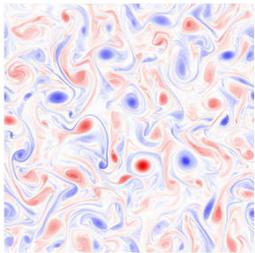




Data-driven Subgrid-scale Models for 2D forced Turbulence

Data

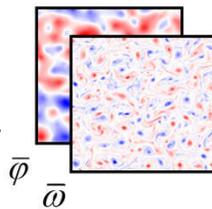
ω , $kf=10$, $NX=1024$



2D forced turbulence flow is solved using a pseudo-spectral method. $Re=20,000$.

Filtering

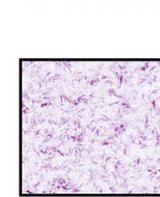
$$\bar{U}(x) = \int_{-\infty}^{\infty} G(r)U(x-r)dr$$



CNN

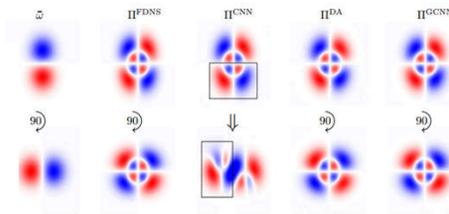
Convolutional layers

Convolutional layers



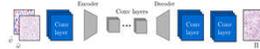
$$\text{Closure term: } \Pi = J(\bar{\varphi}, \bar{\omega}) - \overline{J(\varphi, \omega)}$$

Illustration of translational and rotational equivariance



A posteriori analysis (GCNN)

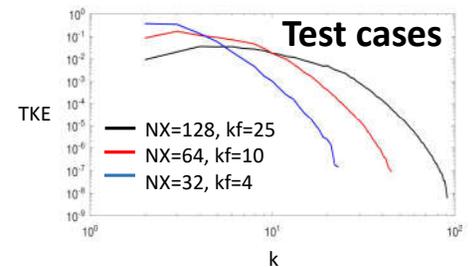
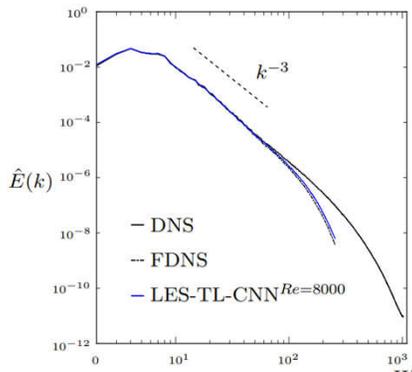
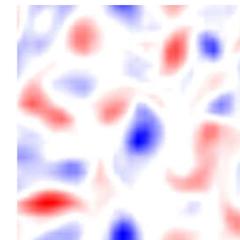
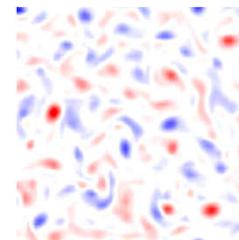
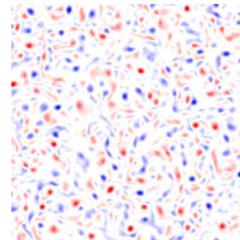
Transfer learning



$kf=25$, $NX=128$

$kf=10$, $NX=64$

$kf=4$, $NX=32$



- [1] Guan, Yifei, Ashesh Chattopadhyay, Adam Subel, and Pedram Hassanzadeh. "Stable a posteriori LES of 2D turbulence using convolutional neural networks: Backscattering analysis and generalization to higher Re via transfer learning." *arXiv preprint arXiv:2102.11400* (2021)
- [2] Subel, Adam, Ashesh Chattopadhyay, Yifei Guan, and Pedram Hassanzadeh. "Data-driven subgrid-scale modeling of forced Burgers turbulence using deep learning with generalization to higher Reynolds numbers via transfer learning." *Physics of Fluids* 33, no. 3 (2021): 031702.