

108 conditions) and wind forcing dominates where  $\left| \frac{z}{L_M} \right| < 1$ . This serves as the basis for scaling  
 109 relationships derived from Monin-Obukhov (MO) similarity theory (Monin and Obukhov, 1959).

110 In the atmosphere, MO scaling relationships for  $\varepsilon$  typically take the form of

$$111 \quad \frac{\varepsilon \kappa z}{u_*^3} = \left[ A^{1/M_1} + B^{1/M_2} \left| z/L_M \right|^{1/M_3} \right]^{M_4} \quad 5.$$

112 where  $A$ ,  $B$ , and  $M_i$  are empirically derived coefficients and  $z$  is height. Here,  $\varepsilon$  is  
 113 nondimensionalized by  $LOW$ . In the OBL, this equation is often rearranged by dividing through  
 114 by  $LOW$  and setting  $M$  equal to unity such that  $\varepsilon$  is presented as a linear combination of TKE  
 115 production by wind and buoyant forcing:

$$116 \quad \varepsilon = A \frac{u_*^3}{\kappa z} + B B_0 \quad 6.$$

117 where  $A$  and  $B$  are typically determined by the averages of  $\varepsilon / \frac{u_*^3}{\kappa z}$ , and  $\varepsilon / B_0$  in their respective  
 118 dominant regimes, and  $B_0$  is restricted to positive values (turbulence producing rather than  
 119 suppressing). Equation 6 was first proposed in Lombardo and Gregg (1989) for an intermediate  
 120  $L_M$ -defined regime in which both mechanical and buoyant forcing contributed significantly to  
 121 turbulence production, though they found it also scaled measurements of turbulence fairly well  
 122 across all observed conditions.

123 The representation of the OBL in MO Similarity Theory as a wave-free, wall-bounded  
 124 layer has been challenged by decades of observational studies of turbulence generated by surface  
 125 wave breaking (Agrawal et al., 1992; Anis and Moum, 1995; Craig and Banner, 1994; Drennan  
 126 et al., 1992; Gemmrich and Farmer, 2004; Soloviev and Lukas, 2003; Terray et al., 1996) and  
 127 wind-wave interaction (D'Asaro, 2014; Sutherland et al., 2014). Wave breaking directly injects  
 128 turbulence into the near-surface "breaking layer", which extends down to a depth of  
 129 approximately 0.6 the significant wave height ( $H_{sw}$ ) (Gerbi et al., 2009; Terray et al., 1996).  
 130 TKE generated in this layer is transported downwards to a "transition layer", also known as  
 131 wave-affected surface layer (WASL) (Gerbi et al., 2009; Stips et al., 2005). According to Terray  
 132 et al., (1996), this transition layer is bounded below by the transition depth,  $z_t$ , though  
 133 observational studies have since shown mixed results on its presence or extent (Esters et al.,  
 134 2018; Sutherland and Melville, 2015). Dissipation rates are expected to deviate from MO  
 135 Similarity Theory (Equations 2, 3, 5, and 6) in the breaking and transition layers, and conform  
 136 below, where TKE from waves has dissipated entirely.

137 While TKE generated through surface wave breaking and the shear of Stokes drift  
 138 velocities is largely confined to the upper few meters of the water column, Langmuir circulation  
 139 can distribute turbulence to the base of the mixed layer through its associated enhancement of  
 140 vertical transport. Because of its importance to mixed layer deepening, there have been many  
 141 efforts to parameterize Langmuir circulation in models of the OBL (Li et al., 2019). The  
 142 Langmuir number,  $L_a = \sqrt{u_* / u_s}$ , arises from a scaled ratio of the wind and wave terms in  
 143 Equation 1 and describes the strength of Langmuir circulation (McWilliams et al., 1997). For  
 144 well-developed seas,  $L_a \sim 0.4$  (Belcher et al., 2012; Sutherland et al., 2014), though misalignment  
 145 of wind and waves is known to broaden the range of  $L_a$  (Van Roekel et al., 2012). According to  
 146 LES results from Grant and Belcher (2009), a distinct Langmuir-driven regime is defined where

147  $L_a < 0.5$ , with the transition to a wind-dominant regime occurring between  $0.5 < L_a < 2$ . A  
 148 second term, the Langmuir stability length scale,  $L_L = -u_*^2 u_s / B_0$ , similarly arises from the  
 149 scaled ratio of the wave and buoyancy terms in Equation 1. It describes the relative strength of  
 150 Langmuir circulation to buoyant forcing (Belcher et al., 2012) and the use of  $\frac{h}{L_L}$  to define  
 151 turbulence regimes, where  $h$  is mixed layer depth, is analogous to that of  $z/L_M$ . Belcher et al.  
 152 (2012) defines Langmuir-dominant and buoyancy-dominant regimes as  $\frac{h}{L_L} > 1$  and  $\frac{h}{L_L} < 1$ ,  
 153 respectively, but because this term contains both  $u_s$  and  $u_*$ , it can also be considered a  
 154 delineation of a buoyancy-dominant regime and that of a composite “wind-wave-induced”  
 155 turbulence that includes the contributions of both wind-induced current shear and Langmuir  
 156 circulation (Esters et al., 2018; Sutherland et al., 2014).

157 Because wind and waves are intrinsically tied, there is some question as to whether it is  
 158 necessary to parameterize Langmuir circulation separately, or if the implicit incorporation of  
 159 wave effects in traditional wind scaling parameterizations is sufficient. In their model study on  
 160 the global prevalence of Langmuir circulation, Belcher et al. (2012) argued against this,  
 161 reasoning that wind and waves are rarely in equilibrium and citing variability in the ratio of  $u_s$  to  
 162  $u_*$  as evidenced by the large range in their computed values of  $L_a$  across the world’s oceans.  
 163 Conversely, a number of observational studies have found  $u_s$  to scale linearly with  $u_*$  (Esters et  
 164 al., 2018; Gargett and Grosch, 2014; Kitaigorodskii et al., 1983). In cases where  $u_s$  is linearly  
 165 proportional to  $u_*$ , it follows that that  $L_a$  is relatively constant and thus  $L_L$  and  $L_M$  become  
 166 linearly proportional as well, as  $L_M = L_a^{-2} L_L$  (omitting the von Kármán constant).

167 A framework based on  $L_a$  and  $L_L$  is presented in Belcher et al. (2012) and has been used  
 168 by both observational (Esters et al., 2017) and large eddy simulation (LES) studies (e.g. Li et al.,  
 169 2019; Li and Fox-Kemper, 2017) to assess the relative contributions of wind-driven current  
 170 shear, buoyancy forcing, and Langmuir circulation to the overall turbulence regime. This  
 171 framework defines TKE as a linear combination of the three forcings, similarly to Equation 6,

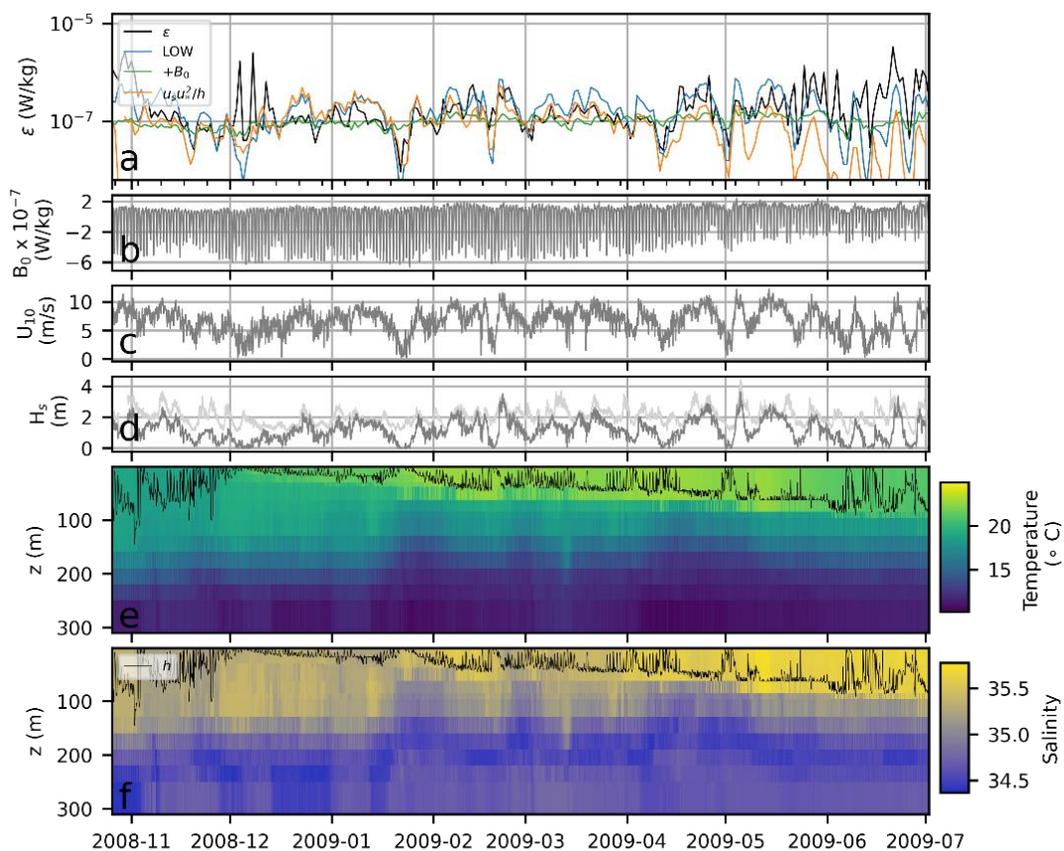
$$172 \quad \varepsilon\left(\frac{z}{h} = 0.5\right) = A_s \frac{u_*^3}{h} + A_L \frac{w_{*L}^3}{h} + A_c \frac{w_*^3}{h} \quad 7.$$

173 where  $w_{*L} = (u_*^2 u_s)^{1/3}$  and  $w_* = (B_0 h)^{1/3}$  are velocity scales for wave and buoyancy-forced  
 174 turbulence and  $A_s = 2 \left(1 - e^{-\frac{1}{2} L_a}\right)$ ,  $A_L = 0.22$ , and  $A_c = 0.3$  are coefficients derived from LES  
 175 studies. This equation applies where  $z$  is half of  $h$ , an arbitrary depth chosen to discern where the  
 176 three forcings are well established.  $A_s$  is made a function of  $L_a$  to account for the inhibition of  
 177 vertical velocity shear and thus shear production by the enhanced vertical velocities associated  
 178 with Langmuir circulation. Equation 7 is rearranged into a scaling relationship of the form

$$179 \quad \frac{\varepsilon\left(\frac{z}{h}=0.5\right)}{\frac{u_*^3}{h}} = A_s + A_L L_a^{-2} + A_c L_a^{-2} \frac{h}{L_L} \quad \text{where } B_0 > 0 \quad 8.$$

180 which is used to define a turbulence regime diagram in  $L_a - h/L_L$  space (e.g. Figure 2). The  
 181 three “corners” of this diagram denote regimes where either wind, Langmuir, or buoyancy is the  
 182 dominant forcing.

183 Here, we use both MO similarity and the more recent Belcher et al. (2012) framework to  
 184 explore the scaling of  $\varepsilon$  estimates obtained from a moored Pulse-Coherent acoustic Doppler  
 185 current velocity profiler (ADCP) in the Southeast Pacific Ocean Stratus region. Moored ADCP  
 186 measurements represent a relatively new methodology (Zippel et al., 2021) that allows for the  
 187 analysis of turbulence across an extended length of time and range of conditions. The moored  
 188 nature of these measurements also allows for concurrent, in-situ measurements of wind, waves,  
 189 and surface fluxes, which are not always possible in more standard deployments of  
 190 ascending/descending profilers. The ADCP was deployed at 8.4 meters water depth on the  
 191 Stratus Mooring at 20°S, 85°W in 2008-2010, as part of the Variability of American Monsoon  
 192 Systems (VAMOS) Ocean–Cloud–Atmosphere–Land Study Regional Experiment (VOCALS-  
 193 Rex) (Mechoso et al., 1995; Wood et al., 2011). The Stratus Mooring has been maintained by the  
 194 Woods Hole Oceanographic Institution Upper Ocean Processes Group since 2000 and has been  
 195 integral in efforts to characterize boundary layer processes in the Stratus region. Results from  
 196 data collected at the mooring site are considered applicable over large swaths of the Stratus  
 197 region, as it is known to lack synoptic forcing and exhibit relative uniformity in hydrographic  
 198 surveys and wind fields (Holte et al., 2014; Weller et al., 2014).



199  
 200 **Figure 1.** Time series of daily-averaged a) TKE dissipation rate ( $\varepsilon$ ) overlaid with the Law of the Wall (LOW; Equation 2),  
 201 destabilizing (positive) surface buoyancy flux ( $+B_0$ ; Equation 3) and  $u_s u_s^2/h$  scalings, b) surface buoyancy flux ( $B_0$ ), c)  
 202 wind speeds at 10 meters height ( $U_{10}$ ), d) significant wave height ( $H_s$ ) calculated from measured wave spectra (full

203 spectrum in light gray, wind-sea in dark gray), e) potential temperature and f) practical salinity, overlaid by mixed layer  
204 depth ( $h$ ; black line)

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## 206 **2 Data and Methods**

### 207 **2.1 Pulse-coherent ADCP**

208 Fine-scale velocity measurements were collected with a 2 MHz Nortek AquaDopp High-  
209 Resolution (HR) velocity profiler installed at 8.4 meters water depth on the mooring line and  
210 outfitted with a fin that allowed it to remain in-line with and facing the prevailing current (see  
211 Zippel et al., 2021). The AquaDopp HR is a pulse-to-pulse coherent ADCP that transmits two  
212 sequential pulses of which the phase shift allows for the calculation of radial velocities at  
213 centimeter-scale resolution. The specifics and validation of obtaining microstructure turbulence  
214 measurements using pulse-coherent ADCPs were first described in Veron and Melville (1999)  
215 and later in the context of moored deployments in Zippel et al. (2021). The instrument was fitted  
216 with a custom sensor head with 3 beams: two beams in a plane orthogonal to the cylindrical axis  
217 and a third beam directed upward  $45^\circ$  to this plane and  $45^\circ$  between the two horizontal  
218 orthogonal beams. The system was set to sample only Beam 1, orthogonal to the instrument axis  
219 and into the flow along the axis of the vane, in order to maximize the sample rate at 4 Hz.  
220 Profiles of along-beam velocities were 1.38 meters total in length and range-gated into 53 cells,  
221 each 26 millimeters in size. The nominal velocity range in each bin was  $\pm 10.5 \text{ cm s}^{-1}$  and  
222 sampling occurred over 135 second “bursts” once every hour at a rate of 4 Hz for a total of 540  
223 profiles per burst. Over 5000 bursts were collected in total over the study period.

### 224 **2.2 Calculation of TKE dissipation rate**

225 The AquaDopp HR appeared significantly bio-fouled upon recovery, so velocity  
226 measurements were truncated at 02-July-2009, shortly before the velocity and corresponding  
227 ping correlation values (a measure of strength-of-return) became erratic. The remaining data  
228 were quality-controlled and used to calculate  $\varepsilon$  following the methods detailed in Zippel et al.  
229 (2021). A simplified overview of these methods is provided here.

230 Data are first corrected for phase wrapping, an artifact associated with pulse-coherent  
231 ADCPs in which radial velocities exceeding a so-called ambiguity velocity “wrap around” and  
232 are recorded as abruptly high or low values in multiples of  $2\pi$ . Then, “unwrapped” velocity  
233 profiles with an averaged ping correlation lower than 60% and individual pings with correlations  
234 lower than 40% are removed. Power spectra are calculated from the individual velocity profiles  
235 collected during each 135-second burst, then averaged together into a single, burst-averaged  
236 power spectrum.  $\varepsilon$  is estimated from the inertial subrange of each burst-averaged spectrum,  
237 defined as the region where the slope of the spectrum is equal to the theoretical  $-5/3$  from  
238 Kolmogorov’s “ $5/3$ ” law for energy distribution in a turbulent fluid (Kolmogorov, 1941):

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$$240 \quad E(k) = C_1 \varepsilon^{2/3} k^{-5/3} \quad 9.$$

241 Here,  $E(k)$  is the power spectral density of turbulent velocities in the inertial subrange,  $k$  is  
242 wavenumber, and  $C_1 = 0.53$  (Sreenivasan, 1995). Values of  $\varepsilon$  below  $10^{-9} \text{ W/kg}$  (constituting  
243 3% of total data) are masked as they are likely close to the instrument noise floor, as reported for  
244 a similar pulse-coherent ADCP configuration in Zippel et al. (2021).

### 245 2.3 Temperature, salinity, and mixed layer depth

246 Temperature and salinity were measured from a suite of conductivity-temperature loggers  
247 installed on the mooring line at depths of 0.85, 3.7, 6.75, 16, 30, 37.5, 40, 62.5, 85, 96.3, 130,  
248 160, 190, 220, 250, and 310 meters. Four different sensor models were used: RBR XR-420, Sea-  
249 Bird Electronics (SBE)-39, SBE-16, and SBE-37. Mixed layer depth,  $h$ , was calculated using  
250 hourly-averaged temperature measurements interpolated over half meter intervals, and defined to  
251 extend down to the depth at which temperature first differs by 0.1 degrees from the surface.

### 252 2.4 Meteorological measurements

253 Wind speed, wind direction, air temperature, humidity, shortwave radiation, and  
254 longwave radiation were recorded once per minute from an Improved Meteorological (IMET)  
255 sensor suite installed on the buoy about 2.7 meters above sea surface (Colbo and Weller, 2009).  
256 Buoyancy flux, defined as positive out of the ocean and in units of  $W/kg$ , was calculated as

$$257 \quad B_0 = -\frac{g\alpha Q_{net}}{\rho c_p} + g\beta(E - P)S_0 \quad 10.$$

258 where  $g$  is gravity,  $\alpha$  is the thermal expansion coefficient,  $Q_{net}$  is surface heat flux,  $\rho$  is ocean  
259 density,  $c_p$  is the specific heat of water,  $\beta$  is the haline contraction coefficient,  $E$  and  $P$  are the  
260 rates of evaporation and precipitation, and  $S_0$  is the surface salinity.  $P$ , measured using a rain  
261 gauge on the buoy, was effectively  $0 \text{ m s}^{-1}$  across the entire study period.  $Q_{net}$  is calculated as  
262 the net sum of the shortwave, net longwave, latent, and sensible fluxes. Net longwave radiation  
263 and the turbulent heat fluxes were calculated using version 3.6 of the COARE bulk flux  
264 algorithm (Fairall et al., 2003, 1996). Only the amount of shortwave radiation absorbed in the  
265 mixed layer ( $I$ ) is used in the calculation of  $Q_{net}$ , which can at times exclude upwards of 20% of  
266 the total incoming radiation ( $I_0$ ). This is calculated as:

$$267 \quad I = I_0 - \left[ I_0 (I_1 e^{-\frac{h}{\lambda_1}} + I_2 e^{-\frac{h}{\lambda_2}}) \right] \quad 11.$$

268 where subscripts 1 and 2 indicate the shortwave and longwave components of insolation,  
269 following Price et al. (1986).  $I_1 = 0.62$ ,  $I_2 = 1 - 0.62$ ,  $\lambda_1 = 0.6m$ ,  $\lambda_2 = 20m$  for fairly clear,  
270 mid-ocean water (Paulson and Simpson, 1977). COARE was also used to calculate  $E$  and wind  
271 stress ( $\tau = \rho \overline{u'w'}$ ). Water-side friction velocity was calculated as  $u_* = \left( \frac{|\tau|}{\rho} \right)^{\frac{1}{2}}$  and  $\alpha$ ,  $c_p$ ,  $\beta$  and  
272  $\rho$  were calculated with the Gibbs Seawater Oceanographic Toolbox.

### 273 2.5 Wave measurements

274 Wave data were acquired from the National Buoy Data Center (NBDC) wave and marine  
275 data acquisition system (WAMDAS; Teng et al. (2005)) installed on the mooring's 2.7m-  
276 diameter surface buoy. The inertial measurement unit for the WAMDAS was installed inside the  
277 buoy, near the water line. Two-dimensional wave frequency spectra were calculated from the  
278 wave spectral density and Longuet-Higgins Fourier Coefficients provided for the Stratus  
279 mooring station by the NBDC. The measured frequencies ranged from 0.020 to 0.485 Hz and  
280 higher frequencies are estimated using an  $f^{-5}$  spectral tail calculated according to Appendix B  
281 of Webb and Fox-Kemper (2015). Though patching on an  $f^{-5}$  tail is a standard method of  
282 extending the spectra beyond what is feasibly measured, we recognize that it may result in an  
283 underestimation of Stokes drift on the order of  $\sim 10$ -30% if the highest measured ("cut-off")

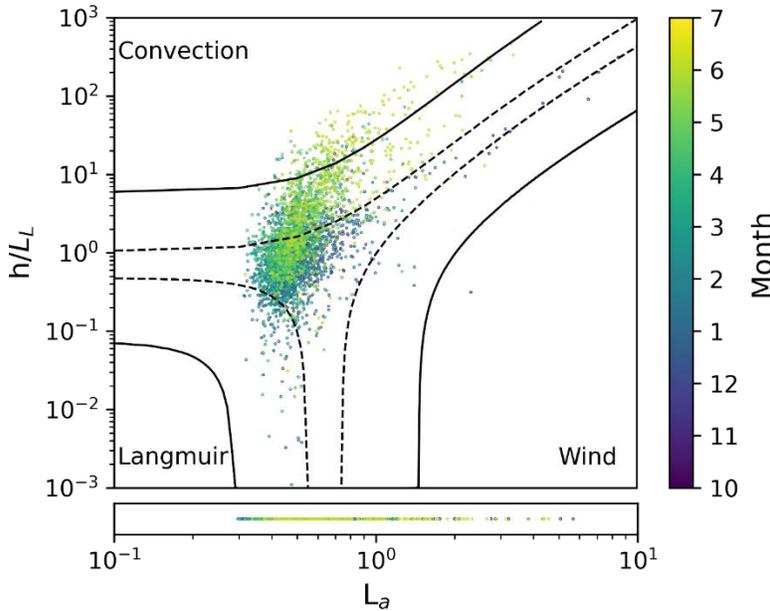
284 frequency is lower than that of the transition between equilibrium and saturation ranges (Lenain  
 285 and Pizzo, 2020). Stokes drift at the surface is calculated as

$$286 \quad u_s|_{z=0} \approx \frac{16\pi^3}{g} \int_0^\infty \int_{-\pi}^\pi (\cos\theta, \sin\theta, 0) f^3 S_{f\theta}(f, \theta) d\theta df \quad 12.$$

287 where  $f$  is frequency and  $S_{f\theta}$  is the directional wave spectrum. To obtain the component of the  
 288 Stokes drift in the direction of the wind, Equation 12 is multiplied by the cosine of the difference  
 289 between the direction of Stokes drift with that of the wind. From here onward,  $u_s$  denotes the  
 290 component of the surface Stokes drift in the direction of the wind.

291 The wind-sea separation frequency was calculated systematically using methods  
 292 described in Wang and Hwang (2001) and Hwang et al. (2011). Significant wave height of the  
 293 wind-sea,  $H_{sw}$ , is defined as  $\frac{1}{4}\sqrt{m_0}$ , where  $m_0$  is the zeroth integral moment of the 1-D wave  
 294 spectral density of the wind-sea spectra. Phase speed is calculated as  $c_p = 1.56/f_{peak}$ , where  
 295  $f_{peak}$  is the peak frequency of the wind-sea. The wave transition depth is defined in Terray et al.  
 296 (1996) as  $z_t = 0.3\kappa\bar{c}/u_*$ , where  $\bar{c}$  is an effective phase speed related to the flux of energy from  
 297 wind stress into the wave field. We use the approximation  $\bar{c} = \frac{1}{2}c_p$ , which represents an upper-  
 298 bound estimate.

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301  
 302 **Figure 2.** Turbulence regime diagram showing the relative contributions to TKE by convection, Langmuir circulation,  
 303 and wind-generated current shear, after Belcher et al. (2012). Data are colored by the calendar month during which they  
 304 were collected, with partial data from July and October and no data from August and September. Solid and dashed lines  
 305 indicate regions where 90% and 60%, respectively, of overall TKE is generated by a single forcing, as calculated from  
 306 Equation 8. The regime diagram is defined only for destabilizing  $B_0$ , so data in stabilizing conditions are shown in 1-  
 307 dimensional  $L_a$  space below.

308

### 309 3 Results

#### 310 3.1 Conditions at the Stratus Mooring Site

311 Monthly-averaged destabilizing buoyancy fluxes are strongest in May and June  
312 ( $\sim 1.5 \times 10^{-7} \text{Wkg}^{-1}$ ), and weakest in the austral summer months ( $\sim 8 \times 10^{-8} \text{Wkg}^{-1}$ ) (Figure  
313 1b). The average hourly change in wind direction is  $7.4^\circ$ , in line with the remarkably  
314 directionally steady trade wind regime noted by Weller (2015). The magnitude of wind forcing  
315 is also fairly steady across the study period, with an average  $U_{10} = 6.7 \text{ms}^{-1}$ , standard deviation  
316 of  $2.2 \text{ms}^{-1}$ , and average hourly change of  $0.64 \text{ms}^{-1}$  (Figure 1c). However, there are several  
317 days-long periods where wind speeds drop to near-zero across the study period, such as in late  
318 January and mid-May. Trade winds in the region are driven by a high pressure cell to the  
319 southwest of the mooring, and dip when this cell is shifted and its associated pressure gradient is  
320 weakened (Weller et al., 2014). Dissipation rate drops in response to these dips in wind speed,  
321 though the magnitude of this response is variable (Figure 1a).

322 Spectra show the wind-sea to propagate primarily to the northwest whereas swell,  
323 originating from storms in the South Pacific, is primarily to the northeast. The equilibrium state  
324 of wind and wind-sea can be inferred with wave age,  $\frac{c_p}{U_{10}}$ , with young seas where  $\frac{c_p}{U_{10}} < 0.8$ ,  
325 mature seas where  $0.8 < \frac{c_p}{U_{10}} < 2$ , and old seas where  $\frac{c_p}{U_{10}} > 2$  (Edson et al., 2007). The average  
326 wave age of the wind-sea for conditions of  $U_{10} > 3 \text{ms}^{-1}$  is 1.8 with a standard deviation of 1,  
327 suggesting the prevalence of mature seas at the mooring site. There is a clear linear dependence  
328 between  $u_s$  and  $u_*$ , with  $u_s = 5.5u_* + 9 \times 10^{-3}$  and an  $r^2$  value of 0.62 (Supplemental Figure  
329 1). From November through May,  $L_a$  averages to 0.51 with a standard deviation of 0.16. In June,  
330 the average and standard deviation are higher, at 0.86 and 0.72, respectively. Temperature and  
331 salinity data show the presence of the cold, fresh ( $11\text{-}13^\circ \text{C}$ ,  $34.1\text{-}34.3$ ; Schneider et al., 2003)  
332 Eastern South Pacific Intermediate Water (ESPIW) underlying the mixed layer at about  $\sim 200 \text{m}$ .  
333 The mixed layer depth broadly tracks the seasonal increase in destabilizing buoyancy fluxes and  
334 is modulated on shorter time scales by wind speed; e.g. the abrupt shoaling of the mixed layer  
335 depth that coincides with a drop in wind speeds that occurs in late January (Figure 1e,f).

336 Daily-averaged  $\varepsilon$  is shown in Figure 1a, overlain with daily-averaged LOW, destabilizing  
337  $B_0$ , and  $u_*^2 u_s / h$ . There are periods of time, such as in late December, where  $B_0$  clearly captures  
338 the magnitude of  $\varepsilon$  more closely than LOW or  $w_{*L} / h$ . Late February is an example of where the  
339 opposite is true. There are also periods where  $u_*^2 u_s / h$  matches the magnitude of  $\varepsilon$  more closely  
340 than LOW (all of March), and vice versa (late May). This is indicative of differing turbulence  
341 regimes at the mooring site, which are illustrated by Figure 2. In this diagram, the relative  
342 contributions of destabilizing surface buoyancy flux, wind-driven current shear, and Langmuir  
343 processes to the turbulence regime are calculated according to Equation 8 and colored by month  
344 to highlight variability across seasons. Stabilizing buoyancy flux conditions are represented in 1-  
345 dimensional  $L_a$  space below. As in Belcher et al. (2012) and following (Leibovich, 1983),  $L_a$  is  
346 calculated only for values of  $U_{10}$  above  $3 \text{m/s}$ , which excludes 3% of data in conditions of  
347 destabilizing  $B_0$  and 8% in conditions of stabilizing  $B_0$ . The black lines indicate regions where a  
348 single forcing is the dominant mechanism of turbulence production; the dotted and solid lines

349 ostensibly indicate a 60% and 90% contribution, respectively, to overall turbulence, as calculated  
 350 from ratios of the terms in Equation 8. Turbulence appears more buoyancy-forced in the austral  
 351 winter months (yellow) than during the rest of the study period, when a mix of buoyant- and  
 352 Langmuir-forced conditions prevail.

Study	Setting	Instrumentation	Scaling relationship for $\varepsilon$	
<b>Wyngaard &amp; Coté (1971)</b>	ABL; Wheat field	Hot-wire anemometer	$\frac{\varepsilon K Z}{u_*^3} = [1 + 0.5] \left  \frac{z}{L} \right ^{2/3}]^{3/2}$	where $\frac{z}{L_M} < 0$
			$\frac{\varepsilon K Z}{u_*^3} = [1 + 2.5] \left  \frac{z}{L} \right ^{3/5}]^{3/2}$	where $\frac{z}{L_M} > 0$
<b>Edson &amp; Fairall (1998)</b>	Marine ABL; Northeast Pacific, Northwest Atlantic	Sonic anemometer	$\frac{\varepsilon K Z}{u_*^3} = \frac{1 - \frac{z}{L_M}}{1 - 7 \frac{z}{L_M}} - \frac{z}{L_M}$	where $\frac{z}{L_M} < 0$
			$\frac{\varepsilon K Z}{u_*^3} = 1 + 5 \frac{z}{L_M}$	where $\frac{z}{L_M} > 0$
<b>Lombardo &amp; Gregg (1989)</b>	Northeast Pacific	Descending microstructure profiler	$\varepsilon = 1.76 \frac{u_*^3}{\kappa z } + 0.58B_0$	where $\frac{h}{L_M} > 0$
<b>Esters et al. (2018)</b>	Subtropical and North Atlantic, Arctic Ocean	Ascending microstructure profiler	$\varepsilon = 0.63 \left( 0.90 \frac{u_*^3}{\kappa z } + 0.91B_0 \right)$	where $\frac{h_\varepsilon}{L_L} > 1$
<b>Callaghan et al. (2014)</b>	Indian Ocean	Ascending microstructure profiler	$\varepsilon = 0.73 \frac{u_*^3}{\kappa z } + 0.81B_0$	where $B_0 > 0$
<b>Tedford et al. (2014)</b>	Lake Pleasant, New York	Ascending temperature-gradient microstructure profiler	$\varepsilon = 0.56 \frac{u_*^3}{\kappa z } + 0.77B_0$	where $B_0 > 0$

353

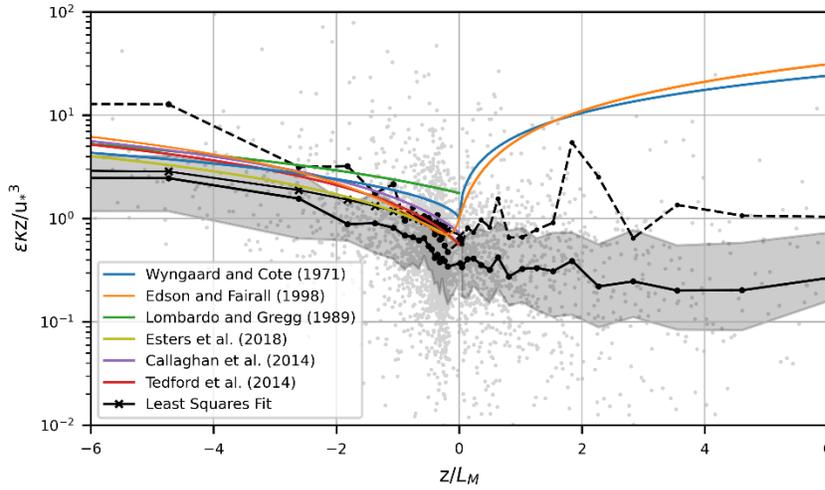
354 **Table 1. Scaling relationships examined in Figure 3.**

355

### 356 3.2 Scaling of $\varepsilon$

357 Measurements of  $\varepsilon$  binned by  $z/h$  show a marked deviation from the LOW, buoyancy  
 358 flux, and  $u_*^2 u_s/h$  scalings when the instrument is very near to ( $\frac{z}{h} \sim 1$ ) and very far from ( $\frac{z}{h} \ll 1$ )  
 359 the base of the mixed layer (Supplemental Figure 2). Because moored pulse-coherent ADCPs are  
 360 at a fixed depth and may remain near the top or bottom of the mixed layer for significant periods  
 361 of time, boundary processes may considerably influence measured dissipation. Such processes at  
 362 the base of the mixed layer include internal wave breaking and inertial shear, and at its upper  
 363 bound bordering the transition zone, surface wave breaking. While the depth of our instrument is  
 364 consistently 3-4 times that of  $H_{sw}$  and therefore out of the direct influence of breaking wave  
 365 turbulence, calculation of  $z_t$  from Terray et al. (1996) suggests that up to 10% of data may be  
 366 influenced by wave breaking turbulence transported downwards from the breaking layer. As a

367 heuristic means of minimizing the influence of turbulent processes other than current shear,  
 368 buoyancy flux, and Langmuir circulation in our scaling analysis, we examine the scaling of  $\varepsilon$  by  
 369 LOW, buoyancy flux, and  $u_*^2 u_s/h$  in the range of  $0.135 < \frac{z}{h} < 0.5$ , which includes  $\sim 60\%$  of  
 370 measurements in destabilizing conditions (turbulence is generated) and  $\sim 40\%$  in stabilizing  
 371 conditions (turbulence is suppressed). These cutoffs correspond to  $\frac{z}{h}$  bins below and above which  
 372 the large deviations of  $\varepsilon$  from these scalings are evident (Supplemental Figure 2).



373  
 374 **Figure 3.** Measurements of  $\varepsilon$  (away from the boundaries of the mixed layer;  $0.135 < \frac{z}{h} < 0.5$ ) scaled by Law of the Wall  
 375 (Equation 2) across  $z/L_M$  regimes. Negative  $z/L_M$  corresponds to destabilizing conditions. The mean and median of bins  
 376 containing equal numbers of data are denoted by the dashed and solid black lines, respectively. The shaded region  
 377 indicates the interquartile range. The overlaid MO scaling relationships are defined in Table 1 and the least squares fit by  
 378 Equation 13.

### 379 3.2.1 Shear and buoyancy regimes

380 Scaled  $\varepsilon$  is shown across  $z/L_M$  regimes in Figure 3, overlaid with bin-averaged mean and  
 381 median. A least squares regression to Equation 6 of data excluding outlying values of  $\frac{\varepsilon K Z}{u_*^3}$  (the  
 382 highest and lowest 1%) returns:

$$383 \quad \frac{\varepsilon K Z}{u_*^3} = 0.69 - 0.46z/L_M \quad 13.$$

384 Also overlaid are scaling relationships developed in prior studies of the ABL (Edson and Fairall,  
 385 1998; Wyngaard and Coté, 1971), OBL (Callaghan et al. 2014; Esters et al., 2018; Lombardo and  
 386 Gregg, 1989) and lake surface boundary layer (Tedford et al., 2014). The scaling relationships,  
 387 detailed in Table 1, are evaluated at each bin across the full  $z/L_M$  range of our data, though the  
 388 actual ranges of data from which they were developed were either narrower or unspecified. We  
 389 note that the scaling relationship from Esters et al. (2018) is defined for conditions of buoyancy  
 390 dominance,  $\frac{h_\varepsilon}{L_L} > 1$ , where  $h_\varepsilon$  is the active mixing layer, though we present it across all data  
 391 where  $B_0 > 0$ . In destabilizing conditions, these scaling relationships describe the binned mean  
 392 and least squares fit of our data well where  $|z/L_M| < 1$ , but diverge at greater values, where they

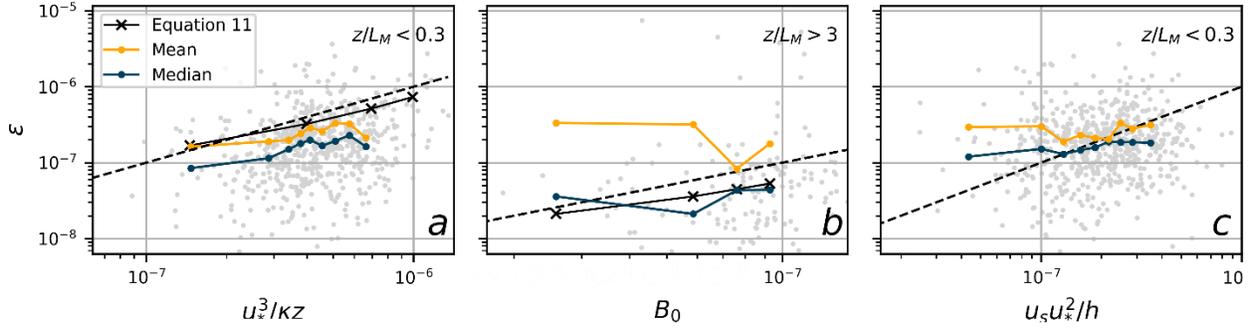


Figure 4. Measurements of  $\varepsilon$  (away from the boundaries of the mixed layer;  $0.135 < \frac{z}{h} < 0.5$ ) in destabilizing conditions plotted directly against the Law of the Wall (Equation 2), surface buoyancy flux (Equation 3), and  $u_s u_*^2/h$  scalings. Dominant forcing regimes are defined using  $z/L_M$ , with  $\frac{z}{L_M} < 0.3$  denoting a buoyancy-dominant regime and  $\frac{z}{L_M} > 3$  denoting a shear-dominant regime. The dashed black line corresponds to a 1:1 line. Bins contain equal numbers of data points.

393 overestimate our bin-averaged  $\varepsilon$ . In stabilizing conditions, there is little variability in the binned  
 394 mean and median of scaled  $\varepsilon$  across  $z/L_M$  regimes and the data are poorly described by the MO  
 395 similarity relationships.

396 Measurements of  $\varepsilon$  in destabilizing conditions are shown plotted directly against the  
 397 LOW, surface buoyancy flux, and  $\frac{u_s u_*^2}{h}$  scalings in regimes defined by  $z/L_M$  in Figure 4 and by  
 398  $h/L_L$  in Figure 5. Each scaling is compared only against data that falls in its respective  
 399 dominance regime; for LOW and the Langmuir scaling, this is defined as  $\frac{z}{L_M} < 0.3$  and  $\frac{h}{L_L} < 0.5$   
 400 and for buoyancy-flux,  $\frac{z}{L_M} > 3$  and  $\frac{h}{L_L} > 5$ . A 1:1 line is shown in each panel to represent  
 401 idealized conditions where the scaling and measured  $\varepsilon$  are equivalent. In addition, Equation 13 is  
 402 shown in Figures 4a-b calculated with bin-averaged LOW and  $B_0$ . MO similarity relationships  
 403 are intended to capture the varying influence of shear and buoyancy-driven turbulence along the  
 404 continuum of  $\frac{z}{L_M}$  rather than in discrete regimes, therefore Equation 13 likely better represents

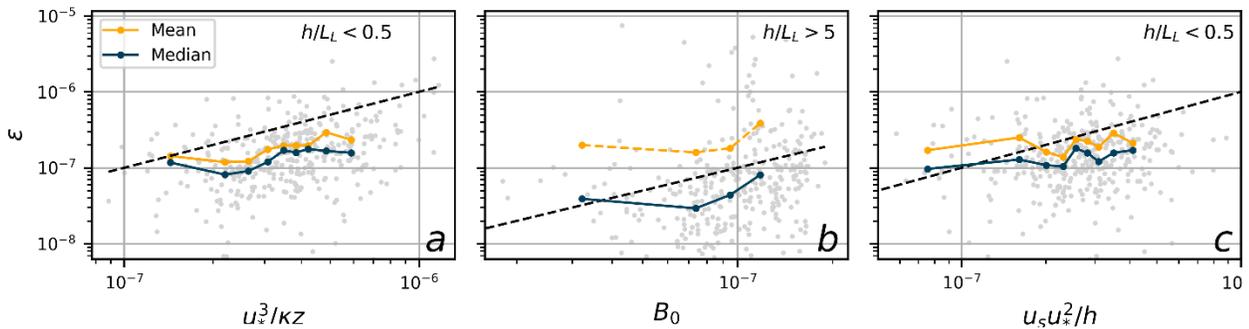


Figure 5 Same as Figure 4 but with regimes defined by  $\frac{h}{L_L} < 0.5$  (buoyancy-dominant regime) and  $\frac{h}{L_L} > 5$  (shear-dominant regime).

405 real conditions than a 1:1 line. Indeed, it better describes the slopes of the bin-averaged mean and  
 406 median than the 1:1 line in Figure 4a, though the comparison is less clear in Figure 4b.

407

Destabilizing conditions	All	$ \frac{h}{L_L}  < 0.5$ (Shear dominant)	$ \frac{z}{L_M}  < 0.3$ (Wind dominant)	$ \frac{h}{L_L}  > 5$ ( $B_0$ dominant)	$ \frac{z}{L_M}  > 3$ ( $B_0$ dominant)
$n$	2226	400	517	368	149
$\epsilon z \kappa / u_*^3$					
Median	0.56	<b>0.40</b>	<b>0.38</b>	1.36	2.86
Mean	2.45	<b>0.67</b>	<b>0.60</b>	10.04	20.90
Q75 – Q25	1.13	<b>0.50</b>	<b>0.48</b>	2.77	6.55
$\epsilon / B_0$					
Median	1.05	1.52	1.60	<b>0.63</b>	<b>0.61</b>
Mean	2.79	3.31	3.87	<b>2.87</b>	<b>2.49</b>
Q75 – Q25	1.96	2.04	2.31	<b>1.16</b>	<b>0.86</b>
$\epsilon h / u_s u_*^2$					
Median	1.32	<b>0.56</b>	<b>0.83</b>	8.10	12.11
Mean	21.20	<b>1.03</b>	<b>6.48</b>	123.75	243.37
Q75 – Q25	3.27	<b>0.62</b>	<b>1.27</b>	20.91	42.50

408

409 **Table 2.** Median, mean, and interquartile range (Q75-Q25) of  $\epsilon$  scaled by the Law of the Wall (Equation 2), surface  
 410 buoyancy flux (Equation 3), and  $u_s u_*^2 / h$  scalings in destabilizing conditions ( $B_0 > 0$ ). Only data away from the  
 411 boundaries of the mixed layer ( $0.135 < \frac{z}{h} < 0.5$ ) are considered.

412

413 To quantify the relationship between each scaling and measured  $\epsilon$ , we present summary  
 414 statistics of scaled  $\epsilon$  in destabilizing conditions (Table 2) and stabilizing conditions (Table 3).  
 415 Statistics are bolded for each scaling in their respective dominance regimes (as defined above).  
 416 LOW consistently scales  $\epsilon$  to an average of  $\sim 0.65$  across destabilizing and stabilizing conditions  
 417 in “shear-dominant” regimes, which we use to describe the wind- and wind-wave-dominant  
 418 regimes defined by  $z/L_M$  and  $h/L_L$ , respectively.  $B_0$  scales  $\epsilon$  to averages of 2.9 and 2.5 in  
 419 destabilizing, buoyancy-dominant conditions defined by  $z/L_M$  and  $h/L_L$ , respectively. The  
 420  $u_s u_*^2 / h$  scaling is less consistent, scaling  $\epsilon$  to averages of 1.03 and 6.5 in stabilizing, shear-  
 421 dominant conditions. Notably, the interquartile range, which contains 50% of all data and  
 422 describes their spread about the median, is reduced for each scaling in its dominant regime  
 423 relative to the entire dataset, and increased in non-dominant regimes. For example, the

424 interquartile range of  $\varepsilon$  scaled by LOW in Table 2 is decreased from  $\sim 1.1$  to  $\sim 0.5$  in the wind-  
 425 dominant regimes but increased to upwards of 2 in the buoyancy-dominant regimes, where the  
 426 scaling is not expected to apply. Effective scalings should collapse measurements of  $\varepsilon$ , so the  
 427 observed decreases in the spread of data supports the use of these scaling as well as the ability of  
 428 the Belcher and MO frameworks to delineate turbulence regimes.

429

Stabilizing conditions	All	$ \frac{h}{L_L} < 0.5 $ (Shear dominant)	$ \frac{z}{L_M} < 0.3 $ (Wind dominant)	$ h/L_L > 5 $ ( $B_0$ dominant)	$ z/L_M > 3 $ ( $B_0$ dominant)
$n$	1064	175	177	318	247
$\varepsilon z \kappa / u_*^3$					
Median	0.34	<b>0.35</b>	<b>0.37</b>	0.38	0.35
Mean	3.41	<b>0.61</b>	<b>0.69</b>	9.55	11.78
Q75 – Q25	0.78	<b>0.49</b>	<b>0.51</b>	0.86	0.97
$\varepsilon h / u_s u_*^2$					
Median	0.77	<b>0.64</b>	<b>0.84</b>	1.10	0.79
Mean	34.89	<b>1.55</b>	<b>2.37</b>	115.65	130.78
Q75 – Q25	1.72	<b>0.76</b>	<b>1.16</b>	4.86	3.48

430

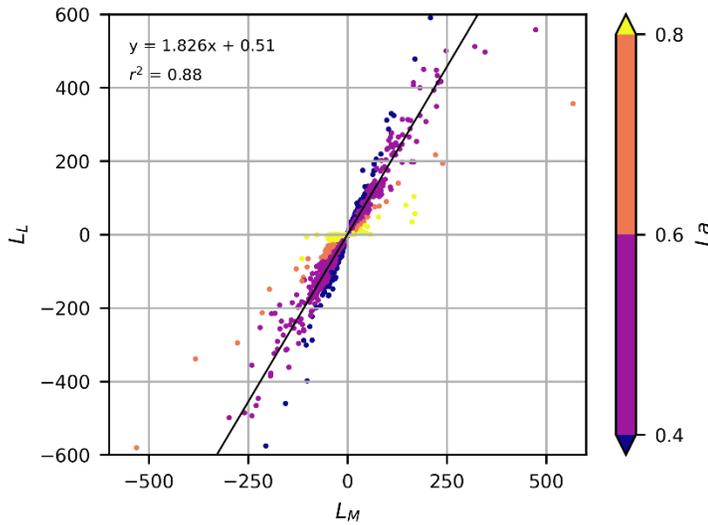
431 Table 3. Same as in Table 2, but in stabilizing conditions ( $B_0 < 0$ ).

432

### 433 3.2.2 Dependence on $La$

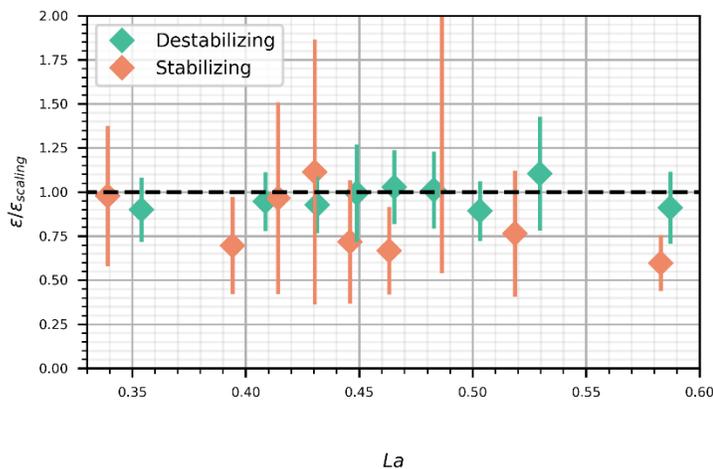
434 That the calculated statistics for LOW and  $B_0$  vary relatively little in Tables 2 and 3  
 435 between  $z/L_M$  and  $h/L_L$  regimes suggests that the distinction between a wind-dominant regime,  
 436 defined by  $z/L_M$ , and a Langmuir-dominant regime, defined by  $h/L_L$ , is unimportant in the  
 437 Stratus region. This is tied to the low variability seen in  $La$  over most of the study period, which  
 438 results in the linear dependency between  $L_L$  and  $L_M$  ( $L_M \propto La^{-2} L_L$ ) shown in Figure 6. This  
 439 relationship is described well by a least squares regression with a slope of 1.83 and an  $r^2$  value  
 440 of 0.88. Figure 7 shows  $\varepsilon$  scaled by Equation 13, calculated from binned values of LOW and  $B_0$ ,  
 441 in  $La$  space. Scaling by Equation 13 removes variability tied to  $B_0$  and  $u_*$ , so if Langmuir effects  
 442 were not sufficiently accounted for by LOW, we would expect to see a large deviation from  
 443 unity at lower values of  $La$ , where Langmuir forcing is stronger. Instead, there is very little

444 variability in  $La$  space, suggesting that  $La$  offers little to no additional predictive power over  $u_*$   
 445 at this field site.



446 **Figure 6.** Least squares linear regression of  $L_L$  against  $L_M$ , illustrating the relationship  $L_M \propto La^{-2}L_L$ . Colors highlight the  
 447 variation in slope associated with different values of binned  $La$ .

448 Furthermore, for  $\varepsilon$  scaled by LOW, we see little change in calculated statistics in the  
 449 shear-dominant regime in both destabilizing and stabilizing conditions when data coinciding  
 450 with lower  $La$  values are excluded (Table 4). The median of scaled  $\varepsilon$  increases slightly from 0.4  
 451 to 0.54 in destabilizing conditions and remains  $\sim 0.3$  in stabilizing conditions, regardless of the  
 452 degree of exclusion. In destabilizing conditions, the mean increases as more data are excluded,  
 453 but only because the influence of several outlying data points on the mean is strengthened with  
 454 increasingly fewer data points.



455 **Figure 7.** Bin-averaged measurements of  $\varepsilon$  (away from the boundaries of the mixed layer;  $0.135 < \frac{z}{h} < 0.5$ ) scaled by  
 456 Equation 13 in destabilizing conditions and Law of the Wall (Equation 2) in stabilizing conditions across  $La$  space.  
 457 Because Equation 13 was fitted to data in which the highest and lowest 1% of values were excluded, the same filter is  
 458 applied to the data in destabilizing conditions shown here. Each bin contains the same number of points. Vertical bars  
 459 show the 95% confidence interval (1.96 multiplied by the standard error) of each bin.

$$\varepsilon z \kappa / u_*^3$$

		Excluding $La < 0.4$	Excluding $La < 0.45$	Excluding $La < 0.5$
$B_0 > 0,$ $\left  \frac{h}{L_L} \right  < 0.5$				
$n$	400	300	167	59
Median	0.40	0.42	0.44	0.54
Mean	0.67	0.72	0.82	1.26
Q75 – Q25	0.50	0.51	0.52	0.60
$B_0 < 0,$ $\left  \frac{h}{L_L} \right  < 0.5$				
$n$	175	132	77	38
Median	0.35	0.34	0.29	0.29
Mean	0.61	0.67	0.66	0.68
Q75 – Q25	0.49	0.49	0.54	0.72

461

462 Table 4. Median, mean, and interquartile range (Q75-Q25) calculated for  $\varepsilon$  scaled by LOW where subsets of data defined  
 463 using the Langmuir number,  $La$ , are excluded in order to explore the distinction between Langmuir and current shear-  
 464 forced regimes in our data. Only data that fall away from the boundaries of the mixed layer ( $0.135 < \frac{z}{h} < 0.5$ ) are  
 465 considered.

466

#### 467 4 Discussion

468 The Stratus region is characterized by directionally-steady southeast trade winds (Weller et  
 469 al., 2014), which likely contributes to the observed linear relationship between  $u_s$  and  $u_*$  and an  
 470 overall narrow range in  $La$  across the study period. The stronger the relationship between  $u_s$  and  
 471  $u_*$ , the more functionally equivalent  $w_{*L}$  and  $u_*$  become, a concept noted by Gargett and Grosch  
 472 (2014). Therefore, at the Stratus mooring site, there appears to be little need to distinguish  
 473 between wind-driven current shear- and Langmuir- dominant regimes in the context of  
 474 turbulence scaling. We see a strong linear relationship between  $L_M$  and  $L_L$  and little difference in  
 475 the normalization of  $\varepsilon$  by traditional MO scalings in regimes defined by  $\frac{h}{L_L}$  compared to  $\frac{z}{L_M}$ . The  
 476 mean, median, and interquartile range of  $\varepsilon \kappa z / u_*^3$  are nearly identical across  $\frac{h}{L_L}$  and  $\frac{z}{L_M}$  wind-  
 477 dominant regimes in both destabilizing and stabilizing conditions, as are the statistics for  $\varepsilon / B_0$   
 478 for both buoyancy-dominant regimes in destabilizing conditions. The ability to consider current  
 479 shear- and Langmuir-dominant regimes as a single “wind-wave”, or “shear-dominant”, regime,  
 480 irrespective of  $La$ , may be relevant in efforts to improve the performance of coupled atmosphere-  
 481 ocean general circulation models (GCMs) in the region, which suffer from systematic warm SST  
 482 biases, in part due to poorly constrained upper-ocean processes (Lin, 2007; Ma et al., 1996;

483 Mechoso et al., 1995; Richter, 2015; Zheng et al., 2011; Zuidema et al., 2016). This may also be  
484 broadly applicable to turbulence scaling outside of the steadily-forced Stratus region: in a study  
485 of dissipation rates from microstructure profiler deployments at several sites ranging from the  
486 Arctic Ocean to the subtropical Atlantic ocean, Esters et al. (2018) found that the observed linear  
487 relationship between  $u_*$  and  $u_s$  allowed them to describe their data using a version of Equation 8  
488 in which  $u_s$  is substituted by  $u_*$  multiplied by a constant factor.

489 While our analysis shows that  $\varepsilon$  scaling is not sensitive to the  $La$  regime, this does not mean  
490 that Langmuir circulation/turbulence is unimportant in the Stratus region, only that it is  
491 sufficiently accounted for by  $u_*$  (because of the linear relationship between  $u_*$  and  $u_s$ ).  
492 Langmuir scaling has not been widely examined outside of modelling studies because of the  
493 difficulty in obtaining quality wave data concurrently with in-situ measurements of  $\varepsilon$ . That  
494  $u_s u_*^2 / h$  appears to scale  $\varepsilon$  closer to unity than LOW for much of November-April (Figure 1a),  
495 which is perhaps surprising, as this scaling is a relatively new development (Grant and Belcher,  
496 2009) and limited observational studies of the TKE budget have disagreed on the magnitude of  
497 the stokes production term relative to the dissipation term (Gerbi et al., 2009; Jarosz et al., 2021;  
498 Yoshikawa et al., 2018). Regardless, by June, the wind-sea weakens (monthly-averaged  $H_{sw}$  is  
499 0.86m compared to  $\sim 1.2$ m across the whole study period) and the scaling grossly underestimates  
500  $\varepsilon$ . Filtering out values of  $H_{sw} < 1$ , as well as  $U_{10} < 5$  and  $u_s < 0.03$ , which would coincide  
501 with conditions of weak Langmuir forcing, does not systemically separate instances of  
502 significant underestimation of  $\varepsilon$  by  $u_s u_*^2 / h$  from instances where it performs well. Therefore, as  
503 discussed below, LOW serves as a more reliable scaling for  $\varepsilon$  in shear-dominant conditions, as  
504 its overestimation bias is fairly consistent and more easily corrected for.

505 In general, MO similarity works well in describing turbulence at the Stratus mooring site:  
506 LOW collapses the scatter of  $\varepsilon$  and scales it to an average of  $\sim 0.65$  in shear-dominant conditions  
507 across both destabilizing and stabilizing conditions. The scaling of  $\varepsilon$  close to, but not exactly,  
508 unity is not uncommon in observational studies. For example, Callaghan et al. (2014) suggested  
509 that an observed overestimation of  $\varepsilon$  by LOW was due to a period of continually changing wind  
510 direction in which a misalignment of the wind and wave field reduced the effective wind stress  
511 on the ocean. Tedford et al., (2014) attributed overestimation by LOW in a lake setting to  
512 enhanced stratification brought on by the lateral advection of cool water. In our own data, we  
513 also see individual instances where LOW departs significantly from measurements of  $\varepsilon$ . For  
514 example, in mid-February and throughout June, LOW tracks a sudden dip in wind speed  
515 characteristic to the Stratus region, while measured  $\varepsilon$  remains at relatively elevated levels  
516 (Figure 1). These dips in wind speed have been observed to generate near-inertial oscillations  
517 (Weller et al., 2014) that can alter currents and impact the turbulence regime through the  
518 generation of additional current shear. Additionally, the persistence of the wind-sea and  
519 associated Langmuir circulation following a drop in winds can create a lag between wind stress  
520 and  $\varepsilon$ . However, there are also instances where measured  $\varepsilon$  plummets following a drop to near-  
521 zero winds (e.g. mid-January, mid April, early May), a change that is tracked remarkably well by  
522 LOW. While these sudden, short-term drops in wind speed do add some short-term complexity  
523 to the scaling of  $\varepsilon$ , the slight overestimation represented by the average  $\frac{\varepsilon_{KZ}}{u_*^3} = 0.65$  across the

524 study period appears more systematic than the individual instances of dips in wind speed, and we  
525 hypothesize some possible causes: LES studies have shown the enhancement of vertical mixing  
526 associated with Langmuir circulation reduces vertical shear in the upper ocean, thus inhibiting  
527 current shear production of TKE (Belcher et al., 2012; Fan et al., 2020) and therefore reducing  $\varepsilon$   
528 relative to the wind stress. Another possibility relates to the assumption of a constant stress layer  
529 upon which MO similarity theory and LOW rely. Observations (Gerbi et al., 2008) and linear  
530 surface stress scaling (e.g. Fisher et al., 2017) show stress to decay with depth according to  $\tau_z =$   
531  $\tau(1 - \frac{z}{h})$ , suggesting LOW calculated from  $\tau$  at the surface would overestimate shear  
532 turbulence at depth. When calculating LOW using decayed stress,  $\tau_z$ , our measurements of  $\varepsilon$   
533 (within the same  $0.135 < \frac{z}{h} < 0.5$  range as before) are scaled with averages of 1.28 and 1.01  
534 where  $|\frac{h}{L_L}| < 0.5$  and 0.95 and 1.04 where  $|\frac{z}{L_M}| < 0.3$ , in destabilizing and stabilizing  
535 conditions, respectively. These values are notably closer to unity than  $\sim 0.65$ . There is little  
536 reason to assume the constant stress layer assumption holds at the 8.4 m depth of our  
537 measurements, and these calculations suggest that stress decay may be a factor in the deviation  
538 of the scaling of  $\varepsilon$  by LOW from unity in real-world conditions. Nevertheless, our results support  
539 the merit of classic MO scaling despite a possible violation of the constant stress layer  
540 assumption. Future work is needed to more fully assess if full flux-profile relationships are  
541 tenable outside of the constant stress layer, but within the ocean surface mixed layer.

542 As for the buoyancy flux scaling, scatter is collapsed in destabilizing, buoyancy-dominant  
543 conditions, but  $\varepsilon$  is overestimated by an average of  $\sim 2.5$ . The median of  $\sim 0.6$  is closer to unity  
544 and the findings of other studies, such as  $\sim 0.58$  in Lombardo and Gregg (1989) and 0.81 in (Anis  
545 and Moum, 1992), and indicates that most of the data are scaled near unity but that the mean is  
546 influenced by extreme outliers. This is likely the case because the Stratus mooring site does not  
547 experience true buoyancy-dominant conditions, which are typically defined as  $|z/L_M| > 10$  (e.g.  
548 Lombardo and Gregg, 1989). Out of necessity, we defined a less conservative threshold of  
549  $|z/L_M| > 3$ , which likely resulted in the influence of turbulent processes not captured by  $B_0$ .

550 Scaling relationships from prior studies describe the binned mean of our data well for  
551 destabilizing conditions of  $|\frac{z}{L_M}| < 1$  (wind-dominant), except for those of Lombardo and Gregg  
552 (1989) and Wyngaard and Cote (1971). Lombardo and Gregg (1989) may differ from the other  
553 aquatic studies because it utilized a descending microstructure profiler that necessarily excluded  
554 data 5-10 meters near the surface, possibly excluding wave-related turbulence otherwise captured  
555 in our data and studies utilizing ascending profilers. Likewise, Edson and Fairall (1998),  
556 conducted in the ABL above the ocean, may have been influenced by wave activity while  
557 Wyngaard and Cote (1971) did not. Regardless, all of the relationships deviate from the binned  
558 mean of our data in destabilizing conditions of  $|\frac{z}{L_M}| > 2$ . This could be because in general, fewer  
559 data exist at greater values of  $|\frac{z}{L_M}|$ , making statistics and linear regressions derived from these  
560 data less universal. Furthermore, similarity relationship with coefficients derived from the  
561 scaling of  $\varepsilon$  by LOW and  $B_0$  ostensibly describe wind-generated current shear and convective  
562 turbulence, but inadvertently capture the effects of many other processes that are potentially

563 unique to the place and time of data collection, with the intermittent nature of turbulence adding  
564 additional complexity. Data collected in studies using microstructure profilers represent  
565 snapshots in time and are therefore perhaps more susceptible to this temporal and spatial  
566 variability, resulting in the large spread of functions derived from field estimates of  $\varepsilon$ .

## 567 **5 Conclusion**

568 Moored, pulse-coherent ADCP measurements of  $\varepsilon$  are a useful development in the study of  
569 ocean turbulence, allowing for analysis of turbulence across an extended range of conditions and  
570 length of time at a single site. Here, we use similarity scaling to explore 9 months of moored  
571 measurements of  $\varepsilon$  across a range of forcing conditions in the upper mixed layer of the Stratus  
572 mooring site. We find that:

- 573 • LOW scales  $\varepsilon$  well in shear-dominant conditions across both destabilizing and stabilizing  
574 conditions, as determined by a) its ability to collapse measurements of  $\varepsilon$  and b) the  
575 proximity of the mean or median of scaled  $\varepsilon$  to unity
- 576 •  $B_0$  scales  $\varepsilon$  well in buoyancy-dominant conditions in destabilizing conditions, by the  
577 same standards as above
- 578 •  $u_s u_*^2 / h$  scales  $\varepsilon$  well for a large portion of the study period, but does very poorly in May  
579 and June. It is difficult to parse out the conditions in which it performs well, therefore  
580 LOW remains the more useful scaling in shear-dominant conditions
- 581 •  $h/L_L$  and  $z/L_M$  are functionally equivalent means for separating the shear-dominant  
582 regime from the buoyancy-dominant regime in the Stratus region because of the strong  
583 linear relationship between  $u_*$  and  $u_s$
- 584 • Prior scaling relationships largely agree with our measurements in destabilizing  
585 conditions of  $|z/L_M| < 1$ , but their deviation elsewhere highlights how field estimates of  $\varepsilon$   
586 are susceptible to variability across space and time

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## 597 **Open Research**

598 Velocity, correlation, amplitude, and other outputs from the 2 MHz Nortek AquaDopp  
599 High-Resolution (HR) Pulse-Coherent ADCP are available at <https://doi.org/10.7916/xs7h-b561>.  
600 Data from the Stratus Ocean Reference Station are made freely available by the OceanSITES  
601 project (Send et al., 2010) and the national programs that contribute to it, and are obtained from  
602 <https://dods.ndbc.noaa.gov/oceansites/>). Wave data are hosted by the National Buoy Data Center

603 and are obtained at [https://www.ndbc.noaa.gov/station\\_page.php?station=32012](https://www.ndbc.noaa.gov/station_page.php?station=32012). The MATLAB  
604 code used to quality control the ADCP data and calculate  $\varepsilon$  is available on GitHub at:  
605 <https://github.com/zippelsf/MooredTurbulenceMeasurements>. The Python code used to process  
606 meteorological and wave data and to generate figures is available from the author upon request.

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