Emulating present and future simulations of melt rates at the base of Antarctic ice shelves with neural networks

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Abstract

Melt rates at the base of Antarctic ice shelves are needed to drive projections of the Antarctic ice sheet mass loss. Current basal melt parameterisations struggle to link open ocean properties to ice-shelf basal melt rates for the range of current sub-shelf cavity geometries around Antarctica. We present a novel parameterisation based on deep learning. With a simple feedforward neural network, or multilayer perceptron, acting on each grid cell separately, we emulate the behavior of circum-Antarctic cavity-resolving ocean simulations. We explore different neural network sizes and find that, in all cases containing at least one hidden layer, this kind of emulator produces reasonable basal melt rates for our training ensemble, closer to the reference simulation than traditional parameterisations. For testing, we use an independent ensemble of simulations that was produced with the same ocean model but with different model parameters, different cavity geometries and different forcing. In this challenging test, traditional and neural network parameterisations yield similar results on present conditions. In much warmer conditions than the training ensemble, both traditional parameterisations and neural networks struggle, but the neural networks tend to produce basal melt rates closer to the reference than a majority of traditional parameterisations. These neural networks are therefore suitable for century-scale Antarctic ice-sheet projections.

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Key Points:

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11	•	We show that simple neural networks can produce reasonable basal melt rates by
12		emulating circum-Antarctic cavity-opening ocean simulations.
13	•	Predicted melt rates for present and warmer conditions are similar or closer to the
14		reference simulation than traditional parameterisations.
15	•	We show that neural networks are suited to be used as basal melt parameterisa-
16		tions for century-scale ice-sheet projections.

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17 Abstract

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35 Plain Language Summary

A warmer ocean around Antarctica leads to higher melting of the floating ice shelves, 36 which influence the ice loss from the Antarctic ice sheet and therefore sea-level rise. In 37 computer simulations of the ocean, these ice shelves are often not represented. For sim-38 ulations of the ice sheet, so-called parameterisations are used to link the oceanic prop-39 erties in front of the shelf and the melt at their base. We show that this link can be em-40 ulated with a simple neural network, which performs at least as well as traditional phys-41 ical parameterisations both for present and much warmer conditions. This study also 42 proposes several potential ways of further improving the use of deep learning to param-43 eterise basal melt. 44

45 **1** Introduction

The contribution of the Antarctic Ice Sheet to sea-level rise has been increasing in 46 past decades and this increase is projected to continue with increasing greenhouse gas 47 emissions (Fox-Kemper et al., 2021). Most of the mass loss is occurring at the margins 48 of the ice sheet through faster ice flow from the grounded ice sheet to the ocean, mainly 49 in West Antarctica (Mouginot et al., 2014; Rignot et al., 2014; Scheuchl et al., 2016; Khazen-50 dar et al., 2016; Shen et al., 2018; The IMBIE Team, 2018). This is because the float-51 ing ice shelves at the margins of the ice sheet, which usually buttress the ice flow, are 52 rapidly thinning and retreating due to ocean-induced melt at their base (Rignot et al., 53 2013; Paolo et al., 2015; Adusumilli et al., 2020). In some bedrock configurations, increased 54 ocean-induced melt can even trigger marine ice sheet instabilities (Weertman, 1974; Schoof, 55 2007; Gudmundsson et al., 2012), which have the potential to strongly increase Antarc-56 tic mass loss, on timescales below a century (Fox-Kemper et al., 2021). This makes ocean-57 induced sub-shelf melt, or basal melt, one of the main sources of uncertainty for future 58 projections of sea-level rise. 59

Basal melt is a result of warm ocean water coming into contact with the base of the ice shelf. Which water masses reach the ice-ocean interface depends on the circulation of the water, not only in front of the ice shelf, but also after entering the ice-shelf cavity (Dinniman et al., 2016). As a consequence, to simulate the properties of the water at the ice-ocean interface accurately, both the ocean circulation around Antarctica and the circulation in the cavities below the ice shelves need to be simulated accurately. A few global or circum-Antarctic ocean models already include ice-shelf modules (Losch,

2008; Timmermann et al., 2012; Dinniman et al., 2015; Mathiot et al., 2017; Comeau et 67 al., 2022), but such ocean models are expensive to run on long timescales or for large en-68 sembles. Instead, a majority of the global climate models used until now in the Coupled 69 (CMIP) or Paleoclimate (PMIP) Model Intercomparison Projects still poorly represent 70 the ocean dynamics along the Antarctic margins and do not include ice-shelf cavities (Beadling 71 et al., 2020; Heuzé, 2021). Getting the right water masses in the right place around Antarc-72 tica is a matter for global and regional ocean modelling and will not be the focus of this 73 study. In this study, we focus on the circulation within the ice-shelf cavities and the re-74 sulting melt. 75

To infer the basal melt forcing for projections of the Antarctic contribution to sea-76 level rise, ice-sheet models commonly rely on parameterisations linking hydrographic prop-77 erties in front of the ice shelves, given by observations or oceanic output from global cli-78 mate models, and the basal melt (Jourdain et al., 2020). Due to different assumptions 79 and simplifications concerning the circulation in the cavities, the range of existing basal 80 melt parameterisations leads to widely differing melt patterns and associated contribu-81 tions to sea-level rise (Favier et al., 2019; Burgard et al., 2022). The magnitude of the 82 resulting uncertainty contribution is similar, or even larger, than the choice of emission 83 scenario used to force the projections (Seroussi et al., 2020; Edwards & the ISMIP6 Team, 84 2021).85

Emulating the three-dimensional ocean circulation within the cavity in simplified 86 physical parameterisations is challenging and calls for exploring alternative approaches. 87 We suggest that deep learning can be one tool to tackle this challenge. In recent years, 88 the amount of ocean simulation output including ice-shelf cavities has increased and tools 89 that make the application of deep learning techniques easily accessible have been devel-90 oped, opening up the possibility of developing a neural network parameterisation for basal 91 melt. If trained with high-resolution model output, a neural network parameterisation 92 could implicitly include more intrinsic information about the system than a traditional 03 physical parameterisation. This approach has been applied promisingly in several areas of Earth System Sciences in the form of multilayer perceptrons applied on the grid-cell 95 level (e.g. Gentine et al., 2018; Rasp et al., 2018), convolutional neural networks applied 96 on multidimensional fields (e.g. Bolton & Zanna, 2019; Rosier et al., 2023) or random 97 forests (e.g. Yuval & O'Gorman, 2020). 98

Deep learning has also been explored for basal melt parameterisations. Rosier et 99 al. (2023) performed promising experiments that showed that a cavity-resolving ocean 100 model can be emulated with a convolutional neural network in a variety of idealised ice-101 shelf geometries. In the present study, we choose a different deep learning approach to 102 developing such a *deep emulator*, or *surrogate model*, which differs on two fundamental 103 points. On the one hand, we train on the circum-Antarctic cavity-resolving ocean sim-104 ulations with realistic geometries used in Burgard et al. (2022). On the other hand, we 105 use a multilayer perceptron architecture applied to each grid cell, as preliminarily ex-106 plored in Bouissou et al. (2022). In the following, we present a proof of concept for a mul-107 tilayer perceptron, which takes in hydrographic properties in front of the ice shelf and 108 the geometric information at each grid point. In Sec. 2, we present the training and test-109 ing data, the neural network architecture, and the evaluation procedure. In Sec. 3, we 110 show that the multilayer perceptron can successfully emulate cavity-resolving ocean sim-111 ulations and produce integrated basal melt and patterns at least as close as but gener-112 ally closer to the reference than traditional parameterisations in conditions similar to present. 113 In Sec. 4 we explore the applicability of such a neural network to an independent set of 114 simulations produced with a few different model parameters, slightly different geome-115 tries and in warmer oceanic conditions. Finally, in Sec. 5, we discuss the lessons learned 116 from our study and give an outlook on possible directions to explore further in the fu-117 ture. 118

¹¹⁹ 2 Data and Methods

The goal of this study is to explore if and how a neural network, in the form of a multilayer perceptron, can emulate the link between hydrographic properties in front of an ice shelf, geometric characteristics of the cavity, and the melt rates at its base as simulated by a cavity-resolving ocean model. In the following, we present the ocean model used and the set of simulations used for training, validation and testing the neural network; the neural network, its architecture, and its input variables; and the training and testing procedure.

2.1 Data

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We choose to emulate a cavity-resolving version of the 3-D primitive-equation coupled ocean-sea-ice model NEMO (Nucleus for European Modelling of the Ocean, NEMO Team, 2019) run on the eORCA025 horizontal grid (Storkey et al., 2018). This grid has a resolution of 0.25° in longitude on average, i.e. a resolution of 4 to 14 km in the Antarctic seas and below the ice shelves, which is sufficient to capture the basic ocean circulation below multiple Antarctic ice shelves (Mathiot et al., 2017; Bull et al., 2021).

For the training phase, we use the same ensemble of simulations as used for the as-134 sessment of traditional basal melt parameterisations in Burgard et al. (2022). The en-135 semble is composed of four ocean simulations spanning 30 to 40 years, depending on the 136 simulation, between 1979 and 2018. They were run with a standalone version of NEMO 137 and forced with atmospheric forcing from JRA55-do version 1.4 (Tsujino et al., 2018). 138 The Antarctic continental shelf bathymetry and ice shelf draft are constant and based 139 on Bedmachine Antarctica version 2 (Morlighem, 2020; Morlighem et al., 2020). The sim-140 ulations in the ensemble differ in a small number of parameters which are not directly 141 related to the physics driving the ocean circulation and melt within the ice-shelf cavi-142 ties but rather lead to a variety of hydrographic properties all around Antarctica. A more 143 detailed description of the exact model configuration and differences in parameters can 144 be found in Burgard et al. (2022). 145

For the testing phase, we use two simulations independent from the ensemble used 146 for training. In this case, NEMO was run in coupled mode as the oceanic component of 147 the Earth System Model UKESM1.0-ice (Smith et al., 2021), which couples the UK Earth 148 System Model (UKESM1, Sellar et al., 2019) to an adapted version of the ice-sheet model BISICLES (Cornford et al., 2013). In this coupled configuration, the cavities below the 150 ice shelves are open and the ice-shelf melt is computed with the same approach as in the 151 training ensemble (as proposed by Mathiot et al., 2017). This means that a z^* coordi-152 nate is used for depth and the three equations are used to parameterise the ice-shelf melt 153 in the ice-ocean boundary layer. Due to the coupled setup, the ice-shelf draft evolves ac-154 cording to the simulated evolution of the ice sheet. Note that the position of the ice front 155 at the surface remains fixed by ice-sheet model design. More details about the config-156 uration of NEMO in this model setup can be found in Smith et al. (2021). The two test 157 simulations differ in their atmospheric forcing. In the first one, which we will call "RE-158 PEAT1970", UKESM1.0-ice was run for several decades under constant 1970 greenhouse 159 gas and other forcings. In the second one, which we will call "4xCO2", UKESM1.0-ice 160 was run for several decades under instantaneously quadrupled 1970 CO_2 concentrations. 161 In our study, we use 60 years of simulation, from year 10 to year 70, for both runs. 162

The training and the testing dataset result from NEMO simulations. Nevertheless, next to differences in forcing from the atmosphere and the ice and bed geometry, the training and testing ensembles also differ in several technical aspects of NEMO. The training simulations were run with the version of 4.0.4. of NEMO (NEMO Team, 2019), including the sea-ice model SI³, while the test simulations were run with the version 3.6 of NEMO (Madec & NEMO Team, 2017) and version 5.1 of the Community Ice CodE (CICE, Hunke et al., 2015). In addition, a few different parameter choices may affect the

link between hydrographic properties in front of the ice shelf and the melt at the base 170 of the ice shelf. The training ensemble was computed on 121 vertical levels (represent-171 ing 20 m at 600 m depth), while the testing ensemble was computed on 75 vertical lev-172 els (representing 60 m at 600 m depth). In both ensembles, the thickness of the top bound-173 ary layer is bound at 20 m but can differ locally due to the different vertical resolutions. 174 In the training ensemble, the thermal Stanton number is set to 7×10^{-4} while in the test-175 ing ensemble the thermal Stanton number is set to 1.45×10^{-3} . In the training ensem-176 ble, the top tidal velocity varies locally based on the CATS2008 dataset (Padman et al., 177 2008; Howard et al., 2019), while it is fixed to 5 cm/s in the testing ensemble. In con-178 clusion, this means that the testing ensemble is a slightly different model than the model 179 which the neural network is trained to emulate and therefore represents a demanding test-180 ing experiment. 181

The training and testing ensembles cover a range of states that do not necessar-182 ily match observational estimates of hydrographic properties and basal melt rates. In 183 both standalone and coupled mode, eORCA025 configurations are prone to biases in the 184 ocean circulation around Antarctica (Smith et al., 2021). Nevertheless, in Burgard et al. 185 (2022), we showed that, if the forcing and parameters were carefully chosen to reproduce 186 realistic ocean conditions in the Southern Ocean, the resulting basal melt rates were in 187 agreement with observational estimates from Rignot et al. (2013). The physical link be-188 tween the hydrographic properties in front of the ice shelves and the basal melt rates is 189 therefore reasonable. Based on this assumption, biases in the input properties should not 190 affect the credibility of the training and evaluation procedure and the resulting neural 191 network. On the contrary, a large variety of states is even beneficial because it provides 192 more cases for our neural network to train on than only using the very limited sample 193 of observations. 194

On a more technical note, for this study, the NEMO output was interpolated bi-195 linearly to a stereographic grid of 5 km spacing, as ice-sheet models and basal melt pa-196 rameterisations are commonly run on a stereographic grid. All pre-processing, training, 197 testing, and analysis is conducted using this regridded data. From this regridded data, 198 we cut out the different ice shelves according to latitude and longitude limits defined on 199 the present geometry (details found in Burgard (2022)) and then apply a routine to adapt 200 this mask to slightly different geometries, like the ones resulting from the fully coupled 201 UKESM1.0-ice runs. Of these ice shelves, we only keep the largest ice shelves. The ef-202 fective resolution of physical ocean models, i.e. the resolution below which the circula-203 tion might not be resolved well, is typically 5 to 10 times the grid spacing (Bricaud et 204 al., 2020). We empirically choose a cutoff at an area of 2500 km² (i.e. 6.25 Δx) to be 205 in this range while keeping a sufficiently large number of ice shelves. Due to different ge-206 ometries in the training and testing ensemble, this results into a slightly different ensem-207 ble of resolved ice shelves in these two ensembles (as listed in the figures of Appendix 208 A). 209

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2.2 Neural network

We design our neural network to predict the basal melt rates based on information 211 about the ocean temperature and salinity in front of the ice shelf and about the ice-shelf 212 geometry (Fig. 1). To link the input to the prediction, we use a multilayer perceptron, 213 which is applied to each grid cell independently. A multilayer perceptron is the simplest 214 form of a neural network and is a composition of functions (also called hidden layers), 215 which takes an input array containing any number of variables and outputs a prediction. 216 Specifying its number of neurons, each hidden layer is characterised by its parameters 217 - the weights and biases, that connect each layer to its previous layer and shift the val-218 ues in the hidden layer, respectively. An activation function in the hidden layer intro-219 duces non-linearities in the relationship between input and output. In this study, we ex-220 plore different numbers of layers and numbers of neurons per layer. As activation func-221

- tion, we use the rectified linear unit (ReLU, Fukushima, 1975; Nair & Hinton, 2010). The
- multilayer perceptron is implemented in Python with the package Keras (Chollet et al.,
- 224 2015).

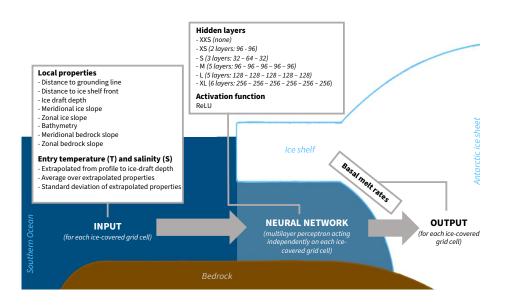


Figure 1. Schematic of the workflow around our neural network.

The strength of a neural network, and supervised machine learning techniques in 225 general, is that it can reproduce complex non-linear relationships without being given 226 the driving equations behind the data. Instead, its performance is driven by the super-227 vised training phase, which determines the weights and biases of each neuron in the net-228 work. During training, the loss, describing the averaged distance of the network predic-229 tions to a given target output, is backpropagated to the weights of the network. The weights 230 are then optimised with stochastic gradient descent. The training dataset is randomly 231 split up into batches, over which the optimisation is looped. A complete pass through 232 the batches defines an epoch, and the weights and biases are optimised over several such 233 epochs. In parallel to the training, the neural network is applied to a validation dataset 234 to monitor its performance on data that has not been used for the training. After train-235 ing, the final performance of the neural network is estimated by applying it to a previ-236 ously unseen testing dataset. 237

In this study, to train the neural network, the loss which we reduce is the meansquared-error over all ice-covered points between the predicted (m_{NN}) and target (m_{ref}) basal melt rates,

$$MSE = \frac{\sum_{i}^{N_{\text{pts}}} \sum_{t}^{N_{\text{years}}} (m_{\text{NN}}[i,t] - m_{\text{ref}}[i,t])^2}{N_{\text{pts}} N_{\text{years}}}$$
(1)

where N_{pts} is the number of ice-covered grid points and N_{years} is the number of years 241 used in the training. In Burgard et al. (2022), we argued that tuning on the grid-cell level 242 would give too much weight to the larger ice shelves, as they cover a larger area. We still 243 agree with this statement for traditional parameterisations because they already intrin-244 sically contain assumptions about the physics of the circulation and the melt before tun-245 ing and have only one or two tuneable parameters. In the case of our neural network, 246 the relationship between the properties in front of the ice shelf and the melt is learnt from 247 scratch, and it contains a larger number of parameters to adjust. We therefore argue that 248 training on the grid-cell level is more sensible. 249

The neural network is optimised with Adam (Kingma & Ba, 2014), an initial learning rate of 0.001, $\beta_1=0.9$ and $\beta_2=0.999$. We split the training dataset in batches with a size of 512 samples and optimise the neural network for at most 100 epochs. If the validation loss is not improved for 5 epochs, we reduce the learning rate by a factor of 2. If the validation loss is not improved for 10 epochs, we stop the training early. After early stopping, the model weights with the lowest validation loss are restored.

2.3 Input variables

The multilayer perceptron takes an array of variables as input for each grid cell independently. In our case, the input array contains information about the geometrical properties of the grid cell and the hydrographic forcing (Fig. 1).

For the geometrical properties, the input contains the following information: the ice draft depth, the local meridional and zonal slopes of the ice draft, the bathymetry, the local meridional and zonal slopes of the bedrock, and the distance of the grid cell to the nearest grounding line cell and the distance to the nearest ice front cell. All these variables are defined on the same horizontal plane and domain as the output array, the basal melt rates.

For the hydrographic forcing, more pre-processing is needed. To map the hydro-266 graphic forcing to the same grid cells as the other input variables, we proceed in the same 267 manner as for traditional simple parameterisations in Burgard et al. (2022). First, we 268 convert the conservative temperature and absolute salinity given by NEMO into poten-269 tial temperature and practical salinity with the GSW oceanographic toolbox (Firing et 270 al., 2021). Second, we average the potential temperature and practical salinity, respec-271 tively, over the continental shelf within 50 km of the front of each ice shelf. The conti-272 nental shelf is defined as grid cells where the depth of the bathymetry is shallower than 273 1500 m. The 50 km criterion imitates CMIP-type global ocean models that have reso-274 lutions around 1° (Heuzé, 2021), corresponding to a distance of between 38 km $(70^{\circ}S)$ 275 and 56 km (60° S) in longitude. Third, we extrapolate the temperature and salinity from 276 these mean profiles in front of the ice shelf to the local ice-draft depth, resulting in one 277 local temperature and local salinity value per grid cell in the ice-shelf domain. Fourth, 278 we also compute, for each time step, the average and standard deviation of these extrap-279 olated temperature and salinity fields and use them as additional input variables for each 280 grid cell. 281

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2.4 Training, validation and testing methodology

In a first step, we explore different neural network sizes using the method of cross validation on our training ensemble. In a second step, we choose a subsample of the neural networks to explore their performance on the testing dataset.

We conduct two variations of leave-one-block-out cross validation to estimate the 286 validation loss (MSE as defined in Eq. 1), one on the ice shelf dimension and one on the 287 time dimension, like in Burgard et al. (2022). This approach consists of dividing the dataset 288 into N blocks, training the neural network to minimise the training loss on N-1 blocks 289 and using the left-out block to compute the validation loss (Wilks, 2006; Roberts et al., 290 2017). The procedure is re-iterated N times, leaving out each of the N blocks succes-291 sively, so that, in the end, each N-th block has been left out of training once. All pre-292 dictions for the left-out blocks, using the separately trained neural networks, are then 293 concatenated to form a "synthetically independent" evaluation dataset. Applying an eval-294 uation metric on this evaluation dataset, we assess how well the neural network gener-295 alises to data "unseen" during training. We use N=35 for the cross validation over ice 296 shelves. For the cross validation over time, we divide the years into blocks of approxi-297 mately 10 years (ten 10-year blocks and three 9-year blocks) to reduce the effect of au-298

Neural network configuration	Number of hidden layers	Number of neurons
XXS	0	0
XS	2	96/96
S	3	32/64/32
\mathbf{M}	5	96/96/96/96/96
L	5	128/128/128/128/128
XL	6	256/256/256/256/256/256

 Table 1.
 Neural network size of the different variations explored in the cross validation.

to correlation, which is typically 2 to 3 years in our input temperatures. This results in N=13 for the cross validation over time.

Before training, we normalise the training sample to put each of the 14 input variables (listed in Fig. 1) as well as the output variable on a similar order of magnitude and avoid potential problems of gradient explosion. We do so by subtracting the mean and dividing by the standard deviation of the training sample. To avoid that validation data leaks into the training, this normalisation is reiterated for each iteration of the cross validation.

We use the framework of cross validation to evaluate not only one but several neural networks to estimate the effect of their size on their performance. We sample different sizes ranging from an extra-extra small (XXS) neural network, with no hidden layer, and thus corresponding to a linear regression, to an extra-large (XL) neural network, with six hidden layers, each containing 256 neurons. The different sizes are listed in Table 1.

To evaluate the resulting basal melt rates, we use the same metrics as in Burgard et al. (2022), namely: (1) the root-mean-squared error (RMSE) of the yearly integrated melt on the ice-shelf level and (2) the RMSE of the mean melt near the grounding line for each ice shelf. For the former, we compute the RMSE between the simulated and emulated yearly integrated melt (M) of the individual ice shelves [in Gt/yr] as follows:

$$RMSE_{\rm int} = \sqrt{\frac{\sum_{k=1}^{N_{\rm isf}} \sum_{t=1}^{N_{\rm years}} (M_{\rm NN}[k,t] - M_{\rm ref}[k,t])^2}{N_{\rm isf}N_{\rm years}}}$$
(2)

where the subscript NN stands for neural network, N_{isf} is the number of ice shelves and N_{years} the number of simulated years, and the integrated melt M of ice shelf k [in Gt/yr] is:

$$M[k] = \rho_i \times 10^{-12} \sum_{j}^{N_{\text{grid cells in k}}} m_j a_j \tag{3}$$

where ρ_i is the ice density, m_j is the melt [in m ice per year] in grid cell j, and a_j is the area of grid cell j. For the latter, we compute the RMSE between the simulated and emulated yearly mean melt rate near the grounding line [in m ice per year]:

$$RMSE_{\rm GL} = \sqrt{\frac{\sum_{k}^{N_{\rm isf}} \sum_{n}^{N_{\rm simu}} (m_{\rm GL,NN}[k,n] - m_{\rm GL,ref}[k,n])^2}{N_{\rm isf}N_{\rm simu}}}$$
(4)

where N_{simu} is the number of simulations in the ensemble and where m_{GL} for ice shelf k and simulation n is:

$$m_{\rm GL}[k,n] = \frac{1}{N_{\rm years \ in \ n}} \sum_{t}^{N_{\rm years \ GL \ near \ GL \ in \ k}} \frac{\sum_{j}^{N_{\rm grid \ cells \ near \ GL \ in \ k}} (m_j a_j)}{\sum_{j}^{N_{\rm grid \ cells \ near \ GL \ in \ k}} a_j}$$
(5)

The domain "near the grounding line" is the area covered by the first box prepared for the box parameterisation, when considering a maximum amount of five boxes, and is equivalent to approximately 10 % of the shelf area.

After cross validation, we choose a subsample of these neural networks to do fur-328 ther evaluation on a completely independent dataset. To do so, we reiterate the train-329 ing of the subsample of neural networks over the whole training dataset and choose to 330 work with a deep ensemble (Lakshminarayanan et al., 2017). The final weights and bi-331 ases of neural networks depend on the initialisation of the weights before the first train-332 ing iteration (Goodfellow et al., 2016). To account for this uncertainty and gain a more 333 robust performance from the neural networks, we reiterate the training of the subsam-334 ple of neural networks ten times with ten different random initialisations. We then ap-335 ply this deep ensemble of ten neural networks to the independent testing input and com-336 pute an ensemble mean over the ten resulting melt rates. Note that we only investigate 337 a small sample of neural network sizes for exploration in this study and do not claim that 338 the best performing neural network here is the best performing neural network for the 339 problem. This study is rather a proof of concept to encourage further research in this 340 direction. 341

³⁴² **3** Training and cross validation

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3.1 Integrated melt and mean melt near the grounding line

The two evaluation metrics for the cross validation of the different neural network 344 sizes are shown in Fig. 2. In addition, to compare the performance to traditional param-345 eterisations, we show the evaluation metrics for a subset of existing parameterisations: 346 the quadratic local parameterisation using a constant Antarctic slope (e.g. Holland et 347 al., 2008) and using a local slope (e.g. Favier et al., 2019; Jourdain et al., 2020), the plume 348 parameterisation proposed by Lazeroms et al. (2019), the box parameterisation with the 349 same box amount as in Reese et al. (2018), and the PICOP parameterisation from Pelle 350 et al. (2019). The parameterisations are used as presented and tuned in Burgard et al. 351 (2022).352

Corresponding to a linear regression, the XXS neural network leads to a RMSE of a similar order as traditional parameterisations in the cross validation over time and, for the melt near the grounding line, in the cross validation over ice shelves as well. For the integrated melt, the cross validation over ice shelves leads to a comparably high RMSE. In the further course of this study, we therefore focus on neural networks that include hidden layers.

For both metrics, the RMSE for the cross validation over time is considerably reduced when using a neural network with hidden layers compared to traditional parameterisations and the XXS neural network. The RMSE for the cross validation over ice shelves is higher than for the cross validation over time but remains on the lower end of the range of RMSEs given by traditional parameterisations.

The RMSE_{int} of the cross validation over time is very similar between neural network sizes and spans between 6 Gt/yr (XL) and 11 Gt/yr (S). It remains well below the mean reference integrated melt on the ice-shelf level of 39 Gt/yr. The RMSE_{int} of the

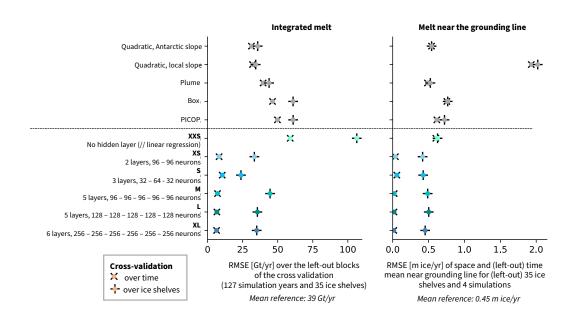


Figure 2. Summary of the RMSE of the integrated melt $(RMSE_{int})$ for the cross validation over time (×) and for the cross validation over ice shelves (+) for a selection of traditional parameterisations (as shown in Burgard et al., 2022) [in Gt/yr] (left) and summary of the RMSE of the melt rate averaged over time and space near the grounding line $(RMSE_{GL})$ [in m ice/yr] (right). The colors represent the different parameterisation approaches: traditional parameterisations (grey), neural network (shades of blue). The RMSE is computed following Eq. (2), left panel, and Eq. (4), right panel, on the synthetically independent evaluation dataset.

cross validation over ice shelves varies more and is higher, between 24 (S) and 45 Gt/yr
 (M). The performance does not correlate with the neural network size. On the contrary,
 the lowest RMSE_{int} of the cross validation over ice shelves is found for a comparably small
 neural network (S).

For the melt near the grounding line, the RMSE_{GL} does not vary much in both cross validations between neural network sizes. The cross validation over time leads to a very low RMSE, varying from 0.02 m/yr (M,L,XL) to 0.06 m/yr (S). The cross validation over ice shelves leads to a RMSE between 0.42 m/yr (XS,S) and 0.50 m/yr (L), on the same order as the mean reference melt near the grounding line on the ice-shelf level, which is 0.45 m ice/yr.

The neural networks have more difficulties generalising to unseen ice shelves than 377 generalising to unseen time periods. This means that one of the obstacles for the neu-378 ral networks' performance is the application to unknown cavity geometries. Some of the 379 cavity geometries are so different from the rest of the ensemble that they force the neu-380 ral networks to extrapolate far from their training domain. However, if they have seen 381 a given geometry at least once during training, they perform well on this geometry for 382 another time step. This aspect is encouraging, as this means that the neural networks 383 adapt well to temperature and salinity variations across the training ensemble. 384

3.2 Spatial patterns

385

To add on the metrics at the ice-shelf level, we analyse the spatial patterns resulting from the XS, S and L neural networks (Fig. 3) for the training ensemble member clos-

est to realistic conditions (called REALISTIC in Burgard et al., 2022). For the cross val-388 idation over time, the patterns of XS, S and L are nearly indistinguishable from the ref-389 erence for Filchner-Ronne, Pine Island, Fimbul, and Totten ice shelves. For Ross ice shelf, 390 all patterns are close to the reference, but the S pattern contains more widespread melt-391 ing.

392

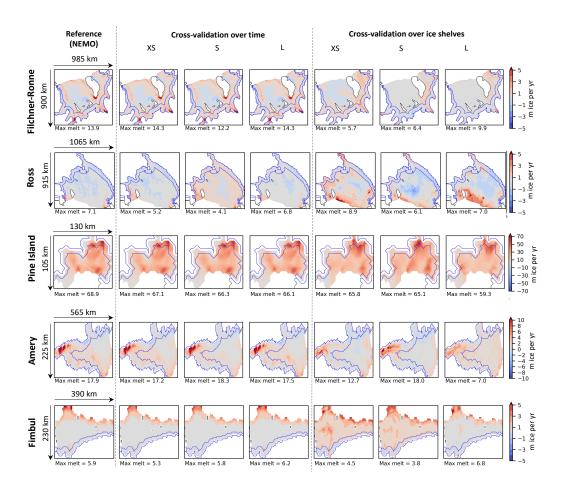


Figure 3. Subset of ice shelves for a visual evaluation of the melt patterns. This is the time average for the training ensemble member closest to real conditions (39 years) where the melt for each timestep has been computed with the neural network trained on the dataset leaving out that timestep (cross validation over time, columns 2 to 4) and where the melt of each ice-shelf has been computed with the neural network trained on the dataset leaving out that ice shelf (cross validation over ice shelves, columns 5 to 7). The blue line indicates the region used to evaluate the melt rate near the grounding line (which is defined as the first box in the 5-box setup of the box parameterisation).

For the cross validation over ice shelves, the patterns are not matching in as much 393 detail as in the cross validation over time. In particular for the two largest ice shelves, 394 Filchner-Ronne and Ross, it becomes clear that if the neural network has been trained 395 without one of them, it will mimic the spatial pattern of the other because they are the 396 only ones to share given ranges in the input variables, such as for example large distances 397 to the ice front and grounding line. For Filchner-Ronne and Ross, the result of the cross 398 validation over ice shelves does not match the reference in any of the neural networks. 399

For Pine Island and Amery, the XS and S patterns match the reference better than the L pattern, while, for Fimbul and Totten, the L pattern is a little better.

The low RMSE in the cross validation over time suggests an overfit on the geom-402 etry, which is fixed over time in the training dataset. The patterns very close to the ref-403 erence in the cross validation over time show that, even if our neural networks are ap-404 plied on each grid-cell separately, the location of the grid cell is more or less encoded in 405 one or more input variables. However, as our problem is not necessarily well constrained 406 with the input variables given, we suggest that this overfit can be used to our advantage. 407 Our hypothesis is that, if the neural network has seen each ice shelf once, it has captured the variety of geometries and will be able to generalise to future changes in these "known" 409 ice shelves. We do not expect new and completely different ice shelves to appear in the 410 next centuries. To assess this idea, we need to investigate how well the neural network 411 will perform on a geometry which is similar to but not identical to the training. 412

In the following, we investigate further if the neural networks are suitable for evolving ice-shelf geometries that are close to existing geometries and to temperature and salinity input properties outside the training range. We choose to continue with (1) the S size, because it has the lowest RMSE in the cross validation over ice shelves, (2) the XS size because it has similarly low RMSE to the larger sizes but remains very small and simple, and (3) the L size to include a larger neural network and explore potential differences during the testing compared to its behavior in the cross validation.

420 4 Testing on independent simulations

We apply our subsample of neural network sizes on two independent datasets, one 421 representing 60 years of constant 1970-forcing (REPEAT1970), and one representing warmer 422 conditions, i.e. 60 years of abrupt $4xCO_2$ forcing $(4xCO_2)$, from Smith et al. (2021). The 423 REPEAT1970 simulation has a relatively steady ice-sheet geometry, similar (but not iden-424 tical) to the training geometry and is useful to assess the sensitivity of the neural net-425 works to different near-present-day atmospheric conditions (from the UKESM atmosphere 426 component), to different parameters used in NEMO, and to slightly different geometries. 427 The 4xCO₂ simulation experiences larger changes in ice-sheet geometry and much warmer 428 conditions, which is useful to test the neural networks far outside of their training range. 429 As a consequence, this evaluation is demanding and permits to evaluate the limits of the 430 neural networks. 431

For evaluation, we divide the 4xCO₂ run into two 30-year blocks to capture potential differences with warming in time. As explained in Sec. 2.4, we train the XS, S and L neural networks ten times each, with ten different random initialisations. In the following, the results shown are averages over the predictions of the ten ensemble members for each neural network size.

437

4.1 Integrated melt and melt near the grounding line

The neural networks reproduce well the REPEAT1970 melt rates integrated over individual ice shelves, with a RMSE_{int} of 16 to 19 Gt/yr (Fig. 4a, left). This error is slightly larger than in the cross validation over time (see Fig. 2), and becomes similar to the quadratic and plume parameterisations. It should be noted that the RMSE_{int} of these parameterisations is lower than in the cross validation, likely because of the overall lower melt rates in this simulation (24 Gt/yr compared to 39 Gt/yr in the training ensemble). The neural networks still clearly outperform the box and PICOP parameterisation (RMSE_{int} \simeq 35 Gt/yr).

For the melt near the grounding line, all parameterisations are uncertain, with $RMSE_{GL}$ close to the reference mean melt near the grounding line of 0.34 m/yr (Fig. 4a, right). The neural networks and the traditional parameterisations yield similar $RMSE_{GL}$, be-

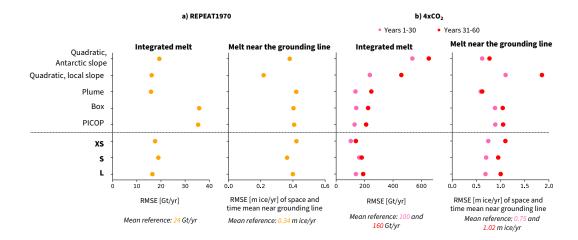


Figure 4. Summary of the RMSE of the integrated melt $(RMSE_{int})$ [in Gt/yr] and of the RMSE of the melt rate averaged over time and space near the grounding line $(RMSE_{GL})$ [in m ice/yr] for a selection of traditional parameterisations and a subsample of neural networks for the application on REPEAT1970 (a) and $4xCO_2$ (b). Note the change in x-axis between the (a) and (b) panels.

tween 0.36 and 0.42 m/yr, except the quadratic using a local slope, which leads to a slightly lower RMSE, on the order of 0.22 m/yr.

For the warmer conditions $(4xCO_2)$, all parameterisations struggle to reproduce 450 the integrated melt on the ice-shelf level, with high spread in performance between the 451 parameterisations (Fig. 4b, left). The RMSE_{int} is multiplied by more than 10 for the neu-452 ral networks and reaches nearly 650 Gt/yr for the quadratic parameterisation using an 453 Antarctic slope in the second period. While this jump in RMSE can be explained by a 454 higher mean reference integrated melt (100 Gt/yr for the first period and 159 Gt/yr for 455 the second period, see also Fig. A3), it is probably also a result of forcing unseen dur-456 ing training such as much warmer and less saline ocean conditions (Figs. A1 and A2). 457 Over both periods, the neural networks remain at the lower range of the difference to 458 the reference melt rates. While neural networks, plume, box and PICOP parameterisa-459 tion have comparable RMSEs for the first warm period (between 103 and 163 Gt/yr), 460 the RMSE increases more for the plume, box and PICOP parameterisation (between 211 461 and 248 Gt/yr) than for the neural networks (between 138 and 191 Gt/yr) in the even 462 warmer second period. 463

For the melt near the grounding line, the parameterisations perform differently than 464 for the integrated melt, pointing to potential challenges outside the domain near the ground-465 ing line. The neural networks perform in a similar uncertain manner as in the REPEAT1970 466 case (Fig. 4b, right). Their RMSE_{GL} (0.69-0.75 m/yr in the first period and 0.95-1.10 m/yr 467 in the second period) is close to the reference mean melt near the grounding line (0.75 m/yr)468 for the first period and 1.02 m/yr for the second period). In the first period, only the 469 quadratic local parameterisation using an Antarctic slope and the plume parameterisa-470 tion have lower $RMSE_{GL}$ (0.62 and 0.59 m/yr respectively), while in the second period 471 only the quadratic parameterisation using a local slope performs clearly worse than the 472 other parameterisations. For all, the RMSE increases with warmer conditions but the 473 gap between the periods depends on the parameterisation, ranging from a difference of 474 0.04 m/yr for the plume parameterisation to a difference of 0.76 m/yr for the quadratic 475 parameterisation using a local slope. 476

From this demanding application on an independent testing dataset, several con-477 clusions can be drawn. First, the neural networks apply reasonably well to data inde-478 pendent from training in present conditions. This means that, if they have seen all ge-479 ometries of the main circum-Antarctic ice shelves, they can adapt to slightly different geometries. This is even more encouraging as the testing simulations were conducted with 481 a slightly different version of NEMO than the neural networks were trained on. Second, 482 none of the neural networks seems to constantly be the one with the best performance 483 for all metrics. Third, the RMSE of the neural networks is higher when applied to warmer 484 conditions, but, in comparison with the traditional parameterisations, it performs at least 485 as well or even better. 486

487 4.2

4.2 Spatial patterns

Looking at the spatial patterns averaged over the last 10 years of the $4xCO_2$ run, 488 it becomes clear that all parameterisations, both neural networks and traditional ones, 489 struggle with warmer conditions and different geometries to the training ensemble (Fig. 5). 490 The maximum melt rates remain far below the maximum melt rates of the reference for 491 all of them except the quadratic parameterisation using the local slope, which largely 492 overestimates the maximum melt rates (as seen already in Burgard et al., 2022). Look-493 ing at the general patterns, the neural networks tend to overestimate the melt on wide areas of Filchner-Ronne and Ross but underestimate it over the whole ice shelf for smaller 495 ones. The quadratic parameterisations (both using Antarctic and local slope) and, in some 496 cases, the plume parameterisation, tend to overestimate the melt over wide areas, in par-497 ticular for the Ross and Filchner-Ronne ice shelves. The box parameterisation under-498 estimates the melt for all ice shelves, completely missing regions of strong melt. 499

500 5 Discussion

In this study, we showed that a simple multilayer perceptron can emulate melt rates 501 as simulated by the cavity-resolving ocean model NEMO. This result is encouraging for 502 further development because, as it is applied on a grid-cell level, it allows larger amounts 503 of training data to be used than architectures containing convolutions such as MELT-504 NET (Rosier et al., 2023) or, more generally, U-Nets (Ronneberger et al., 2015), which 505 take spatial domains as inputs. In addition, this architecture is independent of the do-506 main size and is therefore directly applicable to any ice shelf around Antarctica. In the 507 following, we discuss insights from this study and possible further improvements to this 508 approach. 509

510

5.1 Variable importance

One argument that is often made against the use of neural networks is that they 511 remain statistical emulators of the training data and do not contain any physical con-512 straints. The performance when applied to a slightly different model and to different con-513 ditions (see Sec. 4) already gives us a sense that the neural networks can reasonably adapt 514 to conditions outside of training. In addition, we now perform a sanity check to verify 515 that the neural network is doing "the right thing for the right reasons". This sanity check 516 also gives insight into the importance of the different input variables and could help fu-517 ture development of deep learning parameterisations as well as physical parameterisa-518 tions to focus on these variables. 519

To assess the importance of the different variables on the performance of the neural networks, we apply two variations of the permute-and-predict approach. In the permuteand-predict approach, one of the variables is shuffled randomly and used as input for the neural network alongside the other variables that remain in the original order. In the first variation (Fig. 6a), we shuffle the input variables within the REPEAT1970 sample to eval-

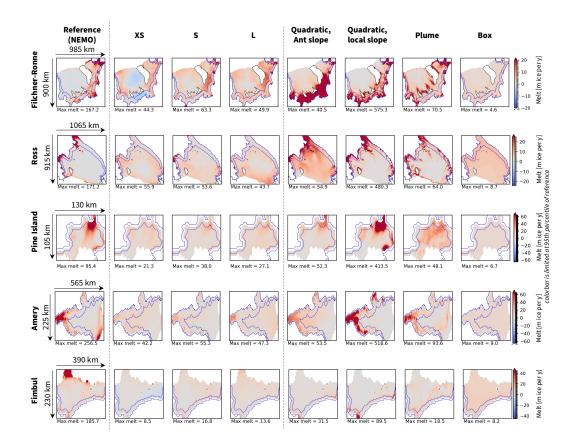


Figure 5. Subset of ice shelves for a visual evaluation of the melt patterns. This is the time average for the last 10 years of the $4xCO_2$ run. The colorbar is limited to the 95th percentile of the NEMO reference. The blue line indicates the region used to evaluate the melt rate near the grounding line (which is defined as the first box in the 5-box setup of the box parameterisation).

⁵²⁵ uate the importance of the different variables in a situation close to the training condi-⁵²⁶tions. In the second variation (Fig. 6b), we use a random sample from the 4xCO₂ input ⁵²⁷for the shuffled variable and run the neural network using all other original input vari-⁵²⁸ables from the REPEAT1970 run to evaluate the importance of different variables in much ⁵²⁹warmer conditions. The shuffling is reiterated for each variable separately. In addition, ⁵³⁰we also shuffle blocks of potentially correlated variables simultaneously to gain insight ⁵³¹on the effect of correlation on the shuffling results.

For the shuffling within the REPEAT1970, the geometric properties dominate the 532 performance of all three neural networks for the integrated melt (Fig. 6a, left). For the 533 XS version, the ice-shelf size, for which the distance to the ice front could be seen as a 534 proxy, and the water column height, through ice-draft depth and bathymetry, have the 535 highest importance. For the S and L version, the bathymetry is less important but the 536 distance to the ice front and the ice-draft depth remain the most important variables, 537 with an effect on the RMSE decreasing from S to L. The shuffling of the temperature 538 and salinity variables have a smaller effect when shuffled separately, which can be ex-539 plained by the correlation between these variables. However, when shuffled by group, the 540 temperature information gains in importance, leading to a similar increase in RMSE as 541 the distance to the ice front in the L version. The bedrock and ice slopes are not impor-542 tant for the performance on the integrated melt. For the melt near the grounding line 543 (Fig. 6a, right), many variables are not important, the RMSE is reduced when they are 544

		Integrated mel [Gt/yr]	lt	Melt	near groundin [m ice/yr]	gline
	XS	S	L	XS	S	L
Original RMSE	17.6	18.9	16.5	0.42	0.36	0.40
(REPEAT 1970)						
		(a) Difference in F	RMSE to original	after shuffling v	within REPEAT19	70
Distance GL	2.5	2.2	-0.4	-0.05	-0.04	-0.06
Distance IF	15.4	15.5		0.03	0.06	0.05
Ice draft depth	20.4	18.8	10.5	0.02	-0.04	-0.02
Bathymetry	16.3	2.3	3.8	0.04	0.01	0.01
Slope bed lon	0.3	0.6	-0.2	-0.01	-0	-0.01
Slope bed lat	0.3	-0.2	0.1	0	0.01	0.01
Slope ice lon	0.4	1	0.5	0.02	0.05	0.03
Slope ice lat	0.1	0	-0	0.01	0.02	0.01
Temperature	4.7	5.2	5.2	0.09		
Salinity	9.4	8.2	1.3	-0.03	-0.01	0
Temperature mean	3.3	5.3	4.4	0.06		0.09
Salinity mean	4.9	3.2	3.6	0.01	0.02	0.03
Temperature std	0.7	0.9	0.5	0	-0.02	0.05
Salinity std	2.2	0.4	1.4	0.02	0.05	0.04
Position	14.2	19	13	-0.02	0.01	-0.01
Water column	14.7	18.9	6.9	-0.03	-0.01	-0.01
Slopes bed	0.6	0.2	0.1	-0.01	0	-0
Slopes ice	1.1	1.1	1	0.05	0.07	0.05
Temperature info	10.2			0.14	0.18	0.17
Salinity info	3.3	5.1	2.6	0.05	0.06	0.08

(b) Difference in RMSE to original after inserting random sample from 4xCO₂ into REPEAT1970

Distance GL	2.5	2.1	-0.4	-0.05	-0.03	-0.07
Distance IF	14.9	15	11.3	0.05	0.06	0.06
Ice draft depth	25.4	15.5	12.7	0.02	-0.04	-0.01
Bathymetry	16.7	2.4	4	0.04	0.01	0.01
Slope bed lon	0.3	0.5	-0.2	-0.01	0	-0.01
Slope bed lat	0.3	-0.1	0.1	0	0.01	0.01
Slope ice lon	0.4	1	0.5	0.02	0.04	0.03
Slope ice lat	0.2	0.2	-0.1	0.01	0.02	0.01
Temperature	179.7	151.7	85	-0.06	-0.01	-0.04
Salinity	51.1	115.2	10.1	0.08	0.04	0.05
Temperature mean	92.5	127.1	91.1	0.1	-0.06	-0.09
Salinity mean	120.9	377.4	55.3	-0.01	0.01	-0.01
Temperature std	12.9	1.9	13.2	-0	0.01	0.02
Salinity std	29.6	11.9	7.9	0.02	0.02	0.01
Position	13.9	18.6	13	-0.01	0.02	0
Water column	15.9	16.3	7.1	-0.03	-0	-0.01
Slopes bed	0.5	0.2	0.1	-0	0	0
Slopes ice	1.1	1.2	0.9	0.04	0.07	0.05
Temperature info	330.6	307.1	266.5	0.21		-0.03
Salinity info	20.7	95.8	3.2	0.07	0	0.06

Figure 6. Difference in RMSE between an application using a random sample for the given variable of the REPEAT1970 input (a) and of the $4xCO_2$ input (b) and the original application on the REPEAT1970 input using the XS, S and L deep ensemble. The original RMSE when applied to REPEAT1970 is indicated above each column. The upper part of the tables shows the results when shuffling the variables individually while the lower part is for variables that have been shuffled as a group. "Temperature" and "Salinity" are the ocean properties extrapolated to the ice-draft depth, "Temperature mean" and "Salinity mean" are their average over each cavity, and "Temperature std" and "Salinity std" their standard deviation over each cavity. In the block *Position* we group the distance to the grounding line and to the ice front, in the block *Water column* we group the ice-draft depth and the bathymetry, in the block *Slopes bed* and *Slopes ice* we group the meridional and zonal slope of the bedrock and ice respectively, in the block *Temperature info* and *Salinity info* we group the local value, the average and the standard deviation of temperature and salinity respectively.

shuffled. The strongest effect is seen when shuffling the temperature variables as a group.
The salinity variables, the ice slopes, and the distance to the ice front are the second most important group.

When inserting random samples of $4xCO_2$ input, the importance of the ice front, 548 the ice-draft depth and the bathymetry remains of a similar order of magnitude for the 549 integrated melt as in the REPEAT1970 shuffling (Fig. 6b, left). However, the effect of 550 the temperature increases drastically and leads to increases in the RMSE of more than 551 300 Gt/yr. For the XS and S, the importance of the grouped salinity information increases 552 553 as well. This result reflects the difficulty for neural networks to extrapolate outside of the training range. Looking at the distribution of the input variables, the geometrical 554 conditions in the $4xCO_2$ run are in a similar range as the training ensemble, despite an 555 involving ice-shelf geometry, while the temperature and salinity variables are clearly out-556 side of the distribution (Fig. A4). For the melt near the grounding line (Fig. 6b, right), 557 introducing variables from warmer conditions does not affect the RMSE very differently 558 than in the REPEAT1970 case. 559

Several conclusions can be drawn from this experiment. First, this experiment shows 560 that the geometry, in particular the distance to the ice front and the ice-draft depth, are 561 key variables for the neural networks to infer reasonable integrated melt when applied 562 on variables close to the training range, closely followed by the temperature. Ice-draft 563 depth and temperature already are an integral part of existing parameterisations (Burgard 564 et al., 2022). However, the distance to the ice-shelf front or the ice-shelf size are currently 565 only partly considered, and only in the more complex parameterisations such as the plume 566 and box parameterisations (Lazeroms et al., 2019; Reese et al., 2018). 567

Second, when applied to much warmer conditions, the distribution of geometric vari-568 ables remains close to their distribution in the training ensemble. In contrast, the tem-569 perature and salinity, well outside the training range, clearly affect the resulting inte-570 grated melt. This suggests that training the neural networks on simulations of warmer 571 conditions could already improve their performance. Even more promising, the low ef-572 fect of geometry changes on integrated melt in warmer conditions suggests that coupled 573 ice-ocean simulations of warmer conditions are not necessarily needed for training and 574 that cavity-opening ocean simulations with fixed geometry could already be sufficient. 575

Third, for the melt near the grounding line, the position of the grid cell is (maybe 576 surprisingly) less important than for the integrated melt and the key variable is the tem-577 perature information, both near the training range and in warmer conditions. While the 578 ice slope does not affect the integrated melt, it has some effect on the melt near the ground-579 ing line. This suggests that including ice slopes is necessary for a good performance near 580 the grounding line. However, the way it is currently included in simple parameterisations 581 is not successful as we showed in Burgard et al. (2022) that it leads to a clear overesti-582 mation of the melt in this region. 583

Fourth, the effect of the shuffling on the RMSE is generally lower for the L size of the neural networks. This could suggest an overfit as it could mean that the neural network is not following variations in the input variables as much as the other neural network sizes and is therefore less flexible. This possible overfit would also explain why we did not see an increase in the performance during the cross-validation with increasing network size in Sec. 3.

590 5.2 Possible improvements

While the results of our neural networks are encouraging, a variety of further improvements can be conducted in the future. The most obvious conclusion from this study is that predicting warmer conditions, similar to climate change conditions, is challenging for this particular neural network architecture because these conditions were not contained during training and neural networks are known to struggle with extrapolation problems. We therefore suggest, when possible, to introduce a set of simulations containing
high-end future scenarios in the training dataset to make the neural network more robust for future projections. At the same time, we saw that the traditional parameterisations struggle to represent future conditions as well. How to tune melt parameterisations to be applicable in both present and future conditions is therefore a problem that
is not limited to deep learning approaches.

Another possible improvement is the treatment of the largest ice shelves. When 602 looking at the cross-validation results into more detail, i.e. at the scale of each ice shelf 603 (not shown), the total RMSE over all ice shelves is strongly influenced by the high RMSE 604 for the Ross ice shelf and, to a smaller extent, by the relatively high RMSE for the Filchner-605 Ronne ice shelves. These two ice shelves have an area which is much larger than the other 606 ice shelves around Antarctica. Their cavities are so large that they develop their own 607 internal circulation (e.g. Gerdes et al., 1999; Naughten et al., 2021) and the residence 608 time of water masses reaches several years (Michel et al., 1979; Nicholls & Østerhus, 2004). 609 It is therefore not too surprising that parameterisations, which use input temperature 610 and salinity averaged over thousands of kilometers at the front of the ice shelves and do 611 not represent horizontal circulation explicitly, struggle with the representation of melt 612 in these cavities. If we remove these two from the RMSE in the $4xCO_2$ case for exam-613 ple, we find that the RMSE is clearly reduced for both neural networks and traditional 614 parameterisations (Fig. 7 compared to Fig. 4b). It would therefore be worth consider-615 ing whether these rather simple parameterisations are appropriate for the application 616 on the Ross and Filchner-Ronne ice shelves and if it would not be wiser to push efforts 617 towards the opening of these two cavities in ocean models, even at the lower resolution 618 of 1° , as was already done for NEMO in Smith et al. (2021) or Hutchinson et al. (2023). 619 On the same line, we suggest it is worth thinking about tuning the parameterisations 620 on the smaller ice shelves, and tuning the parameters and neural networks differently on 621 the larger ice shelves. 622

There is also space for improvement in the definition of input temperatures and 623 salinities. Like in Burgard et al. (2022), the input profiles of temperature and salinity 624 are here averaged over a given domain in front of the ice shelf. Then, we extrapolate the 625 properties to the ice-draft depth. To give the neural network more information about 626 the whole profile, we also gave it the mean and standard deviation of these extrapolated 627 temperature and salinity. However, machine learning gives us the opportunity to think 628 bigger than traditional statistics when representing information about a given domain. 629 One direction that could be explored in further development is the encoding of the im-630 portant information about the water masses in front of the ice shelf using a machine learn-631 ing technique. Ideally, this technique would take in a three-dimensional (horizontal plane 632 and depth), or even a four-dimensional (taking also time as input to account for lags and 633 residence time), field of temperature and salinity in front of the ice shelf and encode in-634 formation about this field in a format to be given to the neural network. Such encod-635 ing might contain more information about the spatial distribution of the properties in 636 front of the ice shelf and therefore potentially encode changes in the ocean circulation 637 which might change the circulation within the cavities, as expected to happen in warmer 638 conditions for the Filchner-Ronne ice shelf (Naughten et al., 2021). 639

Rosier et al. (2023) showed that a convolutional architecture can also be used to 640 infer basal melt rates from hydrographic and geometric properties. A convolutional ar-641 chitecture, often U-Nets, is the preferred choice in many current studies exploring the 642 application of machine learning to Earth System Sciences (e.g. Ebert-Uphoff & Hilburn, 643 2020; Andersson et al., 2021; Finn et al., 2023). In the case of basal melt and the ocean 644 circulation in the cavity, such architectures clearly make sense as they can capture spa-645 tial patterns and correlations. However, these architectures require much more simula-646 tion data for training as they take each time step as one training sample while our ap-647

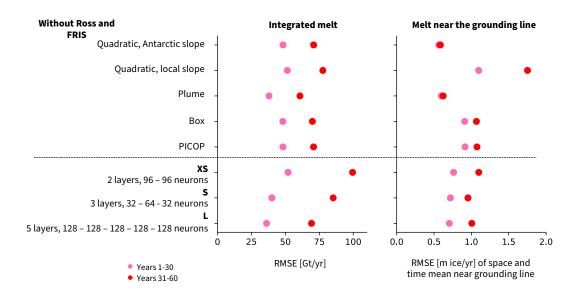


Figure 7. Summary of the RMSE of the integrated melt $(RMSE_{int})$ [in Gt/yr] and of the RMSE of the melt rate averaged over time and space near the grounding line $(RMSE_{GL})$ [in m ice/yr] computed on all ice shelves except Ross and Filchner-Ronne ice shelves for a selection of traditional parameterisations and a subsample of neural networks for the application on a simulation with 4xCO₂ forcing. The lighter colors represent the first 30 years of simulation and the darker colors the last 30 years of simulation.

proach takes each time step and grid cell as one training sample. Also, Rosier et al. (2023)
demonstrate the performance of their MELTNET in a fixed domain and have not yet
shown how to apply it to larger ice shelves than this domain. MELTNET remains however a promising approach and we are looking forward to its further development.

Finally, this study has focussed on the emulation of one ocean model at a given res-652 olution. We acknowledge that NEMO's simulation of basal melt rates is not a perfect 653 reflection of reality. Therefore, an interesting further direction to follow would be to train 654 a neural network to emulate NEMO at other resolutions and also to emulate other cavity-655 resolving ocean models. In this context, to ensure that the relationship remains sensi-656 ble, we suggest training separate emulators and using them as an ensemble. This would 657 provide an ensemble of emulators to be used as a variety of basal melt parameterisations, 658 in addition to physics-based parameterisations. In a context where basal melt remains 659 one of the main sources of uncertainty in projections of the Antarctic contribution to sea-660 level rise, a wide sample of this uncertainty in the form of a higher variety of parame-661 terisations is welcome. 662

663 6 Conclusions

In conclusion, we show that a rather simple neural network architecture can be used to emulate a cavity-resolving ocean model. Our multilayer perceptrons are designed to be rather simply usable as a basal melt parametrisation for ice-sheet modellers. They use input properties needed for the traditional parameterisations already and can be applied on the grid-cell level, similarly to most traditional parameterisations. While they struggle nearly as much as traditional parameterisations to generalise to ice shelves unseen during tuning, the neural networks generalise much better on time blocks unseen during training and the patterns are clearly better represented. In the demanding testing phase, on a dataset produced with different NEMO parameters, geometry perturbations unseen during training and different forcing, they still perform at least as well or even better than traditional parameterisations, both in historical and much warmer conditions.

These results are promising as neural networks and machine learning in general are topics that have been gaining lots of traction lately and efforts are done in many disciplines of the Earth System Sciences to explore their application. In this study, we provide guiding thoughts for further exploration and refinement of this approach, while this first proof of concept can already be used as an additional parameterisation in the icesheet modelling landscape.

Appendix A Distributions of variables of interest in the training and testing ensemble

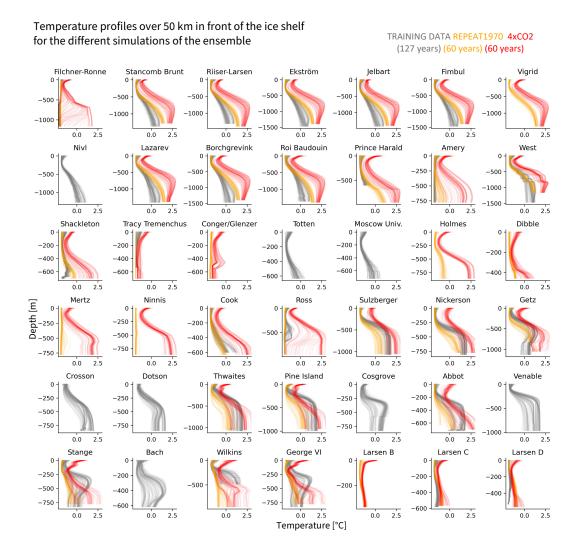
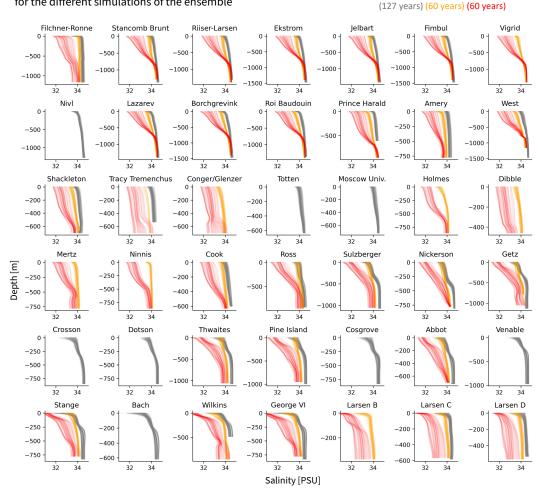


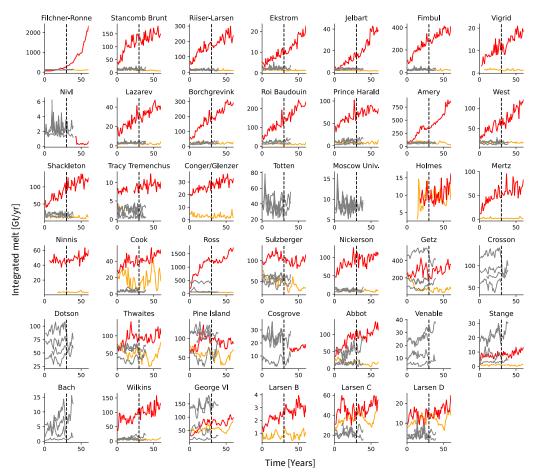
Figure A1. Input profiles of temperature for the different ice shelves. Profiles of the training ensemble are shown in grey, profiles for the REPEAT1970 run in orange and profiles for the $4xCO_2$ run in red.

TRAINING DATA REPEAT1970 4xCO2



Salinity profiles over 50 km in front of the ice shelf for the different simulations of the ensemble

Figure A2. Input profiles of salinity for the different ice shelves. Profiles of the training ensemble are shown in grey, profiles for the REPEAT1970 run in light blue and profiles for the $4xCO_2$ run in dark blue.



Integrated melt over time

TRAINING DATA REPEAT1970 4xCO2 (127 years) (60 years) (60 years)

Figure A3. Timeseries of the integrated melt for the different ice shelves. The training ensemble is shown in grey, the REPEAT1970 run in orange and the $4xCO_2$ run in red. The black dashed line limits the first and second 30-year block used in Sec. 4 for the $4xCO_2$ run

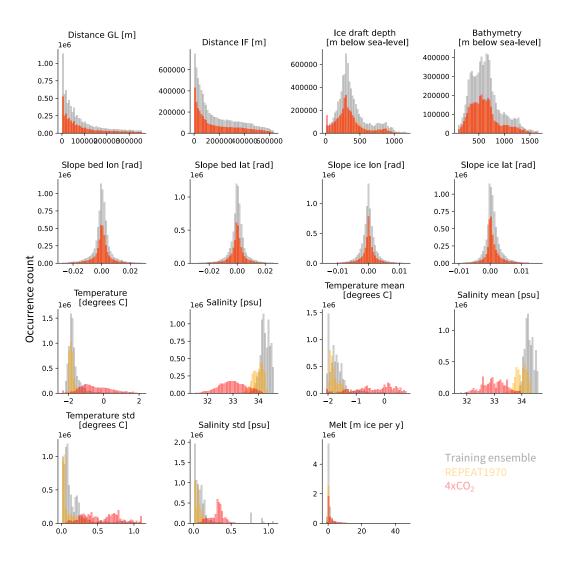


Figure A4. Distribution (occurrence count) of the different input variables and the melt over the training ensemble (grey), the REPEAT1970 run (orange) and the $4xCO_2$ run (red).

⁶⁸⁴ Open Research

The simulation data from Burgard et al. (2022) used for the training ensemble can be found on Zenodo: https://doi.org/10.5281/zenodo.7308352. The simulation data from (Smith et al., 2021) used for the testing ensemble will be uploaded on Zenodo as soon as possible. All code to train the neural networks and produce the figures can be found on Github: https://github.com/ClimateClara/basal_melt_neural_network and will be uploaded to Zenodo upon paper acceptance.

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CB and NCJ developed the original idea of this paper. CB carried out all analyses and wrote the manuscript. PM carried out the NEMO simulations used for training and RSS carried out the UKESM simulations. NCJ, RS and JC provided valuable help and code for the definition of the ice-shelf masks when the ice shelves evolve over time. TSF provided methodological input on the training of neural networks and JEJ provided useful input about how to think about machine learning. CB, NCJ, PM, RS, RSS, JC, TSF, JEJ contributed to discussions.

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Emulating present and future simulations of melt rates at the base of Antarctic ice shelves with neural networks

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Key Points:

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11	•	We show that simple neural networks can produce reasonable basal melt rates by
12		emulating circum-Antarctic cavity-opening ocean simulations.
13	•	Predicted melt rates for present and warmer conditions are similar or closer to the
14		reference simulation than traditional parameterisations.
15	•	We show that neural networks are suited to be used as basal melt parameterisa-
16		tions for century-scale ice-sheet projections.

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17 Abstract

Melt rates at the base of Antarctic ice shelves are needed to drive projections of the Antarc-18 tic ice sheet mass loss. Current basal melt parameterisations struggle to link open ocean 19 properties to ice-shelf basal melt rates for the range of current sub-shelf cavity geome-20 tries around Antarctica. We present a novel parameterisation based on deep learning. 21 With a simple feedforward neural network, or multilayer perceptron, acting on each grid 22 cell separately, we emulate the behavior of circum-Antarctic cavity-resolving ocean sim-23 ulations. We explore different neural network sizes and find that, in all cases contain-24 ing at least one hidden layer, this kind of emulator produces reasonable basal melt rates 25 for our training ensemble, closer to the reference simulation than traditional parameter-26 isations. For testing, we use an independent ensemble of simulations that was produced 27 with the same ocean model but with different model parameters, different cavity geome-28 tries and different forcing. In this challenging test, traditional and neural network pa-29 rameterisations yield similar results on present conditions. In much warmer conditions 30 than the training ensemble, both traditional parameterisations and neural networks strug-31 gle, but the neural networks tend to produce basal melt rates closer to the reference than 32 a majority of traditional parameterisations. These neural networks are therefore suit-33 able for century-scale Antarctic ice-sheet projections. 34

35 Plain Language Summary

A warmer ocean around Antarctica leads to higher melting of the floating ice shelves, 36 which influence the ice loss from the Antarctic ice sheet and therefore sea-level rise. In 37 computer simulations of the ocean, these ice shelves are often not represented. For sim-38 ulations of the ice sheet, so-called parameterisations are used to link the oceanic prop-39 erties in front of the shelf and the melt at their base. We show that this link can be em-40 ulated with a simple neural network, which performs at least as well as traditional phys-41 ical parameterisations both for present and much warmer conditions. This study also 42 proposes several potential ways of further improving the use of deep learning to param-43 eterise basal melt. 44

45 **1** Introduction

The contribution of the Antarctic Ice Sheet to sea-level rise has been increasing in 46 past decades and this increase is projected to continue with increasing greenhouse gas 47 emissions (Fox-Kemper et al., 2021). Most of the mass loss is occurring at the margins 48 of the ice sheet through faster ice flow from the grounded ice sheet to the ocean, mainly 49 in West Antarctica (Mouginot et al., 2014; Rignot et al., 2014; Scheuchl et al., 2016; Khazen-50 dar et al., 2016; Shen et al., 2018; The IMBIE Team, 2018). This is because the float-51 ing ice shelves at the margins of the ice sheet, which usually buttress the ice flow, are 52 rapidly thinning and retreating due to ocean-induced melt at their base (Rignot et al., 53 2013; Paolo et al., 2015; Adusumilli et al., 2020). In some bedrock configurations, increased 54 ocean-induced melt can even trigger marine ice sheet instabilities (Weertman, 1974; Schoof, 55 2007; Gudmundsson et al., 2012), which have the potential to strongly increase Antarc-56 tic mass loss, on timescales below a century (Fox-Kemper et al., 2021). This makes ocean-57 induced sub-shelf melt, or basal melt, one of the main sources of uncertainty for future 58 projections of sea-level rise. 59

Basal melt is a result of warm ocean water coming into contact with the base of the ice shelf. Which water masses reach the ice-ocean interface depends on the circulation of the water, not only in front of the ice shelf, but also after entering the ice-shelf cavity (Dinniman et al., 2016). As a consequence, to simulate the properties of the water at the ice-ocean interface accurately, both the ocean circulation around Antarctica and the circulation in the cavities below the ice shelves need to be simulated accurately. A few global or circum-Antarctic ocean models already include ice-shelf modules (Losch,

2008; Timmermann et al., 2012; Dinniman et al., 2015; Mathiot et al., 2017; Comeau et 67 al., 2022), but such ocean models are expensive to run on long timescales or for large en-68 sembles. Instead, a majority of the global climate models used until now in the Coupled 69 (CMIP) or Paleoclimate (PMIP) Model Intercomparison Projects still poorly represent 70 the ocean dynamics along the Antarctic margins and do not include ice-shelf cavities (Beadling 71 et al., 2020; Heuzé, 2021). Getting the right water masses in the right place around Antarc-72 tica is a matter for global and regional ocean modelling and will not be the focus of this 73 study. In this study, we focus on the circulation within the ice-shelf cavities and the re-74 sulting melt. 75

To infer the basal melt forcing for projections of the Antarctic contribution to sea-76 level rise, ice-sheet models commonly rely on parameterisations linking hydrographic prop-77 erties in front of the ice shelves, given by observations or oceanic output from global cli-78 mate models, and the basal melt (Jourdain et al., 2020). Due to different assumptions 79 and simplifications concerning the circulation in the cavities, the range of existing basal 80 melt parameterisations leads to widely differing melt patterns and associated contribu-81 tions to sea-level rise (Favier et al., 2019; Burgard et al., 2022). The magnitude of the 82 resulting uncertainty contribution is similar, or even larger, than the choice of emission 83 scenario used to force the projections (Seroussi et al., 2020; Edwards & the ISMIP6 Team, 84 2021).85

Emulating the three-dimensional ocean circulation within the cavity in simplified 86 physical parameterisations is challenging and calls for exploring alternative approaches. 87 We suggest that deep learning can be one tool to tackle this challenge. In recent years, 88 the amount of ocean simulation output including ice-shelf cavities has increased and tools 89 that make the application of deep learning techniques easily accessible have been devel-90 oped, opening up the possibility of developing a neural network parameterisation for basal 91 melt. If trained with high-resolution model output, a neural network parameterisation 92 could implicitly include more intrinsic information about the system than a traditional 03 physical parameterisation. This approach has been applied promisingly in several areas of Earth System Sciences in the form of multilayer perceptrons applied on the grid-cell 95 level (e.g. Gentine et al., 2018; Rasp et al., 2018), convolutional neural networks applied 96 on multidimensional fields (e.g. Bolton & Zanna, 2019; Rosier et al., 2023) or random 97 forests (e.g. Yuval & O'Gorman, 2020). 98

Deep learning has also been explored for basal melt parameterisations. Rosier et 99 al. (2023) performed promising experiments that showed that a cavity-resolving ocean 100 model can be emulated with a convolutional neural network in a variety of idealised ice-101 shelf geometries. In the present study, we choose a different deep learning approach to 102 developing such a *deep emulator*, or *surrogate model*, which differs on two fundamental 103 points. On the one hand, we train on the circum-Antarctic cavity-resolving ocean sim-104 ulations with realistic geometries used in Burgard et al. (2022). On the other hand, we 105 use a multilayer perceptron architecture applied to each grid cell, as preliminarily ex-106 plored in Bouissou et al. (2022). In the following, we present a proof of concept for a mul-107 tilayer perceptron, which takes in hydrographic properties in front of the ice shelf and 108 the geometric information at each grid point. In Sec. 2, we present the training and test-109 ing data, the neural network architecture, and the evaluation procedure. In Sec. 3, we 110 show that the multilayer perceptron can successfully emulate cavity-resolving ocean sim-111 ulations and produce integrated basal melt and patterns at least as close as but gener-112 ally closer to the reference than traditional parameterisations in conditions similar to present. 113 In Sec. 4 we explore the applicability of such a neural network to an independent set of 114 simulations produced with a few different model parameters, slightly different geome-115 tries and in warmer oceanic conditions. Finally, in Sec. 5, we discuss the lessons learned 116 from our study and give an outlook on possible directions to explore further in the fu-117 ture. 118

¹¹⁹ 2 Data and Methods

The goal of this study is to explore if and how a neural network, in the form of a multilayer perceptron, can emulate the link between hydrographic properties in front of an ice shelf, geometric characteristics of the cavity, and the melt rates at its base as simulated by a cavity-resolving ocean model. In the following, we present the ocean model used and the set of simulations used for training, validation and testing the neural network; the neural network, its architecture, and its input variables; and the training and testing procedure.

2.1 Data

127

We choose to emulate a cavity-resolving version of the 3-D primitive-equation coupled ocean-sea-ice model NEMO (Nucleus for European Modelling of the Ocean, NEMO Team, 2019) run on the eORCA025 horizontal grid (Storkey et al., 2018). This grid has a resolution of 0.25° in longitude on average, i.e. a resolution of 4 to 14 km in the Antarctic seas and below the ice shelves, which is sufficient to capture the basic ocean circulation below multiple Antarctic ice shelves (Mathiot et al., 2017; Bull et al., 2021).

For the training phase, we use the same ensemble of simulations as used for the as-134 sessment of traditional basal melt parameterisations in Burgard et al. (2022). The en-135 semble is composed of four ocean simulations spanning 30 to 40 years, depending on the 136 simulation, between 1979 and 2018. They were run with a standalone version of NEMO 137 and forced with atmospheric forcing from JRA55-do version 1.4 (Tsujino et al., 2018). 138 The Antarctic continental shelf bathymetry and ice shelf draft are constant and based 139 on Bedmachine Antarctica version 2 (Morlighem, 2020; Morlighem et al., 2020). The sim-140 ulations in the ensemble differ in a small number of parameters which are not directly 141 related to the physics driving the ocean circulation and melt within the ice-shelf cavi-142 ties but rather lead to a variety of hydrographic properties all around Antarctica. A more 143 detailed description of the exact model configuration and differences in parameters can 144 be found in Burgard et al. (2022). 145

For the testing phase, we use two simulations independent from the ensemble used 146 for training. In this case, NEMO was run in coupled mode as the oceanic component of 147 the Earth System Model UKESM1.0-ice (Smith et al., 2021), which couples the UK Earth 148 System Model (UKESM1, Sellar et al., 2019) to an adapted version of the ice-sheet model BISICLES (Cornford et al., 2013). In this coupled configuration, the cavities below the 150 ice shelves are open and the ice-shelf melt is computed with the same approach as in the 151 training ensemble (as proposed by Mathiot et al., 2017). This means that a z^* coordi-152 nate is used for depth and the three equations are used to parameterise the ice-shelf melt 153 in the ice-ocean boundary layer. Due to the coupled setup, the ice-shelf draft evolves ac-154 cording to the simulated evolution of the ice sheet. Note that the position of the ice front 155 at the surface remains fixed by ice-sheet model design. More details about the config-156 uration of NEMO in this model setup can be found in Smith et al. (2021). The two test 157 simulations differ in their atmospheric forcing. In the first one, which we will call "RE-158 PEAT1970", UKESM1.0-ice was run for several decades under constant 1970 greenhouse 159 gas and other forcings. In the second one, which we will call "4xCO2", UKESM1.0-ice 160 was run for several decades under instantaneously quadrupled 1970 CO_2 concentrations. 161 In our study, we use 60 years of simulation, from year 10 to year 70, for both runs. 162

The training and the testing dataset result from NEMO simulations. Nevertheless, next to differences in forcing from the atmosphere and the ice and bed geometry, the training and testing ensembles also differ in several technical aspects of NEMO. The training simulations were run with the version of 4.0.4. of NEMO (NEMO Team, 2019), including the sea-ice model SI³, while the test simulations were run with the version 3.6 of NEMO (Madec & NEMO Team, 2017) and version 5.1 of the Community Ice CodE (CICE, Hunke et al., 2015). In addition, a few different parameter choices may affect the

link between hydrographic properties in front of the ice shelf and the melt at the base 170 of the ice shelf. The training ensemble was computed on 121 vertical levels (represent-171 ing 20 m at 600 m depth), while the testing ensemble was computed on 75 vertical lev-172 els (representing 60 m at 600 m depth). In both ensembles, the thickness of the top bound-173 ary layer is bound at 20 m but can differ locally due to the different vertical resolutions. 174 In the training ensemble, the thermal Stanton number is set to 7×10^{-4} while in the test-175 ing ensemble the thermal Stanton number is set to 1.45×10^{-3} . In the training ensem-176 ble, the top tidal velocity varies locally based on the CATS2008 dataset (Padman et al., 177 2008; Howard et al., 2019), while it is fixed to 5 cm/s in the testing ensemble. In con-178 clusion, this means that the testing ensemble is a slightly different model than the model 179 which the neural network is trained to emulate and therefore represents a demanding test-180 ing experiment. 181

The training and testing ensembles cover a range of states that do not necessar-182 ily match observational estimates of hydrographic properties and basal melt rates. In 183 both standalone and coupled mode, eORCA025 configurations are prone to biases in the 184 ocean circulation around Antarctica (Smith et al., 2021). Nevertheless, in Burgard et al. 185 (2022), we showed that, if the forcing and parameters were carefully chosen to reproduce 186 realistic ocean conditions in the Southern Ocean, the resulting basal melt rates were in 187 agreement with observational estimates from Rignot et al. (2013). The physical link be-188 tween the hydrographic properties in front of the ice shelves and the basal melt rates is 189 therefore reasonable. Based on this assumption, biases in the input properties should not 190 affect the credibility of the training and evaluation procedure and the resulting neural 191 network. On the contrary, a large variety of states is even beneficial because it provides 192 more cases for our neural network to train on than only using the very limited sample 193 of observations. 194

On a more technical note, for this study, the NEMO output was interpolated bi-195 linearly to a stereographic grid of 5 km spacing, as ice-sheet models and basal melt pa-196 rameterisations are commonly run on a stereographic grid. All pre-processing, training, 197 testing, and analysis is conducted using this regridded data. From this regridded data, 198 we cut out the different ice shelves according to latitude and longitude limits defined on 199 the present geometry (details found in Burgard (2022)) and then apply a routine to adapt 200 this mask to slightly different geometries, like the ones resulting from the fully coupled 201 UKESM1.0-ice runs. Of these ice shelves, we only keep the largest ice shelves. The ef-202 fective resolution of physical ocean models, i.e. the resolution below which the circula-203 tion might not be resolved well, is typically 5 to 10 times the grid spacing (Bricaud et 204 al., 2020). We empirically choose a cutoff at an area of 2500 km² (i.e. 6.25 Δx) to be 205 in this range while keeping a sufficiently large number of ice shelves. Due to different ge-206 ometries in the training and testing ensemble, this results into a slightly different ensem-207 ble of resolved ice shelves in these two ensembles (as listed in the figures of Appendix 208 A). 209

210

2.2 Neural network

We design our neural network to predict the basal melt rates based on information 211 about the ocean temperature and salinity in front of the ice shelf and about the ice-shelf 212 geometry (Fig. 1). To link the input to the prediction, we use a multilayer perceptron, 213 which is applied to each grid cell independently. A multilayer perceptron is the simplest 214 form of a neural network and is a composition of functions (also called hidden layers), 215 which takes an input array containing any number of variables and outputs a prediction. 216 Specifying its number of neurons, each hidden layer is characterised by its parameters 217 - the weights and biases, that connect each layer to its previous layer and shift the val-218 ues in the hidden layer, respectively. An activation function in the hidden layer intro-219 duces non-linearities in the relationship between input and output. In this study, we ex-220 plore different numbers of layers and numbers of neurons per layer. As activation func-221

- tion, we use the rectified linear unit (ReLU, Fukushima, 1975; Nair & Hinton, 2010). The
- multilayer perceptron is implemented in Python with the package Keras (Chollet et al.,
- 224 2015).

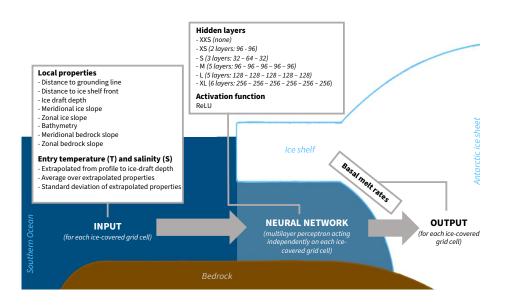


Figure 1. Schematic of the workflow around our neural network.

The strength of a neural network, and supervised machine learning techniques in 225 general, is that it can reproduce complex non-linear relationships without being given 226 the driving equations behind the data. Instead, its performance is driven by the super-227 vised training phase, which determines the weights and biases of each neuron in the net-228 work. During training, the loss, describing the averaged distance of the network predic-229 tions to a given target output, is backpropagated to the weights of the network. The weights 230 are then optimised with stochastic gradient descent. The training dataset is randomly 231 split up into batches, over which the optimisation is looped. A complete pass through 232 the batches defines an epoch, and the weights and biases are optimised over several such 233 epochs. In parallel to the training, the neural network is applied to a validation dataset 234 to monitor its performance on data that has not been used for the training. After train-235 ing, the final performance of the neural network is estimated by applying it to a previ-236 ously unseen testing dataset. 237

In this study, to train the neural network, the loss which we reduce is the meansquared-error over all ice-covered points between the predicted (m_{NN}) and target (m_{ref}) basal melt rates,

$$MSE = \frac{\sum_{i}^{N_{\text{pts}}} \sum_{t}^{N_{\text{years}}} (m_{\text{NN}}[i,t] - m_{\text{ref}}[i,t])^2}{N_{\text{pts}} N_{\text{years}}}$$
(1)

where N_{pts} is the number of ice-covered grid points and N_{years} is the number of years 241 used in the training. In Burgard et al. (2022), we argued that tuning on the grid-cell level 242 would give too much weight to the larger ice shelves, as they cover a larger area. We still 243 agree with this statement for traditional parameterisations because they already intrin-244 sically contain assumptions about the physics of the circulation and the melt before tun-245 ing and have only one or two tuneable parameters. In the case of our neural network, 246 the relationship between the properties in front of the ice shelf and the melt is learnt from 247 scratch, and it contains a larger number of parameters to adjust. We therefore argue that 248 training on the grid-cell level is more sensible. 249

The neural network is optimised with Adam (Kingma & Ba, 2014), an initial learning rate of 0.001, $\beta_1=0.9$ and $\beta_2=0.999$. We split the training dataset in batches with a size of 512 samples and optimise the neural network for at most 100 epochs. If the validation loss is not improved for 5 epochs, we reduce the learning rate by a factor of 2. If the validation loss is not improved for 10 epochs, we stop the training early. After early stopping, the model weights with the lowest validation loss are restored.

2.3 Input variables

The multilayer perceptron takes an array of variables as input for each grid cell independently. In our case, the input array contains information about the geometrical properties of the grid cell and the hydrographic forcing (Fig. 1).

For the geometrical properties, the input contains the following information: the ice draft depth, the local meridional and zonal slopes of the ice draft, the bathymetry, the local meridional and zonal slopes of the bedrock, and the distance of the grid cell to the nearest grounding line cell and the distance to the nearest ice front cell. All these variables are defined on the same horizontal plane and domain as the output array, the basal melt rates.

For the hydrographic forcing, more pre-processing is needed. To map the hydro-266 graphic forcing to the same grid cells as the other input variables, we proceed in the same 267 manner as for traditional simple parameterisations in Burgard et al. (2022). First, we 268 convert the conservative temperature and absolute salinity given by NEMO into poten-269 tial temperature and practical salinity with the GSW oceanographic toolbox (Firing et 270 al., 2021). Second, we average the potential temperature and practical salinity, respec-271 tively, over the continental shelf within 50 km of the front of each ice shelf. The conti-272 nental shelf is defined as grid cells where the depth of the bathymetry is shallower than 273 1500 m. The 50 km criterion imitates CMIP-type global ocean models that have reso-274 lutions around 1° (Heuzé, 2021), corresponding to a distance of between 38 km $(70^{\circ}S)$ 275 and 56 km (60° S) in longitude. Third, we extrapolate the temperature and salinity from 276 these mean profiles in front of the ice shelf to the local ice-draft depth, resulting in one 277 local temperature and local salinity value per grid cell in the ice-shelf domain. Fourth, 278 we also compute, for each time step, the average and standard deviation of these extrap-279 olated temperature and salinity fields and use them as additional input variables for each 280 grid cell. 281

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2.4 Training, validation and testing methodology

In a first step, we explore different neural network sizes using the method of cross validation on our training ensemble. In a second step, we choose a subsample of the neural networks to explore their performance on the testing dataset.

We conduct two variations of leave-one-block-out cross validation to estimate the 286 validation loss (MSE as defined in Eq. 1), one on the ice shelf dimension and one on the 287 time dimension, like in Burgard et al. (2022). This approach consists of dividing the dataset 288 into N blocks, training the neural network to minimise the training loss on N-1 blocks 289 and using the left-out block to compute the validation loss (Wilks, 2006; Roberts et al., 290 2017). The procedure is re-iterated N times, leaving out each of the N blocks succes-291 sively, so that, in the end, each N-th block has been left out of training once. All pre-292 dictions for the left-out blocks, using the separately trained neural networks, are then 293 concatenated to form a "synthetically independent" evaluation dataset. Applying an eval-294 uation metric on this evaluation dataset, we assess how well the neural network gener-295 alises to data "unseen" during training. We use N=35 for the cross validation over ice 296 shelves. For the cross validation over time, we divide the years into blocks of approxi-297 mately 10 years (ten 10-year blocks and three 9-year blocks) to reduce the effect of au-298

Neural network configuration	Number of hidden layers	Number of neurons
XXS	0	0
XS	2	96/96
S	3	32/64/32
\mathbf{M}	5	96/96/96/96/96
L	5	128/128/128/128/128
XL	6	256/256/256/256/256/256

 Table 1.
 Neural network size of the different variations explored in the cross validation.

to correlation, which is typically 2 to 3 years in our input temperatures. This results in N=13 for the cross validation over time.

Before training, we normalise the training sample to put each of the 14 input variables (listed in Fig. 1) as well as the output variable on a similar order of magnitude and avoid potential problems of gradient explosion. We do so by subtracting the mean and dividing by the standard deviation of the training sample. To avoid that validation data leaks into the training, this normalisation is reiterated for each iteration of the cross validation.

We use the framework of cross validation to evaluate not only one but several neural networks to estimate the effect of their size on their performance. We sample different sizes ranging from an extra-extra small (XXS) neural network, with no hidden layer, and thus corresponding to a linear regression, to an extra-large (XL) neural network, with six hidden layers, each containing 256 neurons. The different sizes are listed in Table 1.

To evaluate the resulting basal melt rates, we use the same metrics as in Burgard et al. (2022), namely: (1) the root-mean-squared error (RMSE) of the yearly integrated melt on the ice-shelf level and (2) the RMSE of the mean melt near the grounding line for each ice shelf. For the former, we compute the RMSE between the simulated and emulated yearly integrated melt (M) of the individual ice shelves [in Gt/yr] as follows:

$$RMSE_{\rm int} = \sqrt{\frac{\sum_{k=1}^{N_{\rm isf}} \sum_{t=1}^{N_{\rm years}} (M_{\rm NN}[k,t] - M_{\rm ref}[k,t])^2}{N_{\rm isf}N_{\rm years}}}$$
(2)

where the subscript NN stands for neural network, N_{isf} is the number of ice shelves and N_{years} the number of simulated years, and the integrated melt M of ice shelf k [in Gt/yr] is:

$$M[k] = \rho_i \times 10^{-12} \sum_{j}^{N_{\text{grid cells in } k}} m_j a_j \tag{3}$$

where ρ_i is the ice density, m_j is the melt [in m ice per year] in grid cell j, and a_j is the area of grid cell j. For the latter, we compute the RMSE between the simulated and emulated yearly mean melt rate near the grounding line [in m ice per year]:

$$RMSE_{\rm GL} = \sqrt{\frac{\sum_{k}^{N_{\rm isf}} \sum_{n}^{N_{\rm simu}} (m_{\rm GL,NN}[k,n] - m_{\rm GL,ref}[k,n])^2}{N_{\rm isf}N_{\rm simu}}}$$
(4)

where N_{simu} is the number of simulations in the ensemble and where m_{GL} for ice shelf k and simulation n is:

$$m_{\rm GL}[k,n] = \frac{1}{N_{\rm years \ in \ n}} \sum_{t}^{N_{\rm years \ GL \ near \ GL \ in \ k}} \frac{\sum_{j}^{N_{\rm grid \ cells \ near \ GL \ in \ k}} (m_j a_j)}{\sum_{j}^{N_{\rm grid \ cells \ near \ GL \ in \ k}} a_j}$$
(5)

The domain "near the grounding line" is the area covered by the first box prepared for the box parameterisation, when considering a maximum amount of five boxes, and is equivalent to approximately 10 % of the shelf area.

After cross validation, we choose a subsample of these neural networks to do fur-328 ther evaluation on a completely independent dataset. To do so, we reiterate the train-329 ing of the subsample of neural networks over the whole training dataset and choose to 330 work with a deep ensemble (Lakshminarayanan et al., 2017). The final weights and bi-331 ases of neural networks depend on the initialisation of the weights before the first train-332 ing iteration (Goodfellow et al., 2016). To account for this uncertainty and gain a more 333 robust performance from the neural networks, we reiterate the training of the subsam-334 ple of neural networks ten times with ten different random initialisations. We then ap-335 ply this deep ensemble of ten neural networks to the independent testing input and com-336 pute an ensemble mean over the ten resulting melt rates. Note that we only investigate 337 a small sample of neural network sizes for exploration in this study and do not claim that 338 the best performing neural network here is the best performing neural network for the 339 problem. This study is rather a proof of concept to encourage further research in this 340 direction. 341

³⁴² **3** Training and cross validation

343

3.1 Integrated melt and mean melt near the grounding line

The two evaluation metrics for the cross validation of the different neural network 344 sizes are shown in Fig. 2. In addition, to compare the performance to traditional param-345 eterisations, we show the evaluation metrics for a subset of existing parameterisations: 346 the quadratic local parameterisation using a constant Antarctic slope (e.g. Holland et 347 al., 2008) and using a local slope (e.g. Favier et al., 2019; Jourdain et al., 2020), the plume 348 parameterisation proposed by Lazeroms et al. (2019), the box parameterisation with the 349 same box amount as in Reese et al. (2018), and the PICOP parameterisation from Pelle 350 et al. (2019). The parameterisations are used as presented and tuned in Burgard et al. 351 (2022).352

Corresponding to a linear regression, the XXS neural network leads to a RMSE of a similar order as traditional parameterisations in the cross validation over time and, for the melt near the grounding line, in the cross validation over ice shelves as well. For the integrated melt, the cross validation over ice shelves leads to a comparably high RMSE. In the further course of this study, we therefore focus on neural networks that include hidden layers.

For both metrics, the RMSE for the cross validation over time is considerably reduced when using a neural network with hidden layers compared to traditional parameterisations and the XXS neural network. The RMSE for the cross validation over ice shelves is higher than for the cross validation over time but remains on the lower end of the range of RMSEs given by traditional parameterisations.

The RMSE_{int} of the cross validation over time is very similar between neural network sizes and spans between 6 Gt/yr (XL) and 11 Gt/yr (S). It remains well below the mean reference integrated melt on the ice-shelf level of 39 Gt/yr. The RMSE_{int} of the

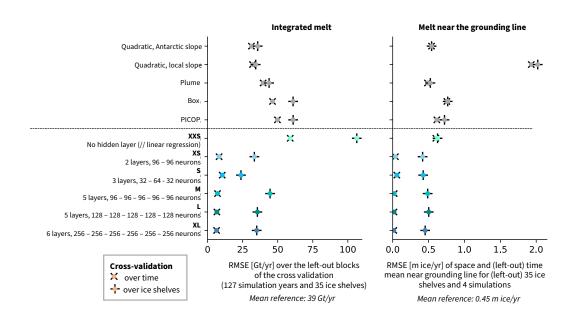


Figure 2. Summary of the RMSE of the integrated melt $(RMSE_{int})$ for the cross validation over time (×) and for the cross validation over ice shelves (+) for a selection of traditional parameterisations (as shown in Burgard et al., 2022) [in Gt/yr] (left) and summary of the RMSE of the melt rate averaged over time and space near the grounding line $(RMSE_{GL})$ [in m ice/yr] (right). The colors represent the different parameterisation approaches: traditional parameterisations (grey), neural network (shades of blue). The RMSE is computed following Eq. (2), left panel, and Eq. (4), right panel, on the synthetically independent evaluation dataset.

cross validation over ice shelves varies more and is higher, between 24 (S) and 45 Gt/yr
 (M). The performance does not correlate with the neural network size. On the contrary,
 the lowest RMSE_{int} of the cross validation over ice shelves is found for a comparably small
 neural network (S).

For the melt near the grounding line, the RMSE_{GL} does not vary much in both cross validations between neural network sizes. The cross validation over time leads to a very low RMSE, varying from 0.02 m/yr (M,L,XL) to 0.06 m/yr (S). The cross validation over ice shelves leads to a RMSE between 0.42 m/yr (XS,S) and 0.50 m/yr (L), on the same order as the mean reference melt near the grounding line on the ice-shelf level, which is 0.45 m ice/yr.

The neural networks have more difficulties generalising to unseen ice shelves than 377 generalising to unseen time periods. This means that one of the obstacles for the neu-378 ral networks' performance is the application to unknown cavity geometries. Some of the 379 cavity geometries are so different from the rest of the ensemble that they force the neu-380 ral networks to extrapolate far from their training domain. However, if they have seen 381 a given geometry at least once during training, they perform well on this geometry for 382 another time step. This aspect is encouraging, as this means that the neural networks 383 adapt well to temperature and salinity variations across the training ensemble. 384

3.2 Spatial patterns

385

To add on the metrics at the ice-shelf level, we analyse the spatial patterns resulting from the XS, S and L neural networks (Fig. 3) for the training ensemble member clos-

est to realistic conditions (called REALISTIC in Burgard et al., 2022). For the cross val-388 idation over time, the patterns of XS, S and L are nearly indistinguishable from the ref-389 erence for Filchner-Ronne, Pine Island, Fimbul, and Totten ice shelves. For Ross ice shelf, 390 all patterns are close to the reference, but the S pattern contains more widespread melt-391 ing.

392

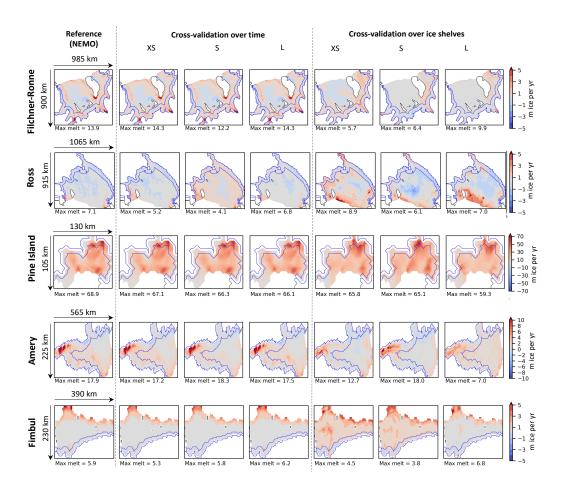


Figure 3. Subset of ice shelves for a visual evaluation of the melt patterns. This is the time average for the training ensemble member closest to real conditions (39 years) where the melt for each timestep has been computed with the neural network trained on the dataset leaving out that timestep (cross validation over time, columns 2 to 4) and where the melt of each ice-shelf has been computed with the neural network trained on the dataset leaving out that ice shelf (cross validation over ice shelves, columns 5 to 7). The blue line indicates the region used to evaluate the melt rate near the grounding line (which is defined as the first box in the 5-box setup of the box parameterisation).

For the cross validation over ice shelves, the patterns are not matching in as much 393 detail as in the cross validation over time. In particular for the two largest ice shelves, 394 Filchner-Ronne and Ross, it becomes clear that if the neural network has been trained 395 without one of them, it will mimic the spatial pattern of the other because they are the 396 only ones to share given ranges in the input variables, such as for example large distances 397 to the ice front and grounding line. For Filchner-Ronne and Ross, the result of the cross 398 validation over ice shelves does not match the reference in any of the neural networks. 399

For Pine Island and Amery, the XS and S patterns match the reference better than the L pattern, while, for Fimbul and Totten, the L pattern is a little better.

The low RMSE in the cross validation over time suggests an overfit on the geom-402 etry, which is fixed over time in the training dataset. The patterns very close to the ref-403 erence in the cross validation over time show that, even if our neural networks are ap-404 plied on each grid-cell separately, the location of the grid cell is more or less encoded in 405 one or more input variables. However, as our problem is not necessarily well constrained 406 with the input variables given, we suggest that this overfit can be used to our advantage. 407 Our hypothesis is that, if the neural network has seen each ice shelf once, it has captured the variety of geometries and will be able to generalise to future changes in these "known" 409 ice shelves. We do not expect new and completely different ice shelves to appear in the 410 next centuries. To assess this idea, we need to investigate how well the neural network 411 will perform on a geometry which is similar to but not identical to the training. 412

In the following, we investigate further if the neural networks are suitable for evolving ice-shelf geometries that are close to existing geometries and to temperature and salinity input properties outside the training range. We choose to continue with (1) the S size, because it has the lowest RMSE in the cross validation over ice shelves, (2) the XS size because it has similarly low RMSE to the larger sizes but remains very small and simple, and (3) the L size to include a larger neural network and explore potential differences during the testing compared to its behavior in the cross validation.

420 4 Testing on independent simulations

We apply our subsample of neural network sizes on two independent datasets, one 421 representing 60 years of constant 1970-forcing (REPEAT1970), and one representing warmer 422 conditions, i.e. 60 years of abrupt $4xCO_2$ forcing $(4xCO_2)$, from Smith et al. (2021). The 423 REPEAT1970 simulation has a relatively steady ice-sheet geometry, similar (but not iden-424 tical) to the training geometry and is useful to assess the sensitivity of the neural net-425 works to different near-present-day atmospheric conditions (from the UKESM atmosphere 426 component), to different parameters used in NEMO, and to slightly different geometries. 427 The 4xCO₂ simulation experiences larger changes in ice-sheet geometry and much warmer 428 conditions, which is useful to test the neural networks far outside of their training range. 429 As a consequence, this evaluation is demanding and permits to evaluate the limits of the 430 neural networks. 431

For evaluation, we divide the 4xCO₂ run into two 30-year blocks to capture potential differences with warming in time. As explained in Sec. 2.4, we train the XS, S and L neural networks ten times each, with ten different random initialisations. In the following, the results shown are averages over the predictions of the ten ensemble members for each neural network size.

437

4.1 Integrated melt and melt near the grounding line

The neural networks reproduce well the REPEAT1970 melt rates integrated over individual ice shelves, with a RMSE_{int} of 16 to 19 Gt/yr (Fig. 4a, left). This error is slightly larger than in the cross validation over time (see Fig. 2), and becomes similar to the quadratic and plume parameterisations. It should be noted that the RMSE_{int} of these parameterisations is lower than in the cross validation, likely because of the overall lower melt rates in this simulation (24 Gt/yr compared to 39 Gt/yr in the training ensemble). The neural networks still clearly outperform the box and PICOP parameterisation (RMSE_{int} \simeq 35 Gt/yr).

For the melt near the grounding line, all parameterisations are uncertain, with $RMSE_{GL}$ close to the reference mean melt near the grounding line of 0.34 m/yr (Fig. 4a, right). The neural networks and the traditional parameterisations yield similar $RMSE_{GL}$, be-

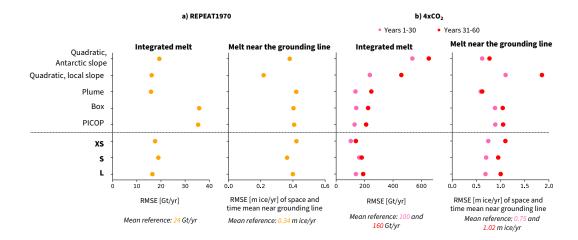


Figure 4. Summary of the RMSE of the integrated melt $(RMSE_{int})$ [in Gt/yr] and of the RMSE of the melt rate averaged over time and space near the grounding line $(RMSE_{GL})$ [in m ice/yr] for a selection of traditional parameterisations and a subsample of neural networks for the application on REPEAT1970 (a) and $4xCO_2$ (b). Note the change in x-axis between the (a) and (b) panels.

tween 0.36 and 0.42 m/yr, except the quadratic using a local slope, which leads to a slightly lower RMSE, on the order of 0.22 m/yr.

For the warmer conditions $(4xCO_2)$, all parameterisations struggle to reproduce 450 the integrated melt on the ice-shelf level, with high spread in performance between the 451 parameterisations (Fig. 4b, left). The RMSE_{int} is multiplied by more than 10 for the neu-452 ral networks and reaches nearly 650 Gt/yr for the quadratic parameterisation using an 453 Antarctic slope in the second period. While this jump in RMSE can be explained by a 454 higher mean reference integrated melt (100 Gt/yr for the first period and 159 Gt/yr for 455 the second period, see also Fig. A3), it is probably also a result of forcing unseen dur-456 ing training such as much warmer and less saline ocean conditions (Figs. A1 and A2). 457 Over both periods, the neural networks remain at the lower range of the difference to 458 the reference melt rates. While neural networks, plume, box and PICOP parameterisa-459 tion have comparable RMSEs for the first warm period (between 103 and 163 Gt/yr), 460 the RMSE increases more for the plume, box and PICOP parameterisation (between 211 461 and 248 Gt/yr) than for the neural networks (between 138 and 191 Gt/yr) in the even 462 warmer second period. 463

For the melt near the grounding line, the parameterisations perform differently than 464 for the integrated melt, pointing to potential challenges outside the domain near the ground-465 ing line. The neural networks perform in a similar uncertain manner as in the REPEAT1970 466 case (Fig. 4b, right). Their RMSE_{GL} (0.69-0.75 m/yr in the first period and 0.95-1.10 m/yr 467 in the second period) is close to the reference mean melt near the grounding line (0.75 m/yr)468 for the first period and 1.02 m/yr for the second period). In the first period, only the 469 quadratic local parameterisation using an Antarctic slope and the plume parameterisa-470 tion have lower $RMSE_{GL}$ (0.62 and 0.59 m/yr respectively), while in the second period 471 only the quadratic parameterisation using a local slope performs clearly worse than the 472 other parameterisations. For all, the RMSE increases with warmer conditions but the 473 gap between the periods depends on the parameterisation, ranging from a difference of 474 0.04 m/yr for the plume parameterisation to a difference of 0.76 m/yr for the quadratic 475 parameterisation using a local slope. 476

From this demanding application on an independent testing dataset, several con-477 clusions can be drawn. First, the neural networks apply reasonably well to data inde-478 pendent from training in present conditions. This means that, if they have seen all ge-479 ometries of the main circum-Antarctic ice shelves, they can adapt to slightly different geometries. This is even more encouraging as the testing simulations were conducted with 481 a slightly different version of NEMO than the neural networks were trained on. Second, 482 none of the neural networks seems to constantly be the one with the best performance 483 for all metrics. Third, the RMSE of the neural networks is higher when applied to warmer 484 conditions, but, in comparison with the traditional parameterisations, it performs at least 485 as well or even better. 486

487 4.2

4.2 Spatial patterns

Looking at the spatial patterns averaged over the last 10 years of the $4xCO_2$ run, 488 it becomes clear that all parameterisations, both neural networks and traditional ones, 489 struggle with warmer conditions and different geometries to the training ensemble (Fig. 5). 490 The maximum melt rates remain far below the maximum melt rates of the reference for 491 all of them except the quadratic parameterisation using the local slope, which largely 492 overestimates the maximum melt rates (as seen already in Burgard et al., 2022). Look-493 ing at the general patterns, the neural networks tend to overestimate the melt on wide areas of Filchner-Ronne and Ross but underestimate it over the whole ice shelf for smaller 495 ones. The quadratic parameterisations (both using Antarctic and local slope) and, in some 496 cases, the plume parameterisation, tend to overestimate the melt over wide areas, in par-497 ticular for the Ross and Filchner-Ronne ice shelves. The box parameterisation under-498 estimates the melt for all ice shelves, completely missing regions of strong melt. 499

500 5 Discussion

In this study, we showed that a simple multilayer perceptron can emulate melt rates 501 as simulated by the cavity-resolving ocean model NEMO. This result is encouraging for 502 further development because, as it is applied on a grid-cell level, it allows larger amounts 503 of training data to be used than architectures containing convolutions such as MELT-504 NET (Rosier et al., 2023) or, more generally, U-Nets (Ronneberger et al., 2015), which 505 take spatial domains as inputs. In addition, this architecture is independent of the do-506 main size and is therefore directly applicable to any ice shelf around Antarctica. In the 507 following, we discuss insights from this study and possible further improvements to this 508 approach. 509

510

5.1 Variable importance

One argument that is often made against the use of neural networks is that they 511 remain statistical emulators of the training data and do not contain any physical con-512 straints. The performance when applied to a slightly different model and to different con-513 ditions (see Sec. 4) already gives us a sense that the neural networks can reasonably adapt 514 to conditions outside of training. In addition, we now perform a sanity check to verify 515 that the neural network is doing "the right thing for the right reasons". This sanity check 516 also gives insight into the importance of the different input variables and could help fu-517 ture development of deep learning parameterisations as well as physical parameterisa-518 tions to focus on these variables. 519

To assess the importance of the different variables on the performance of the neural networks, we apply two variations of the permute-and-predict approach. In the permuteand-predict approach, one of the variables is shuffled randomly and used as input for the neural network alongside the other variables that remain in the original order. In the first variation (Fig. 6a), we shuffle the input variables within the REPEAT1970 sample to eval-

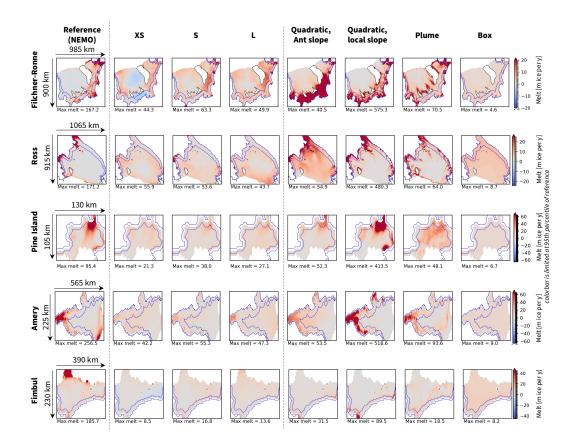


Figure 5. Subset of ice shelves for a visual evaluation of the melt patterns. This is the time average for the last 10 years of the $4xCO_2$ run. The colorbar is limited to the 95th percentile of the NEMO reference. The blue line indicates the region used to evaluate the melt rate near the grounding line (which is defined as the first box in the 5-box setup of the box parameterisation).

⁵²⁵ uate the importance of the different variables in a situation close to the training condi-⁵²⁶tions. In the second variation (Fig. 6b), we use a random sample from the 4xCO₂ input ⁵²⁷for the shuffled variable and run the neural network using all other original input vari-⁵²⁸ables from the REPEAT1970 run to evaluate the importance of different variables in much ⁵²⁹warmer conditions. The shuffling is reiterated for each variable separately. In addition, ⁵³⁰we also shuffle blocks of potentially correlated variables simultaneously to gain insight ⁵³¹on the effect of correlation on the shuffling results.

For the shuffling within the REPEAT1970, the geometric properties dominate the 532 performance of all three neural networks for the integrated melt (Fig. 6a, left). For the 533 XS version, the ice-shelf size, for which the distance to the ice front could be seen as a 534 proxy, and the water column height, through ice-draft depth and bathymetry, have the 535 highest importance. For the S and L version, the bathymetry is less important but the 536 distance to the ice front and the ice-draft depth remain the most important variables, 537 with an effect on the RMSE decreasing from S to L. The shuffling of the temperature 538 and salinity variables have a smaller effect when shuffled separately, which can be ex-539 plained by the correlation between these variables. However, when shuffled by group, the 540 temperature information gains in importance, leading to a similar increase in RMSE as 541 the distance to the ice front in the L version. The bedrock and ice slopes are not impor-542 tant for the performance on the integrated melt. For the melt near the grounding line 543 (Fig. 6a, right), many variables are not important, the RMSE is reduced when they are 544

		Integrated mel [Gt/yr]	lt	Melt	near groundin [m ice/yr]	gline
	XS	S	L	XS	S	L
Original RMSE	17.6	18.9	16.5	0.42	0.36	0.40
(REPEAT 1970)						
		(a) Difference in F	RMSE to original	after shuffling v	vithin REPEAT19	70
Distance GL	2.5	2.2	-0.4	-0.05	-0.04	-0.06
Distance IF	15.4	15.5		0.03	0.06	0.05
Ice draft depth	20.4	18.8	10.5	0.02	-0.04	-0.02
Bathymetry	16.3	2.3	3.8	0.04	0.01	0.01
Slope bed lon	0.3	0.6	-0.2	-0.01	-0	-0.01
Slope bed lat	0.3	-0.2	0.1	0	0.01	0.01
Slope ice lon	0.4	1	0.5	0.02	0.05	0.03
Slope ice lat	0.1	0	-0	0.01	0.02	0.01
Temperature	4.7	5.2	5.2	0.09		
Salinity	9.4	8.2	1.3	-0.03	-0.01	0
Temperature mean	3.3	5.3	4.4	0.06		0.09
Salinity mean	4.9	3.2	3.6	0.01	0.02	0.03
Temperature std	0.7	0.9	0.5	0	-0.02	0.05
Salinity std	2.2	0.4	1.4	0.02	0.05	0.04
Position	14.2	19	13	-0.02	0.01	-0.01
Water column	14.7	18.9	6.9	-0.03	-0.01	-0.01
Slopes bed	0.6	0.2	0.1	-0.01	0	-0
Slopes ice	1.1	1.1	1	0.05	0.07	0.05
Temperature info	10.2			0.14	0.18	0.17
Salinity info	3.3	5.1	2.6	0.05	0.06	0.08

(b) Difference in RMSE to original after inserting random sample from 4xCO₂ into REPEAT1970

Distance GL	2.5	2.1	-0.4	-0.05	-0.03	-0.07
Distance IF	14.9	15	11.3	0.05	0.06	0.06
Ice draft depth	25.4	15.5	12.7	0.02	-0.04	-0.01
Bathymetry	16.7	2.4	4	0.04	0.01	0.01
Slope bed lon	0.3	0.5	-0.2	-0.01	0	-0.01
Slope bed lat	0.3	-0.1	0.1	0	0.01	0.01
Slope ice lon	0.4	1	0.5	0.02	0.04	0.03
Slope ice lat	0.2	0.2	-0.1	0.01	0.02	0.01
Temperature	179.7	151.7	85	-0.06	-0.01	-0.04
Salinity	51.1	115.2	10.1	0.08	0.04	0.05
Temperature mean	92.5	127.1	91.1	0.1	-0.06	-0.09
Salinity mean	120.9	377.4	55.3	-0.01	0.01	-0.01
Temperature std	12.9	1.9	13.2	-0	0.01	0.02
Salinity std	29.6	11.9	7.9	0.02	0.02	0.01
Position	13.9	18.6	13	-0.01	0.02	0
Water column	15.9	16.3	7.1	-0.03	-0	-0.01
Slopes bed	0.5	0.2	0.1	-0	0	0
Slopes ice	1.1	1.2	0.9	0.04	0.07	0.05
Temperature info	330.6	307.1	266.5	0.21		-0.03
Salinity info	20.7	95.8	3.2	0.07	0	0.06

Figure 6. Difference in RMSE between an application using a random sample for the given variable of the REPEAT1970 input (a) and of the $4xCO_2$ input (b) and the original application on the REPEAT1970 input using the XS, S and L deep ensemble. The original RMSE when applied to REPEAT1970 is indicated above each column. The upper part of the tables shows the results when shuffling the variables individually while the lower part is for variables that have been shuffled as a group. "Temperature" and "Salinity" are the ocean properties extrapolated to the ice-draft depth, "Temperature mean" and "Salinity mean" are their average over each cavity, and "Temperature std" and "Salinity std" their standard deviation over each cavity. In the block *Position* we group the distance to the grounding line and to the ice front, in the block *Water column* we group the ice-draft depth and the bathymetry, in the block *Slopes bed* and *Slopes ice* we group the meridional and zonal slope of the bedrock and ice respectively, in the block *Temperature info* and *Salinity info* we group the local value, the average and the standard deviation of temperature and salinity respectively.

shuffled. The strongest effect is seen when shuffling the temperature variables as a group.
The salinity variables, the ice slopes, and the distance to the ice front are the second most important group.

When inserting random samples of $4xCO_2$ input, the importance of the ice front, 548 the ice-draft depth and the bathymetry remains of a similar order of magnitude for the 549 integrated melt as in the REPEAT1970 shuffling (Fig. 6b, left). However, the effect of 550 the temperature increases drastically and leads to increases in the RMSE of more than 551 300 Gt/yr. For the XS and S, the importance of the grouped salinity information increases 552 553 as well. This result reflects the difficulty for neural networks to extrapolate outside of the training range. Looking at the distribution of the input variables, the geometrical 554 conditions in the $4xCO_2$ run are in a similar range as the training ensemble, despite an 555 involving ice-shelf geometry, while the temperature and salinity variables are clearly out-556 side of the distribution (Fig. A4). For the melt near the grounding line (Fig. 6b, right), 557 introducing variables from warmer conditions does not affect the RMSE very differently 558 than in the REPEAT1970 case. 559

Several conclusions can be drawn from this experiment. First, this experiment shows 560 that the geometry, in particular the distance to the ice front and the ice-draft depth, are 561 key variables for the neural networks to infer reasonable integrated melt when applied 562 on variables close to the training range, closely followed by the temperature. Ice-draft 563 depth and temperature already are an integral part of existing parameterisations (Burgard 564 et al., 2022). However, the distance to the ice-shelf front or the ice-shelf size are currently 565 only partly considered, and only in the more complex parameterisations such as the plume 566 and box parameterisations (Lazeroms et al., 2019; Reese et al., 2018). 567

Second, when applied to much warmer conditions, the distribution of geometric vari-568 ables remains close to their distribution in the training ensemble. In contrast, the tem-569 perature and salinity, well outside the training range, clearly affect the resulting inte-570 grated melt. This suggests that training the neural networks on simulations of warmer 571 conditions could already improve their performance. Even more promising, the low ef-572 fect of geometry changes on integrated melt in warmer conditions suggests that coupled 573 ice-ocean simulations of warmer conditions are not necessarily needed for training and 574 that cavity-opening ocean simulations with fixed geometry could already be sufficient. 575

Third, for the melt near the grounding line, the position of the grid cell is (maybe 576 surprisingly) less important than for the integrated melt and the key variable is the tem-577 perature information, both near the training range and in warmer conditions. While the 578 ice slope does not affect the integrated melt, it has some effect on the melt near the ground-579 ing line. This suggests that including ice slopes is necessary for a good performance near 580 the grounding line. However, the way it is currently included in simple parameterisations 581 is not successful as we showed in Burgard et al. (2022) that it leads to a clear overesti-582 mation of the melt in this region. 583

Fourth, the effect of the shuffling on the RMSE is generally lower for the L size of the neural networks. This could suggest an overfit as it could mean that the neural network is not following variations in the input variables as much as the other neural network sizes and is therefore less flexible. This possible overfit would also explain why we did not see an increase in the performance during the cross-validation with increasing network size in Sec. 3.

590 5.2 Possible improvements

While the results of our neural networks are encouraging, a variety of further improvements can be conducted in the future. The most obvious conclusion from this study is that predicting warmer conditions, similar to climate change conditions, is challenging for this particular neural network architecture because these conditions were not contained during training and neural networks are known to struggle with extrapolation problems. We therefore suggest, when possible, to introduce a set of simulations containing
high-end future scenarios in the training dataset to make the neural network more robust for future projections. At the same time, we saw that the traditional parameterisations struggle to represent future conditions as well. How to tune melt parameterisations to be applicable in both present and future conditions is therefore a problem that
is not limited to deep learning approaches.

Another possible improvement is the treatment of the largest ice shelves. When 602 looking at the cross-validation results into more detail, i.e. at the scale of each ice shelf 603 (not shown), the total RMSE over all ice shelves is strongly influenced by the high RMSE 604 for the Ross ice shelf and, to a smaller extent, by the relatively high RMSE for the Filchner-605 Ronne ice shelves. These two ice shelves have an area which is much larger than the other 606 ice shelves around Antarctica. Their cavities are so large that they develop their own 607 internal circulation (e.g. Gerdes et al., 1999; Naughten et al., 2021) and the residence 608 time of water masses reaches several years (Michel et al., 1979; Nicholls & Østerhus, 2004). 609 It is therefore not too surprising that parameterisations, which use input temperature 610 and salinity averaged over thousands of kilometers at the front of the ice shelves and do 611 not represent horizontal circulation explicitly, struggle with the representation of melt 612 in these cavities. If we remove these two from the RMSE in the $4xCO_2$ case for exam-613 ple, we find that the RMSE is clearly reduced for both neural networks and traditional 614 parameterisations (Fig. 7 compared to Fig. 4b). It would therefore be worth consider-615 ing whether these rather simple parameterisations are appropriate for the application 616 on the Ross and Filchner-Ronne ice shelves and if it would not be wiser to push efforts 617 towards the opening of these two cavities in ocean models, even at the lower resolution 618 of 1° , as was already done for NEMO in Smith et al. (2021) or Hutchinson et al. (2023). 619 On the same line, we suggest it is worth thinking about tuning the parameterisations 620 on the smaller ice shelves, and tuning the parameters and neural networks differently on 621 the larger ice shelves. 622

There is also space for improvement in the definition of input temperatures and 623 salinities. Like in Burgard et al. (2022), the input profiles of temperature and salinity 624 are here averaged over a given domain in front of the ice shelf. Then, we extrapolate the 625 properties to the ice-draft depth. To give the neural network more information about 626 the whole profile, we also gave it the mean and standard deviation of these extrapolated 627 temperature and salinity. However, machine learning gives us the opportunity to think 628 bigger than traditional statistics when representing information about a given domain. 629 One direction that could be explored in further development is the encoding of the im-630 portant information about the water masses in front of the ice shelf using a machine learn-631 ing technique. Ideally, this technique would take in a three-dimensional (horizontal plane 632 and depth), or even a four-dimensional (taking also time as input to account for lags and 633 residence time), field of temperature and salinity in front of the ice shelf and encode in-634 formation about this field in a format to be given to the neural network. Such encod-635 ing might contain more information about the spatial distribution of the properties in 636 front of the ice shelf and therefore potentially encode changes in the ocean circulation 637 which might change the circulation within the cavities, as expected to happen in warmer 638 conditions for the Filchner-Ronne ice shelf (Naughten et al., 2021). 639

Rosier et al. (2023) showed that a convolutional architecture can also be used to 640 infer basal melt rates from hydrographic and geometric properties. A convolutional ar-641 chitecture, often U-Nets, is the preferred choice in many current studies exploring the 642 application of machine learning to Earth System Sciences (e.g. Ebert-Uphoff & Hilburn, 643 2020; Andersson et al., 2021; Finn et al., 2023). In the case of basal melt and the ocean 644 circulation in the cavity, such architectures clearly make sense as they can capture spa-645 tial patterns and correlations. However, these architectures require much more simula-646 tion data for training as they take each time step as one training sample while our ap-647

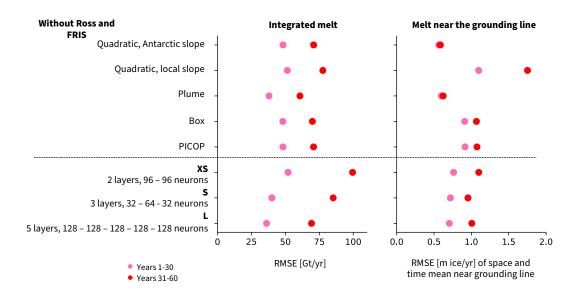


Figure 7. Summary of the RMSE of the integrated melt $(RMSE_{int})$ [in Gt/yr] and of the RMSE of the melt rate averaged over time and space near the grounding line $(RMSE_{GL})$ [in m ice/yr] computed on all ice shelves except Ross and Filchner-Ronne ice shelves for a selection of traditional parameterisations and a subsample of neural networks for the application on a simulation with 4xCO₂ forcing. The lighter colors represent the first 30 years of simulation and the darker colors the last 30 years of simulation.

proach takes each time step and grid cell as one training sample. Also, Rosier et al. (2023)
demonstrate the performance of their MELTNET in a fixed domain and have not yet
shown how to apply it to larger ice shelves than this domain. MELTNET remains however a promising approach and we are looking forward to its further development.

Finally, this study has focussed on the emulation of one ocean model at a given res-652 olution. We acknowledge that NEMO's simulation of basal melt rates is not a perfect 653 reflection of reality. Therefore, an interesting further direction to follow would be to train 654 a neural network to emulate NEMO at other resolutions and also to emulate other cavity-655 resolving ocean models. In this context, to ensure that the relationship remains sensi-656 ble, we suggest training separate emulators and using them as an ensemble. This would 657 provide an ensemble of emulators to be used as a variety of basal melt parameterisations, 658 in addition to physics-based parameterisations. In a context where basal melt remains 659 one of the main sources of uncertainty in projections of the Antarctic contribution to sea-660 level rise, a wide sample of this uncertainty in the form of a higher variety of parame-661 terisations is welcome. 662

663 6 Conclusions

In conclusion, we show that a rather simple neural network architecture can be used to emulate a cavity-resolving ocean model. Our multilayer perceptrons are designed to be rather simply usable as a basal melt parametrisation for ice-sheet modellers. They use input properties needed for the traditional parameterisations already and can be applied on the grid-cell level, similarly to most traditional parameterisations. While they struggle nearly as much as traditional parameterisations to generalise to ice shelves unseen during tuning, the neural networks generalise much better on time blocks unseen during training and the patterns are clearly better represented. In the demanding testing phase, on a dataset produced with different NEMO parameters, geometry perturbations unseen during training and different forcing, they still perform at least as well or even better than traditional parameterisations, both in historical and much warmer conditions.

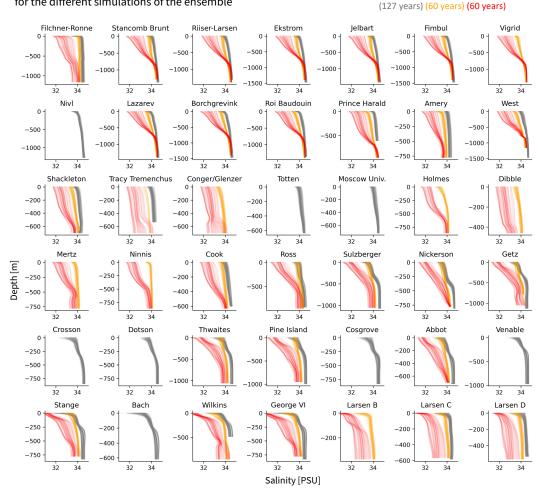
These results are promising as neural networks and machine learning in general are topics that have been gaining lots of traction lately and efforts are done in many disciplines of the Earth System Sciences to explore their application. In this study, we provide guiding thoughts for further exploration and refinement of this approach, while this first proof of concept can already be used as an additional parameterisation in the icesheet modelling landscape.

Appendix A Distributions of variables of interest in the training and testing ensemble



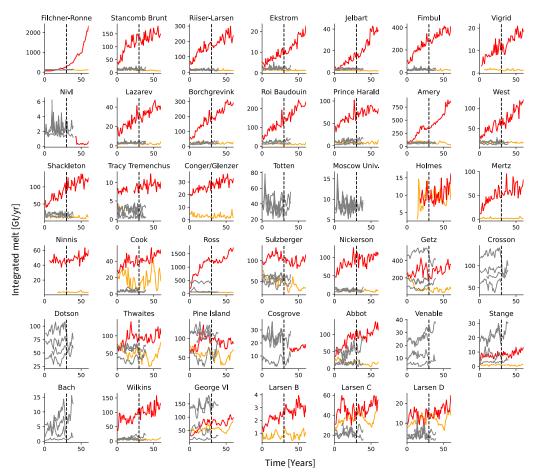
Figure A1. Input profiles of temperature for the different ice shelves. Profiles of the training ensemble are shown in grey, profiles for the REPEAT1970 run in orange and profiles for the $4xCO_2$ run in red.

TRAINING DATA REPEAT1970 4xCO2



Salinity profiles over 50 km in front of the ice shelf for the different simulations of the ensemble

Figure A2. Input profiles of salinity for the different ice shelves. Profiles of the training ensemble are shown in grey, profiles for the REPEAT1970 run in light blue and profiles for the $4xCO_2$ run in dark blue.



Integrated melt over time

TRAINING DATA REPEAT1970 4xCO2 (127 years) (60 years) (60 years)

Figure A3. Timeseries of the integrated melt for the different ice shelves. The training ensemble is shown in grey, the REPEAT1970 run in orange and the $4xCO_2$ run in red. The black dashed line limits the first and second 30-year block used in Sec. 4 for the $4xCO_2$ run

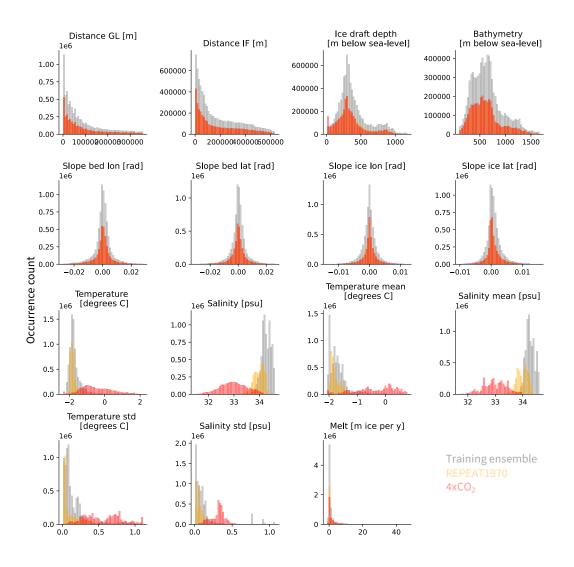


Figure A4. Distribution (occurrence count) of the different input variables and the melt over the training ensemble (grey), the REPEAT1970 run (orange) and the $4xCO_2$ run (red).

⁶⁸⁴ Open Research

The simulation data from Burgard et al. (2022) used for the training ensemble can be found on Zenodo: https://doi.org/10.5281/zenodo.7308352. The simulation data from (Smith et al., 2021) used for the testing ensemble will be uploaded on Zenodo as soon as possible. All code to train the neural networks and produce the figures can be found on Github: https://github.com/ClimateClara/basal_melt_neural_network and will be uploaded to Zenodo upon paper acceptance.

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CB and NCJ developed the original idea of this paper. CB carried out all analyses and wrote the manuscript. PM carried out the NEMO simulations used for training and RSS carried out the UKESM simulations. NCJ, RS and JC provided valuable help and code for the definition of the ice-shelf masks when the ice shelves evolve over time. TSF provided methodological input on the training of neural networks and JEJ provided useful input about how to think about machine learning. CB, NCJ, PM, RS, RSS, JC, TSF, JEJ contributed to discussions.

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