

# Supporting Information for "Conductance Model for Extreme Events : Impact of Auroral Conductance on Space Weather Forecasts"

Agnit Mukhopadhyay<sup>1</sup>, Daniel T. Welling<sup>2</sup>, Michael W. Liemohn<sup>1</sup>, Aaron J.

Ridley<sup>1</sup>, Shibaji Chakraborty<sup>3</sup>, and Brian J. Anderson<sup>4</sup>

<sup>1</sup>Climate and Space Sciences and Engineering Department, University of Michigan, Ann Arbor, MI, USA

<sup>2</sup>Department of Physics, University of Texas at Arlington, Arlington, TX, USA

<sup>3</sup>Department of Electrical and Computer Engineering, Virginia Polytechnic Institute and State University, Blacksburg, VA, USA

<sup>4</sup>Applied Physics Laboratory, Johns Hopkins University, Baltimore, MD, USA

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1. Tables S1 to S15

**Introduction** This supporting information provides performance metrics calculated for multiple  $dB/dt$  and  $\Delta B$  thresholds using the Conductance Model for Extreme Events. The metrics used has been listed in Table 2 of the main article. The format of these tables are similar to Tables 4 and 5 of the main article; for more details about those tables, please refer to Sections 3.2 and 3.3 of the main paper. For convenience, the tables have been coloured differently: In the tables, ***italicized-bolded*** text is used to denote best performance while **italicized-underlined** text is used to denote worst. Usage of the auroral oval and CMEE amounts to an increase in False Negatives (F) in both  $\Delta B$  and  $dB/dt$

predictions, while improving the rest of the quantities (H, M, N). Due to this reason, the FAR values are higher for oval runs, which results in less predictive score using the TSS metric. The new model (without the oval) has more misses (M) than the older model (without the oval), when predicting  $\Delta B$ . For  $dB/dt$  predictions, the amount of skill lost during quieter activity, when simulating using CMEE, is more than regained with massive improvements for extreme driving, as is seen by Tables S3 to S7.

**Table S1. Performance metrics for predicted  $dB/dt$  at Threshold = 0.1 nT/s.**

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	0.7776	0.7801	<b>0.8436</b>	0.8114	0.8342	0.8555	<b>0.8976</b>	0.8973
POFD	0.0631	<b>0.0615</b>	<u>0.0903</u>	0.0744	0.0938	<b>0.0892</b>	0.1687	<u>0.1697</u>
FAR	0.0431	<b>0.0419</b>	<u>0.0560</u>	0.0484	0.0587	<b>0.0547</b>	0.0944	<u>0.0950</u>
MR	0.2997	0.2970	<b>0.2367</b>	0.2686	0.2481	0.2224	<b>0.1817</b>	0.1823
TS	0.7513	0.7544	<b>0.8034</b>	0.7793	0.7929	0.8152	<b>0.8208</b>	0.8201
F1	<u>0.8580</u>	0.8600	<b>0.8910</b>	0.8760	0.8845	0.8982	<b>0.9016</b>	0.9012
TSS	0.6572	0.6611	<b>0.7073</b>	0.6830	0.6932	0.7229	<b>0.7239</b>	0.7227
HSS	0.6645	0.6687	<b>0.7225</b>	0.6959	0.7080	<b>0.7381</b>	0.7263	0.7251

**Table S2. Performance metrics for predicted  $dB/dt$  at Threshold = 0.3 nT/s.**

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	0.5814	<u>0.5628</u>	<b>0.6782</b>	0.6638	0.6444	0.6829	0.7970	<b>0.7979</b>
POFD	0.0416	<b>0.0345</b>	<u>0.0597</u>	0.0477	<b>0.0426</b>	0.0613	0.1038	<u>0.1164</u>
FAR	0.0858	<b>0.0744</b>	<u>0.1034</u>	0.0861	<b>0.0797</b>	0.1053	0.1459	<u>0.1606</u>
MR	0.2499	<u>0.2567</u>	<b>0.2070</b>	0.2121	0.2207	0.2049	<b>0.1473</b>	0.1485
TS	0.5513	<u>0.5384</u>	<b>0.6290</b>	0.6248	0.6103	0.6321	<b>0.7015</b>	0.6922
F1	0.7108	<u>0.7000</u>	<b>0.7723</b>	0.7690	0.7580	0.7746	<b>0.8246</b>	0.8181
TSS	<u>0.6644</u>	0.6689	0.6896	<b>0.7017</b>	0.6996	<u>0.6899</u>	<b>0.7068</b>	0.6909
HSS	0.5642	<u>0.5541</u>	<b>0.6370</b>	0.6368	0.6240	0.6396	<b>0.6987</b>	0.6855

**Table S3. Performance metrics for predicted  $dB/dt$  at Threshold = 0.5 nT/s.**

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	0.4812	0.4840	0.5636	<b>0.5922</b>	0.5496	0.5989	0.7244	<b>0.7451</b>
POFD	0.0331	<b>0.0302</b>	<u>0.0497</u>	0.0435	<b>0.0378</b>	0.0543	0.0926	<u>0.1076</u>
FAR	0.1244	<b>0.1138</b>	<u>0.1539</u>	0.1315	<b>0.1241</b>	0.1576	0.2087	<u>0.2294</u>
MR	<u>0.2065</u>	0.2051	0.1821	<b>0.1713</b>	0.1850	0.1706	0.1284	<b>0.1217</b>
TS	<u>0.4504</u>	0.4557	0.5112	<b>0.5434</b>	0.5099	0.5385	0.6082	<b>0.6098</b>
F1	<u>0.6211</u>	0.6261	0.6765	<b>0.7042</b>	0.6754	0.7001	0.7564	<b>0.7576</b>
TSS	<u>0.6692</u>	0.6811	0.6640	<b>0.6972</b>	<b>0.6909</b>	0.6718	0.6629	<u>0.6489</u>
HSS	<u>0.5069</u>	0.5139	0.5622	<b>0.5977</b>	0.5661	0.5883	<b>0.6458</b>	0.6430

**Table S4.** Performance metrics for predicted  $dB/dt$  at Threshold = 0.7 nT/s.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.3949</u>	0.4278	0.4661	<b>0.5305</b>	<u>0.4812</u>	0.5441	0.6537	<b>0.7057</b>
POFD	<b>0.0255</b>	0.0260	0.0365	<u>0.0387</u>	<b>0.0285</b>	0.0442	0.0801	<u>0.0936</u>
FAR	0.1502	<b>0.1427</b>	<u>0.1765</u>	<u>0.1667</u>	<b>0.1395</b>	0.1821	0.2516	<u>0.2667</u>
MR	<u>0.1847</u>	0.1765	<u>0.1681</u>	<b>0.1512</b>	<u>0.1630</u>	0.1482	0.1208	<b>0.1059</b>
TS	<u>0.3692</u>	0.3994	0.4238	<b>0.4796</b>	<u>0.4463</u>	0.4853	0.5359	<b>0.5615</b>
F1	<u>0.5393</u>	0.5708	0.5953	<b>0.6483</b>	<u>0.6172</u>	0.6535	0.6978	<b>0.7192</b>
TSS	<u>0.6651</u>	0.6809	0.6553	<b>0.6821</b>	<b>0.6974</b>	0.6697	0.6277	<u>0.6274</u>
HSS	<u>0.4451</u>	0.4779	0.4983	<b>0.5559</b>	<u>0.5264</u>	0.5594	0.5975	<b>0.6195</b>

**Table S5.** Performance metrics for predicted  $dB/dt$  at Threshold = 1.1 nT/s.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.2920</u>	0.3310	0.3520	<b>0.4380</b>	<u>0.3770</u>	0.4440	0.5300	<b>0.6230</b>
POFD	<b>0.0222</b>	0.0235	0.0284	<u>0.0372</u>	<b>0.0273</b>	0.0434	0.0687	<u>0.0914</u>
FAR	0.2532	<b>0.2408</b>	0.2651	<u>0.2748</u>	<b>0.2445</b>	0.3041	0.3668	<u>0.3957</u>
MR	<u>0.1395</u>	0.1330	0.1299	<b>0.1156</b>	<u>0.1254</u>	0.1152	0.1015	<b>0.0850</b>
TS	<u>0.2657</u>	0.2995	0.3123	<b>0.3756</b>	<u>0.3360</u>	0.3719	0.4055	<b>0.4425</b>
F1	<u>0.4198</u>	0.4610	0.4760	<b>0.5461</b>	<u>0.5030</u>	0.5421	0.5770	<b>0.6135</b>
TSS	0.6073	<b>0.6262</b>	<u>0.6049</u>	0.6096	<b>0.6301</b>	0.5808	0.5317	<u>0.5193</u>
HSS	<u>0.3533</u>	0.3936	0.4056	<b>0.4736</b>	<u>0.4341</u>	0.4660	0.4924	<b>0.5253</b>

**Table S6.** Performance metrics for predicted  $dB/dt$  at Threshold = 1.5 nT/s.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.2216</u>	0.2490	0.2668	<b>0.3557</b>	<u>0.2791</u>	0.3406	0.4309	<b>0.5554</b>
POFD	<b>0.0169</b>	0.0194	0.0253	<u>0.0319</u>	<b>0.0262</b>	0.0378	0.0566	<u>0.0784</u>
FAR	<b>0.3306</b>	0.3358	<u>0.3810</u>	0.3674	<b>0.3780</b>	0.4182	0.4597	<u>0.4775</u>
MR	<u>0.1089</u>	0.1057	0.1041	<b>0.0932</b>	<u>0.1026</u>	0.0957	0.0852	<b>0.0693</b>
TS	<u>0.1998</u>	0.2211	0.2291	<b>0.2948</b>	<u>0.2386</u>	0.2736	0.3153	<b>0.3684</b>
F1	<u>0.3330</u>	0.3622	0.3728	<b>0.4553</b>	<u>0.3853</u>	0.4297	0.4795	<b>0.5385</b>
TSS	<b>0.5605</b>	0.5585	<u>0.5150</u>	0.5394	<b>0.5194</b>	0.4861	0.4551	<u>0.4532</u>
HSS	<u>0.2855</u>	0.3120	0.3179	<b>0.3973</b>	<u>0.3297</u>	0.3672	0.4094	<b>0.4647</b>

**Table S7.** Performance metrics for predicted  $dB/dt$  at Threshold = 1.7 nT/s.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.1975</u>	0.2070	0.2389	<b>0.3264</b>	<u>0.2452</u>	0.3153	0.3838	<b>0.5207</b>
POFD	0.0161	<b>0.0155</b>	0.0238	<u>0.0287</u>	<b>0.0246</b>	0.0356	0.0529	<u>0.0754</u>
FAR	0.3861	<b>0.3659</b>	<u>0.4340</u>	0.4041	<b>0.4359</b>	0.4649	0.5151	<u>0.5275</u>
MR	<u>0.0957</u>	0.0947	0.0919	<b>0.0826</b>	<u>0.0913</u>	0.0844	0.0779	<b>0.0630</b>
TS	<u>0.1756</u>	0.1849	0.2019	<b>0.2673</b>	<u>0.2062</u>	0.2475	0.2726	<b>0.3293</b>
F1	<u>0.2988</u>	0.3121	0.3359	<b>0.4218</b>	<u>0.3418</u>	0.3968	0.4284	<b>0.4955</b>
TSS	0.5181	<b>0.5395</b>	<u>0.4741</u>	0.5133	<b>0.4728</b>	0.4508	<u>0.4070</u>	0.4095
HSS	<u>0.2573</u>	0.2709	<u>0.2874</u>	<b>0.3706</b>	<u>0.2926</u>	0.3406	<u>0.3639</u>	<b>0.4264</b>

**Table S8.** Performance metrics for predicted  $\Delta B$  at Threshold = 100 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.7293</u>	0.7918	<b>0.8099</b>	0.7879	0.8603	<u>0.8373</u>	<b>0.8882</b>	0.8740
POF	<b>0.1882</b>	0.2296	<u>0.3074</u>	0.2836	0.3388	<b>0.3199</b>	<u>0.4442</u>	0.4003
FAR	<b>0.1013</b>	0.1124	<u>0.1422</u>	0.1358	0.1467	<b>0.1430</b>	<u>0.1792</u>	0.1667
MR	<u>0.4330</u>	<b>0.3823</b>	<u>0.3860</u>	0.4040	0.3261	<u>0.3540</u>	<b>0.3153</b>	0.3249
TS	<u>0.6739</u>	<b>0.7196</b>	0.7140	0.7011	<b>0.7494</b>	<u>0.7346</u>	0.7439	0.7439
F1	<u>0.8052</u>	<b>0.8370</b>	0.8331	0.8243	<b>0.8568</b>	<u>0.8470</u>	0.8532	0.8532
TSS	0.4658	<b>0.5053</b>	0.4718	<u>0.4602</u>	<b>0.5272</b>	<u>0.5030</u>	0.5055	0.5085
HSS	0.4825	<b>0.5256</b>	0.4850	<u>0.4772</u>	<b>0.5243</b>	0.5097	<u>0.4689</u>	0.4891

**Table S9.** Performance metrics for predicted  $\Delta B$  at Threshold = 150 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.6803</u>	0.7440	<b>0.7534</b>	0.7460	0.8184	<u>0.7842</u>	<b>0.8599</b>	0.8432
POF	<b>0.1186</b>	0.1460	<u>0.2487</u>	0.2186	0.2743	<b>0.2469</b>	<u>0.3823</u>	0.3354
FAR	<b>0.1166</b>	0.1294	<u>0.2000</u>	0.1816	0.2025	<b>0.1925</b>	<u>0.2519</u>	0.2315
MR	<u>0.3238</u>	<b>0.2836</b>	0.3024	0.3003	0.2484	<u>0.2745</u>	<b>0.2304</b>	0.2376
TS	<u>0.6242</u>	<b>0.6699</b>	0.6340	0.6400	<b>0.6776</b>	<u>0.6606</u>	0.6668	0.6724
F1	<u>0.7686</u>	<b>0.8023</b>	0.7760	0.7805	<b>0.8078</b>	<u>0.7956</u>	0.8001	0.8041
TSS	0.5595	<b>0.5870</b>	<u>0.4976</u>	0.5181	<b>0.5491</b>	0.5329	<u>0.5177</u>	0.5309
HSS	0.5418	<b>0.5843</b>	<u>0.5000</u>	0.5200	<b>0.5463</b>	0.5348	<u>0.4893</u>	0.5158

**Table S10.** Performance metrics for predicted  $\Delta B$  at Threshold = 200 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.6331</u>	0.6846	<b>0.7241</b>	0.7128	0.7812	<u>0.7466</u>	<b>0.8142</b>	0.8045
POF	<b>0.0711</b>	0.1117	<u>0.1697</u>	0.1523	0.2059	<b>0.1929</b>	<u>0.3183</u>	0.2683
FAR	<b>0.1107</b>	0.1532	<u>0.2063</u>	0.1916	0.2263	<b>0.2228</b>	<u>0.3025</u>	0.2701
MR	<u>0.2625</u>	0.2424	<b>0.2305</b>	0.2339	0.1990	<u>0.2206</u>	0.1973	<b>0.1941</b>
TS	<u>0.5869</u>	0.6092	0.6093	<b>0.6098</b>	<b>0.6359</b>	0.6150	<u>0.6017</u>	0.6200
F1	<u>0.7397</u>	0.7571	0.7573	<b>0.7576</b>	<b>0.7774</b>	0.7616	<u>0.7513</u>	0.7654
TSS	<b>0.6267</b>	0.6043	<u>0.5631</u>	0.5744	<b>0.5747</b>	0.5566	<u>0.5002</u>	0.5358
HSS	0.5702	<b>0.5784</b>	<u>0.5568</u>	0.5638	<b>0.5750</b>	0.5548	<u>0.4918</u>	0.5335

**Table S11.** Performance metrics for predicted  $\Delta B$  at Threshold = 250 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<u>0.5774</u>	0.6071	<b>0.6998</b>	0.6692	0.7686	<u>0.7180</u>	0.7830	<b>0.7887</b>
POF	<b>0.0527</b>	0.0799	<u>0.1231</u>	0.1129	<b>0.1504</b>	<u>0.1504</u>	<b>0.2621</b>	0.2265
FAR	<b>0.1208</b>	0.1656	<u>0.2095</u>	0.2027	<b>0.2277</b>	0.2399	<u>0.3352</u>	0.3020
MR	<u>0.2284</u>	0.2208	<b>0.1851</b>	0.1984	<b>0.1531</b>	<u>0.1805</u>	0.1633	0.1535
TS	<u>0.5350</u>	0.5418	<b>0.5903</b>	0.5719	<b>0.6267</b>	0.5853	<u>0.5613</u>	0.5880
F1	<u>0.6971</u>	0.7028	<b>0.7424</b>	0.7277	<b>0.7705</b>	0.7384	<u>0.7191</u>	0.7406
TSS	<b>0.6508</b>	0.6136	<u>0.6054</u>	0.5989	<b>0.6193</b>	0.5796	<u>0.5015</u>	0.5445
HSS	0.5569	<u>0.5524</u>	<b>0.5881</b>	0.5717	<b>0.6188</b>	0.5729	<u>0.5058</u>	0.5502

**Table S12.** Performance metrics for predicted  $\Delta B$  at Threshold = 300 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	0.5553	<u>0.5422</u>	<b>0.6254</b>	0.6145	0.7021	<u>0.6703</u>	0.7393	<b>0.7426</b>
POF	<b>0.0456</b>	0.0562	<u>0.0960</u>	0.0866	<b>0.1194</b>	0.1229	<u>0.2054</u>	0.1949
FAR	<b>0.1333</b>	0.1624	<u>0.2231</u>	0.2087	<b>0.2414</b>	0.2555	<u>0.3421</u>	0.3294
MR	0.1993	<u>0.2058</u>	<b>0.1812</b>	0.1840	0.1531	<u>0.1672</u>	0.1491	<b>0.1459</b>
TS	0.5116	<u>0.4906</u>	<b>0.5302</b>	0.5287	<b>0.5739</b>	0.5450	<u>0.5340</u>	0.5441
F1	0.6769	<u>0.6582</u>	<b>0.6930</b>	0.6917	<b>0.7292</b>	0.7055	<u>0.6962</u>	0.7048
TSS	<b>0.6674</b>	0.6318	<u>0.5956</u>	0.6073	<b>0.6055</b>	0.5773	<u>0.5088</u>	0.5248
HSS	0.5562	<u>0.5295</u>	0.5546	<b>0.5568</b>	<b>0.5930</b>	0.5604	<u>0.5190</u>	0.5344

**Table S13.** Performance metrics for predicted  $\Delta B$  at Threshold = 350 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	0.5076	<u>0.4810</u>	<b>0.5711</b>	0.5698	0.6345	<u>0.6193</u>	0.6904	<b>0.6967</b>
POF	0.0529	<b>0.0507</b>	<u>0.0752</u>	0.0725	<b>0.1041</b>	0.1052	<u>0.1750</u>	0.1696
FAR	<b>0.1952</b>	0.1970	<u>0.2347</u>	0.2285	<b>0.2764</b>	0.2834	<u>0.3711</u>	0.3616
MR	0.1826	<u>0.1902</u>	<b>0.1662</b>	<b>0.1662</b>	0.1491	<u>0.1546</u>	0.1389	<b>0.1356</b>
TS	0.4520	<u>0.4302</u>	0.4860	<b>0.4875</b>	<b>0.5107</b>	0.4975	<u>0.4905</u>	0.4995
F1	0.6226	<u>0.6016</u>	0.6541	<b>0.6555</b>	<b>0.6761</b>	0.6644	<u>0.6582</u>	0.6663
TSS	<b>0.6222</b>	0.6127	<u>0.5991</u>	0.6053	<b>0.5744</b>	0.5620	<u>0.4900</u>	0.5027
HSS	0.5082	<u>0.4858</u>	0.5345	<b>0.5373</b>	<b>0.5497</b>	0.5348	<u>0.5014</u>	0.5137

**Table S14.** Performance metrics for predicted  $\Delta B$  at Threshold = 400 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	0.4602	<u>0.4385</u>	0.5123	<b>0.5224</b>	0.5687	<u>0.5485</u>	0.6440	<b>0.6671</b>
POF	0.0575	<b>0.0523</b>	0.0616	<u>0.0658</u>	<b>0.0865</b>	0.0901	0.1393	<u>0.1429</u>
FAR	0.2587	<b>0.2500</b>	0.2516	<u>0.2602</u>	<b>0.2982</b>	0.3146	<u>0.3768</u>	0.3745
MR	0.1701	<u>0.1749</u>	0.1568	<b>0.1546</b>	0.1445	<u>0.1508</u>	0.1289	<b>0.1220</b>
TS	0.3965	<u>0.3826</u>	0.4370	<b>0.4413</b>	0.4580	<u>0.4382</u>	0.4635	<b>0.4767</b>
F1	0.5679	<u>0.5534</u>	0.6082	<b>0.6124</b>	0.6283	<u>0.6093</u>	0.6335	<b>0.6457</b>
TSS	<b>0.5712</b>	0.5751	<b>0.5916</b>	0.5851	<b>0.5573</b>	0.5346	<u>0.4943</u>	0.5035
HSS	0.4585	<u>0.4456</u>	0.5015	<b>0.5042</b>	<b>0.5135</b>	<u>0.4898</u>	0.4994	0.5132

**Table S15.** Performance metrics for predicted  $\Delta B$  at Threshold = 450 nT.

Metric	SETA	SETB	SETC	SETD	SETE	SETF	SETG	SETH
POD	<b>0.4211</b>	0.4243	0.4589	<b>0.4803</b>	0.5230	<u>0.4901</u>	0.5855	<b>0.6184</b>
POF	<u>0.0487</u>	<b>0.0482</b>	0.0536	<u>0.0601</u>	0.0715	<b>0.0690</b>	0.1127	<u>0.1246</u>
FAR	0.2768	<b>0.2732</b>	0.2791	<u>0.2930</u>	<b>0.3117</b>	0.3181	0.3894	<u>0.4003</u>
MR	<u>0.1552</u>	0.1544	0.1472	<b>0.1431</b>	0.1343	<u>0.1419</u>	0.1236	<b>0.1163</b>
TS	<u>0.3626</u>	0.3660	0.3897	<b>0.4005</b>	<u>0.4229</u>	0.3989	0.4263	<b>0.4377</b>
F1	<u>0.5322</u>	0.5358	0.5608	<b>0.5720</b>	<u>0.5944</u>	<u>0.5703</u>	0.5978	<b>0.6089</b>
TSS	0.5680	0.5724	<b>0.5737</b>	<u>0.5640</u>	<b>0.5541</b>	0.5400	0.4870	<u>0.4834</u>
HSS	<u>0.4360</u>	0.4401	0.4641	<b>0.4732</b>	<b>0.4928</b>	<u>0.4670</u>	0.4797	0.4885